# EFT approach to the electron EDM at the two-loop level

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based on GP, A. Pomarol, M. Riembau 1810.09413 GP, M. Riembau, T. Vantalon 1712.06337

### The precision frontier

**Precision measurements** provide fundamental tests of the **SM** 

... which means they can probe **new physics** 

They can significantly extend the reach of direct searches

- access hard-to-test parameter space points
- extend reach to new physics at higher energy scales
- Particularly relevant since no convincing direct signal of new physics has been seen at the LHC

### The electron EDM

Excellent probes of new physics are provided by the **Electric Dipole Moment** (EDM) of the electron

- I. predicted to be very small in the SM
- 2. usually enhanced in the presence of new physics
- 3. very well tested experimentally



### The electron EDM in the SM

EDM generated from radiative corrections with CP-violating interactions

In the **SM** the electron EDM is **extremely small** 

$$d_e < 10^{-38} e \text{ cm}$$

- vanishing up to 3 loops [Khriplovich, Pospelov '91]
- severe cancellations due to GIM mechanism



### The electron EDM beyond the SM

BSM physics typically gives rise to additional contributions to EDMs

- additional sources of CP-violation
- cancellations are typically not present
- contributions can arise at low loop level (eg. I-loop or 2-loop)

typical contribution to the electron EDM in the MSSM





BSM corrections much larger than SM prediction

#### The experimental bounds



## The EFT approach

LHC results provide a strong hint that new physics scale should be well above the EW scale

If new physics is heavy, we can adopt the **Effective Field Theory** (EFT) language

- model independent
- bounds easy to be recast in explicit theories

New-physics effects encoded in deformations of the SM Lagrangian

$$\mathcal{L} = \mathcal{L}_{\rm SM} + \sum_{i} \frac{c_i^{(6)}}{\Lambda^2} \mathcal{O}_i^{(6)} + \sum_{i} \frac{c_i^{(8)}}{\Lambda^4} \mathcal{O}_i^{(8)} + \cdots$$

leading corrections from dimension-6 operators  $\mathcal{O}_i^{(6)}$ 

### EDMs in the EFT language

EDMs can be reinterpreted in terms of high-energy effective operators

$$H = -\mu \vec{B} \cdot \frac{\vec{S}}{S} - d \vec{E} \cdot \frac{\vec{S}}{S}$$
relativistic limit
$$\mathcal{L}_{dipole} = -\frac{\mu}{2} \overline{\Psi} \sigma^{\mu\nu} F_{\mu\nu} \Psi - \frac{d}{2} \overline{\Psi} \sigma^{\mu\nu} i \gamma^5 F_{\mu\nu} \Psi$$

$$\int SM: SU(2)_{L} \times U(1)_{Y}$$

$$\mathcal{L} = \frac{c_{eW}}{\Lambda^2} \left( \bar{\ell}_L \sigma^{\mu\nu} \sigma^a e_R \right) HW^a_{\mu\nu} + \frac{c_{eB}}{\Lambda^2} \left( \bar{\ell}_L \sigma^{\mu\nu} e_R \right) HB_{\mu\nu}$$

$$d_e(\mu) = \frac{\sqrt{2}v}{\Lambda^2} \operatorname{Im} \left[ s_{\theta_W} C_{eW}(\mu) - c_{\theta_W} C_{eB}(\mu) \right]$$

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SM: SU(2)L×U(1)Y
$$\mathcal{L} = \frac{c_{eW}}{\Lambda^2} \left( \bar{\ell}_L \sigma^{\mu\nu} \sigma^a e_R \right) H W^a_{\mu\nu} + \frac{c_{eB}}{\Lambda^2} \left( \bar{\ell}_L \sigma^{\mu\nu} e_R \right) H B_{\mu\nu}$$

$$d_e(\mu) = \frac{\sqrt{2}v}{\Lambda^2} \text{Im} \left[ s_{\theta_W} C_{eW}(\mu) - c_{\theta_W} C_{eB}(\mu) \right]$$

# Classifying EFT effects

A preliminary step to apply the EFT approach is to **identify and organize** the most relevant new-physics effects

Classification criteria:

- Ioop order (we will consider affects up to 2 loops)
- additional enhancement from running (large log if there is a significant mass gap)
- power counting

#### Selection rules for RGEs

Running effects are controlled by several selection rules

[ Elias-Miro, Espinosa, Pomarol '14; Cheung, Shen '15 ]



Note: four-fermion operators in Weyl notation

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#### **Classifying RGE contribution**

#### I-loop RGE



**Only one 4-fermion operator**  $\psi^4$  contributes at 1-loop



• The structure of the other four-fermion operators does not allow for I-loop diagrams

#### I-loop RGE



Operators involving the Higgs and gauge bosons  $\mathcal{O}_{W\widetilde{W}} = |H|^2 W^{a\,\mu\nu} \widetilde{W}^a_{\mu\nu} \qquad \mathcal{O}_{B\widetilde{B}} = |H|^2 B^{\mu\nu} \widetilde{B}_{\mu\nu} \qquad \mathcal{O}_{W\widetilde{B}} = (H^{\dagger} \sigma^a H) W^{a\,\mu\nu} \widetilde{B}_{\mu\nu}$   $\stackrel{\text{proportional to}}{\overset{\text{electron Yukawa}}{\overset{\text{d}}{d \ln \mu}} \operatorname{Im} \begin{pmatrix} C_{eB} \\ C_{eW} \end{pmatrix} = -\frac{y_e g}{16\pi^2} \begin{pmatrix} 0 & 2t_{\theta_W} (Y_L + Y_e) & \frac{3}{2} \\ 1 & 0 & t_{\theta_W} (Y_L + Y_e) \end{pmatrix} \begin{pmatrix} C_{W\widetilde{W}} \\ C_{B\widetilde{B}} \\ C_{W\widetilde{B}} \end{pmatrix}$ 



Additional 4-fermion operator  $\psi^4$  contributes at 2-loop double log





**Dipole operators**  $H\psi'^2F$  contribute at 2-loop double log

Two RGE patterns:

• through the 
$$H^2 F^2$$
 operators  

$$\frac{d}{d \ln \mu} C_{W\widetilde{W}} = -\frac{2g}{16\pi^2} \operatorname{Im} \left[ y_{e'} C_{e'W} + y_u N_c C_{uW} + y_d N_c C_{dW} \right]$$

$$\frac{d}{d \ln \mu} C_{B\widetilde{B}} = -\frac{4g'}{16\pi^2} \operatorname{Im} \left[ y_{e'} (Y_L + Y_e) C_{e'B} + y_u N_c (Y_Q + Y_u) C_{uB} + y_d N_c (Y_Q + Y_d) C_{dB} \right]$$

$$\frac{d}{d \ln \mu} C_{W\widetilde{B}} = -\frac{2g}{16\pi^2} \operatorname{Im} \left[ 2t_{\theta_W} \left( y_{e'} (Y_L + Y_e) C_{e'W} - y_u N_c (Y_Q + Y_u) C_{uW} + y_d N_c (Y_Q + Y_d) C_{dW} \right) + y_{e'} C_{e'B} - y_u N_c C_{uB} + y_d N_c C_{dB} \right]$$



**Dipole operators**  $H\psi'^2F$  contribute at 2-loop double log

Two RGE patterns:

- through the  $H^2F^2$  operators
- through the  $\mathcal{O}_{luqe}$  operator

$$\frac{d}{d\ln\mu}C_{luqe} = \frac{g\,y_e}{16\pi^2} \Big[ -8t_{\theta_W}(Y_L + Y_e)C_{uB} + 12C_{uW} \Big]$$





 $F^{3} \text{ operator}$  $\mathcal{O}_{\widetilde{W}} = \varepsilon_{abc} \widetilde{W}_{\mu}^{a\,\nu} W_{\nu}^{b\,\rho} W_{\rho}^{c\,\mu}$ 

• finite I-loop contributions

$$\operatorname{Im}[C_{eW}] = \frac{3}{64\pi^2} y_e g^2 C_{\widetilde{W}}$$





• 2-loop contributions dominant for  $\Lambda > 5 \,\mathrm{TeV}$ 

JW/B

 $e_R$ 

### 2-loop single-log RGE



**4-fermion operators**  $\psi^2 \overline{\psi}^2$  contribute at 2-loop single log

$$\mathcal{O}_{le\bar{d}\bar{q}} = (\bar{L}_L e_R)(\bar{d}_R Q_L) \qquad \mathcal{O}_{le\bar{e}'\bar{l}'} = (\bar{L}_L e_R)(\bar{e}'_R L'_L)$$

 $\frac{d}{d\ln\mu} \operatorname{Im} \begin{pmatrix} C_{eB} \\ C_{eW} \end{pmatrix} = \frac{y_{e'}g^3}{(16\pi^2)^2} \frac{1}{4} \begin{pmatrix} 3t_{\theta_W}Y_L + 4t_{\theta_W}^3(Y_L + Y_e)(Y_L^2 + Y_e^2) \\ \frac{1}{2} + 2t_{\theta_W}^2(Y_L + Y_e)Y_L \end{pmatrix} C_{le\bar{e'}\bar{l'}}$   $\frac{d}{d\ln\mu} \operatorname{Im} \begin{pmatrix} C_{eB} \\ C_{eW} \end{pmatrix} = \frac{y_dg^3}{(16\pi^2)^2} \frac{N_c}{4} \begin{pmatrix} 3t_{\theta_W}Y_Q + 4t_{\theta_W}^3(Y_L + Y_e)(Y_Q^2 + Y_d^2) \\ \frac{1}{2} + 2t_{\theta_W}^2(Y_L + Y_e)Y_Q \end{pmatrix} C_{le\bar{d}\bar{q}}$   $L_{L} = \frac{1}{2} + 2t_{\theta_W}^2(Y_L + Y_e)Y_Q + \frac{1}{2} + 2t_{\theta_W}^2(Y_L + Y_e)Y_Q + \frac{1}{2} + 2t_{\theta_W}^2(Y_L + Y_e)Y_Q + \frac{1}{2} + \frac{1}$ 

- cancellation suppresses leading contributions to electron EDM, only hypercharge terms survive  $q^2 
ightarrow q'^2/8$ 

## 2-loop single-log RGE



Electron Yukawa corrections contribute at 2-loop single log

$$\mathcal{O}_{y_e} = |H|^2 \bar{L}_L e_R H$$

$$\frac{d}{d \ln \mu} \begin{pmatrix} C_{eB} \\ C_{eW} \end{pmatrix} = \frac{g^3}{(16\pi^2)^2} \frac{3}{4} \begin{pmatrix} t_{\theta_W} Y_H + 4t_{\theta_W}^3 Y_H^2 (Y_L + Y_e) \\ \frac{1}{2} + \frac{2}{3} t_{\theta_W}^2 Y_H (Y_L + Y_e) \end{pmatrix} C_{y_e}$$

$$\int_{cancellation suppresses leading contributions to electron EDM, only hypercharge terms survive}$$

$$g^2 \rightarrow g'^2$$

#### EW scale threshold corrections

Additional contribution generated at the EW scale can be relevant

**Example:** threshold effects from Yukawa couplings (from finite Barr-Zee-type diagrams)

• Electron Yukawa

$$\frac{d_e}{e} \simeq -\frac{16}{3} \frac{e^2}{(16\pi^2)^2} v \left(2 + \ln\frac{m_t^2}{m_h^2}\right) \frac{\mathrm{Im}\,C_{y_e}}{\Lambda^2}$$

larger than log-enhanced contributions for  $\Lambda \lesssim 10^3 {
m ~TeV}$ 

• Top Yukawa

$$\frac{d_e}{e} \simeq -\frac{e^2}{(16\pi^2)^2} 4N_c Q_t^2 \frac{m_e}{m_t} v \left(2 + \ln\frac{m_t^2}{m_h^2}\right) \frac{\mathrm{Im}\,C_{y_t}}{\Lambda^2}$$

no contribution from running

#### Implications for BSM

Model-independent constraints

#### Constraints from ACME II

ACME II results translate to very strong constraints on CP-violating effective operators



two-	loops	finite
000.	loopp	1111100

$C_{y_e}$	$14 y_e \lambda_h$	
$C_{y_t}$	$14 y_t \lambda_h$	
$C_{y_b}$	$2.9 \times 10^3 y_b \lambda_h$	
$C_{y_{\tau}}$	$3.4 \times 10^3 y_\tau \lambda_h$	

Obtained by fixing  $\Lambda = 10 \,\mathrm{TeV}$  and considering 3-rd generation fermions

### Estimating BSM effects

Classification in weakly-coupled renormalizable BSM theories



Generated at **loop**:

$$C_{fV} \sim \frac{g_*^3 g}{16\pi^2}$$
,  $C_{V\widetilde{V}} \sim \frac{g_*^2 g^2}{16\pi^2}$   $C_{\widetilde{W}} \sim \frac{g_*^2 g^3}{(16\pi^2)^2}$   
I-loop 2-loops

#### Constraints from electron mass

To keep under control I-loop corrections to the electron mass

$$\left\{\frac{C_{eV}v}{16\pi^2} , \frac{C_{y_e}v^3}{\Lambda^2} , \frac{C_{lequ}m_u}{16\pi^2} , \frac{C_{luqe}m_u}{16\pi^2} , \frac{C_{luqe}m_u}{16\pi^2} , \frac{C_{le\bar{d}\bar{q}}m_d}{16\pi^2} , \frac{C_{le\bar{e}\bar{l}}m_{e'}}{16\pi^2}\right\} \lesssim m_e$$

Automatically satisfied in MFV-like theories

$$C_{fV} \propto y_f$$
,  $C_{y_e} \propto y_e$ ,  $C_{lequ} \propto y_e y_u$ ,  $C_{luqe} \propto y_e y_u$ ,  $C_{le\bar{d}\bar{q}} \propto y_e y_d$ ,  $C_{le\bar{e}'\bar{l}'} \propto y_e y_{e'}$ 

• chirality-flipping operators are proportional to Yukawa couplings

#### Contributions to the electron EDM

Hierarchy of effects taking into account power-counting

I loop log :  $\mathcal{O}_{luqe}$ 

I loop :  $\mathcal{O}_{eV}$ 



**3 loop** :  $\mathcal{O}_{\widetilde{W}}$ 

#### Constraints from ACME II

Constraints taking into account power-counting



( obtained by fixing  $g_* = 1$  )

#### Implications for BSM

Constraints on specific BSM theories

#### Leptoquarks

#### Scalar leptoquarks

 $u_R$ 

 $L_L$ 

 $R_2, S_1$ 

 $e_R$ 

 $Q_L$ 

Contribute to 4-fermion operators

• The R<sub>2</sub> leptoquark (3, 2, 7/6)

• The S<sub>1</sub> leptoquark  $(\overline{3}, 1, 1/3)$ 

#### Vector leptoquarks

Directly contribute to  $\mathcal{O}_{eW}$ ,  $\mathcal{O}_{eB}$ 



• The V<sub>2</sub> leptoquark  $(\overline{3}, 2, 5/6)$ 

$$\mathcal{L} = x_2^{RL} \overline{b}_R^C \gamma^{\mu} V_{2,\mu}^a \varepsilon^{ab} L_{L_1}^b + x_2^{LR} \overline{Q}_{L_3}^{C\,a} \gamma^{\mu} \varepsilon^{ab} V_{2,\mu}^b e_R + \text{h.c.}$$

$$m_{V_2} \gtrsim \mathbf{5.5 \, TeV} \sqrt{rac{\operatorname{Im}(x_2^{LR} x_2^{RL\star})}{y_e y_b}}$$

• The U<sub>1</sub> leptoquark (3, 1, 2/3)

$$\mathcal{L} = x_1^{LL} \overline{Q}_{L_3}^a \gamma^\mu U_{1,\mu} L_{L_1}^a + x_1^{RR} \overline{b}_R \gamma^\mu U_{1,\mu} e_R + \text{h.c.}$$
$$m_{U_1} \gtrsim \mathbf{2.5 \, TeV} \sqrt{\frac{\text{Im}(x_2^{RR} x_2^{LL \star})}{y_e y_b}}$$

#### SUSY

#### Constraints on electron partners



• Simple results in the limit of heavy partners

Strong constraint on mass of electron superpartners

 $m_{\tilde{\ell}} \gtrsim 25 \ (50) \text{ TeV}$  for  $m_{\tilde{\ell}} = M_2 = \mu \ (m_{\tilde{\ell}} \gg M_2 = \mu)$ 

#### Constraints on the stop

2-loop effects through Barr-Zee diagrams



• Can also be interpreted as running induced by AFF operator

Strong constraint on stop mass

 $m_{\tilde{t}} \gtrsim 5 \text{ TeV}$ 

for  $\tan \beta \sim \sin \arg(\mu A_t) \sim 1$ ,  $m_A \sim \mu \sin A_t \sim 1 \text{ TeV}$ 

#### Constraints from heavy EW-inos

Heavy electroweak-inos contribute to HHFF operators



$$C_{loop} \equiv \frac{g^4 \sin 2\beta \sin \varphi}{16\pi^2 |M_2\mu|}, \quad \varphi = \arg[m_{12}^2 \mu^* M_2^*], \quad \rho \equiv |M_2/\mu|^2$$

#### ACME II bounds

 $\sqrt{|M_2\mu|} \gtrsim 4 \,\mathrm{TeV}$ 

for  $\tan \beta \sim 1$  and O(1) CP-violating phases

### Squark-selectron-gauginos loop

Contribution to  $\mathcal{O}_{luqe}$  via squark-selectron-gauginos loop



Strong bounds on superpartner mass scale

 $m_i \gtrsim 7.5 \,\mathrm{TeV}$ 

for degenerate superpartner masses and  $\sin \arg(\mu M_2) / \sin 2\beta \sim 1$ 

#### Composite Higgs

#### Anarchic composite Higgs

Anarchic flavor models generate lepton EDMs at 1-loop level (through the exchange of heavy vectors and electron partners)



### Multi-scale composite Higgs

CP-violating effects can be drastically reduced in multi-scale models

[G.P., Pomarol '16]



Yukawa's for each family generated at different energy scales



### Multi-scale composite Higgs

CP-violating effects can be drastically reduced in **multi-scale models** 

[G.P., Pomarol '16]



High energy scale suppresses flavour effects

▶ negligible EDMs

Main flavor effects from top

#### Bounds on top partners

Main contribution to the electron EDM from top parters

2-loop Barr-Zee diagrams  $c_t$   $t_L$  (h)  $C_t$  (h) T (h)  $d_e$   $(Im c_t) \sin \theta \frac{m_{top}}{m_T^2} \log \frac{m_{top}^2}{m_T^2}$   $(Im c_t) \sin \theta \frac{m_{top}}{m_T^2} \log \frac{m_{top}^2}{m_T^2}$ 

#### Strong bounds on top partners mass scale

 $m_T \gtrsim 20 \text{ TeV}$ 

for Im  $c_t \sim 1$  and  $\sin \theta \sim O(1)$ 

#### Comparison with direct searches

#### **Constraints from ACME II**

**HL-LHC** projections



#### Conclusions

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The electron EDM provides an excellent way to probe new physics

- clean observable, with strong sensitivity to new CP-violating sources
- can test new-physics at the IOTeV scale even with 2-loop effects

New-physics effects can be cleanly classified within an EFT framework



#### Outlook



Experimental bounds steadily improved in the past years

#### Outlook



- Experimental bounds steadily improved in the past years
- Significant boost is expected in the near future

probe most BSM models well beyond the 10<sup>2</sup> TeV scale