



HIGH PRECISION PHENOMENOLOGY OF THE HIGGS BOSON

HUMBOLDT-UNIVERSITÄT ZU BERLIN AND DESY SEMINAR



**Universität
Zürich^{UZH}**

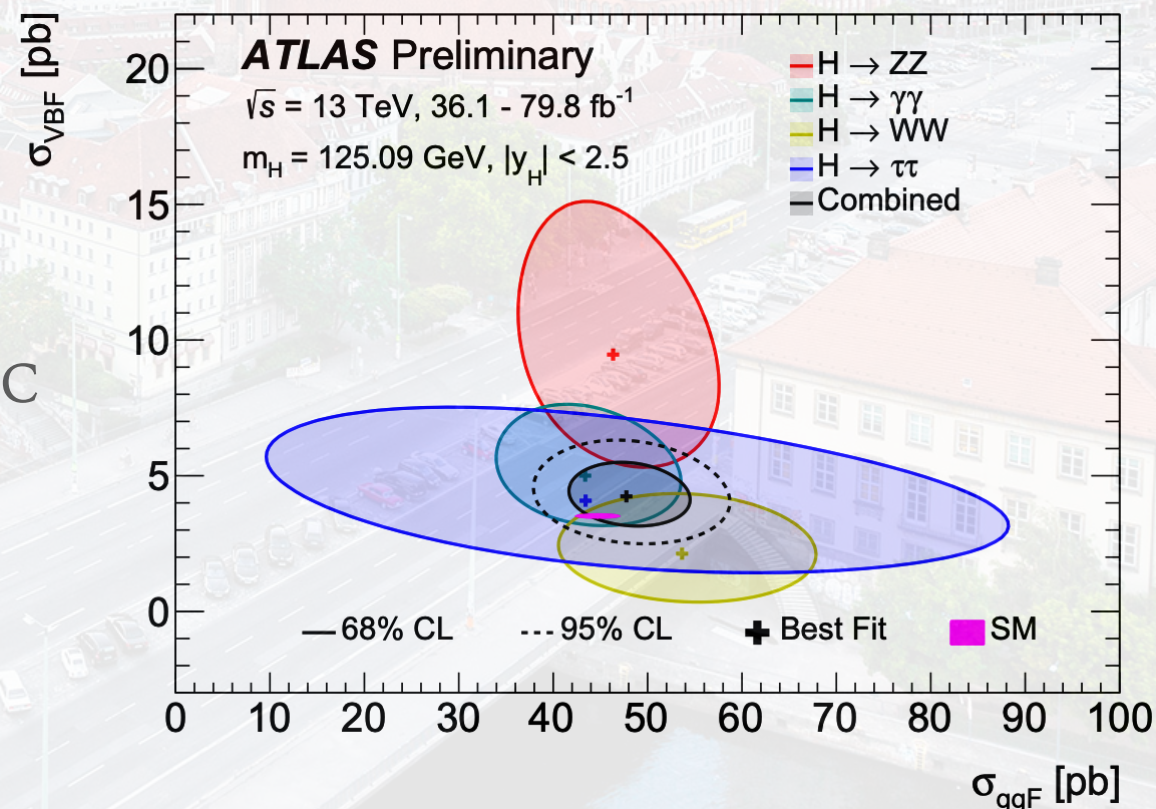
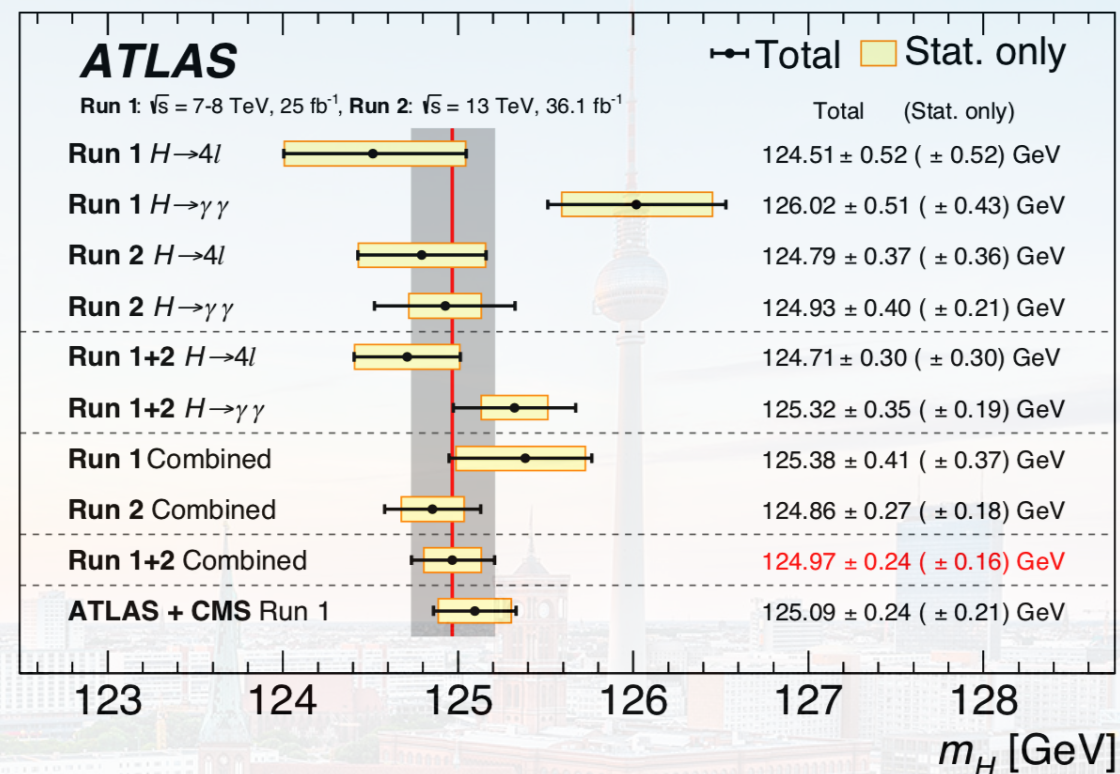
*Xuan Chen
Physik-Institut, Universität Zürich
Berlin, Germany, December 05, 2019*

OUTLINE

- Precision measurements and predictions of the Higgs boson
 - Current status from both theory and experiment (cherry pick)
 - Projection of HL-LHC, is it precise enough?
- Precision QCD calculations in the past, present and future
 - Roadmap of NNLO
 - Roadmap of N3LO
- Higgs production and decay processes in NNLOJET
- Higgs transverse momentum distribution in full spectrum
 - Small, medium and boosted regions
- Higgs rapidity distribution at N3LO (ggF channel)
- Future work & Summary

SUCCESS OF LHC HIGGS EXPERIMENTS

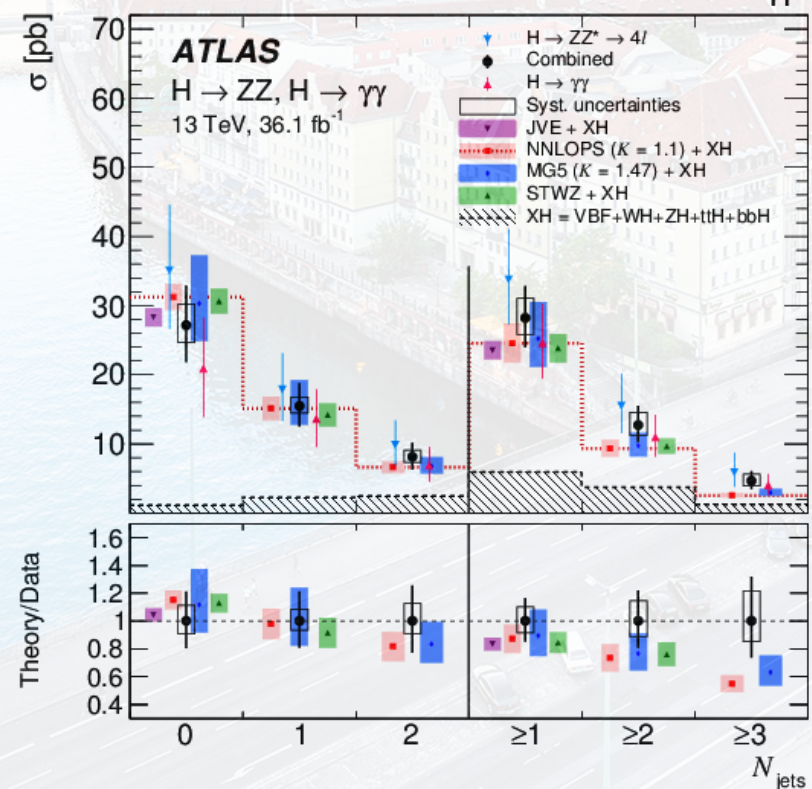
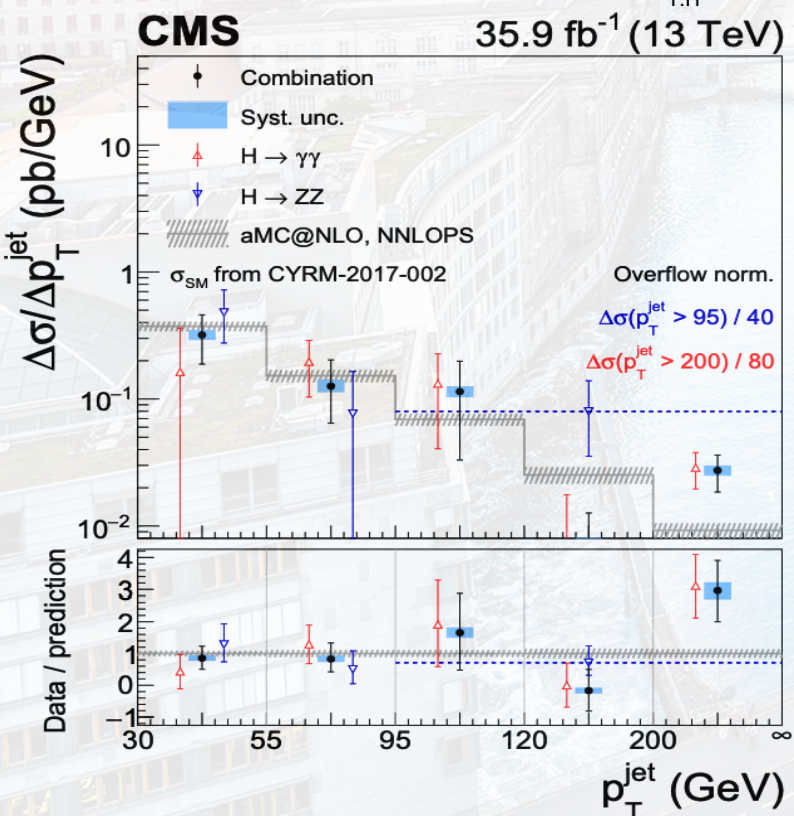
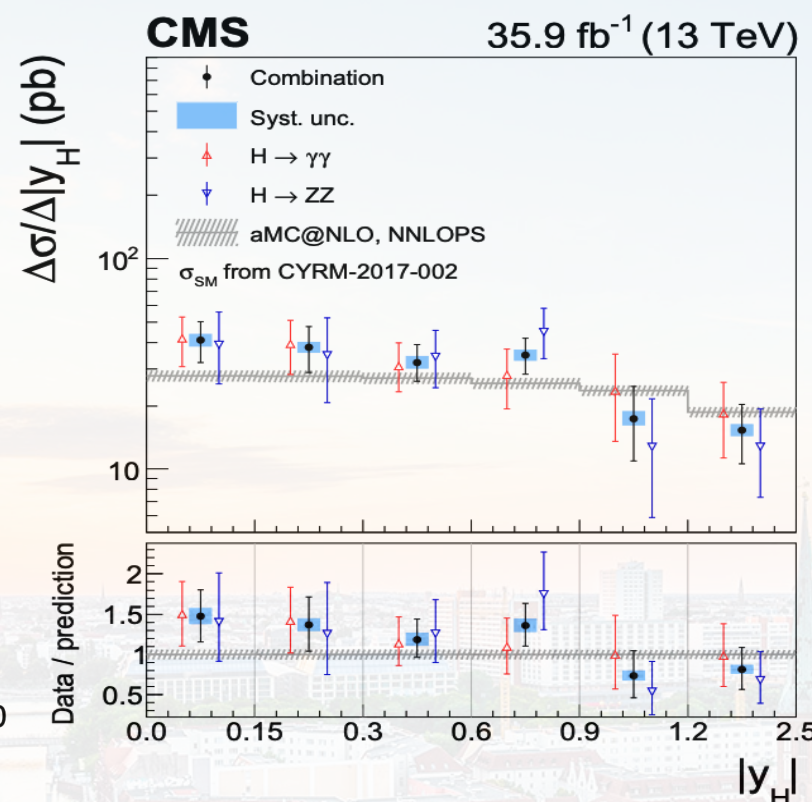
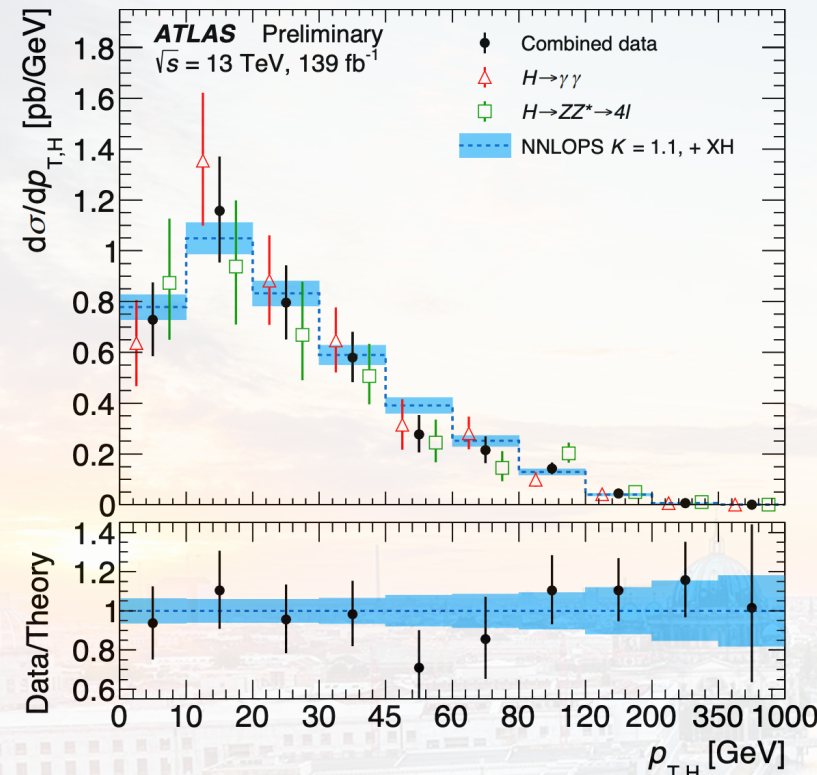
- Higgs boson properties in agreement with SM
 - Bosonic (Run I) and 3rd generation fermionic couplings (Run II) observed with current precision on coupling $\pm 10\text{-}20\%$ (EPS2019)
- Higgs mass uncertainty at $\pm 0.2\%$ level (Run I + II)
- Fiducial total cross section measured with $\pm 9\%$ accuracy (Run I + II)
- 2nd generation fermion couplings still to be established
- HH signal with 10 times SM exclusion limit
- Goal for the future: explore full potential of the LHC
 - Differential in production and decay channels
 - Projection to HL-LHC (estimate challenge)
 - Accelerate searches of new physics



1806.00242

ATLAS-CONF-2018-031

SUCCESS OF LHC HIGGS EXPERIMENTS

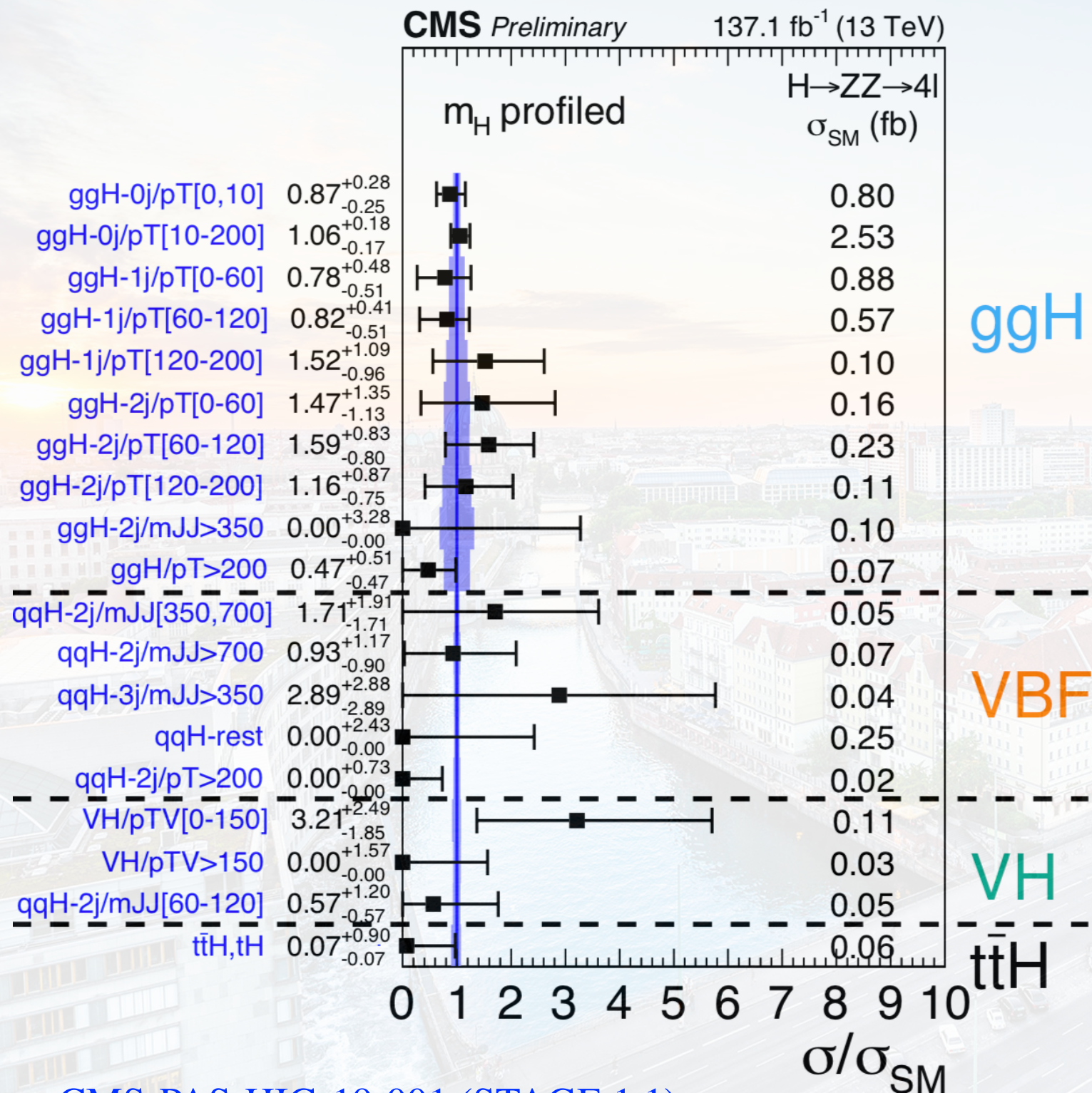


- Typical differential observables for Higgs (+jet) are:

$$\frac{d\sigma}{dp_T^H}, \frac{d\sigma}{d|y^H|}, \frac{d\sigma}{dp_T^{j1}}, \frac{d\sigma}{dN_{jets}}$$
- Inclusive decay observables are reconstructed from individual decay channel
- Combined results with $\pm 20\text{-}40\%$ uncertainties (EPS2019)
[\(ATLAS 1805.10197, CMS 1812.06504, ATLAS-CONF-2019-032\)](#)
- Breakdown in production channels through Simplified Template Cross Section (STXS)
- All Higgs production and decay channels contribute
- Complexity increase from Stage

0 → 1 → 1.1 → ... → 2

SUCCESS OF LHC HIGGS EXPERIMENTS



CMS-PAS-HIG-19-001 (STAGE 1.1)

- Typical differential observables for Higgs (+jet) are:

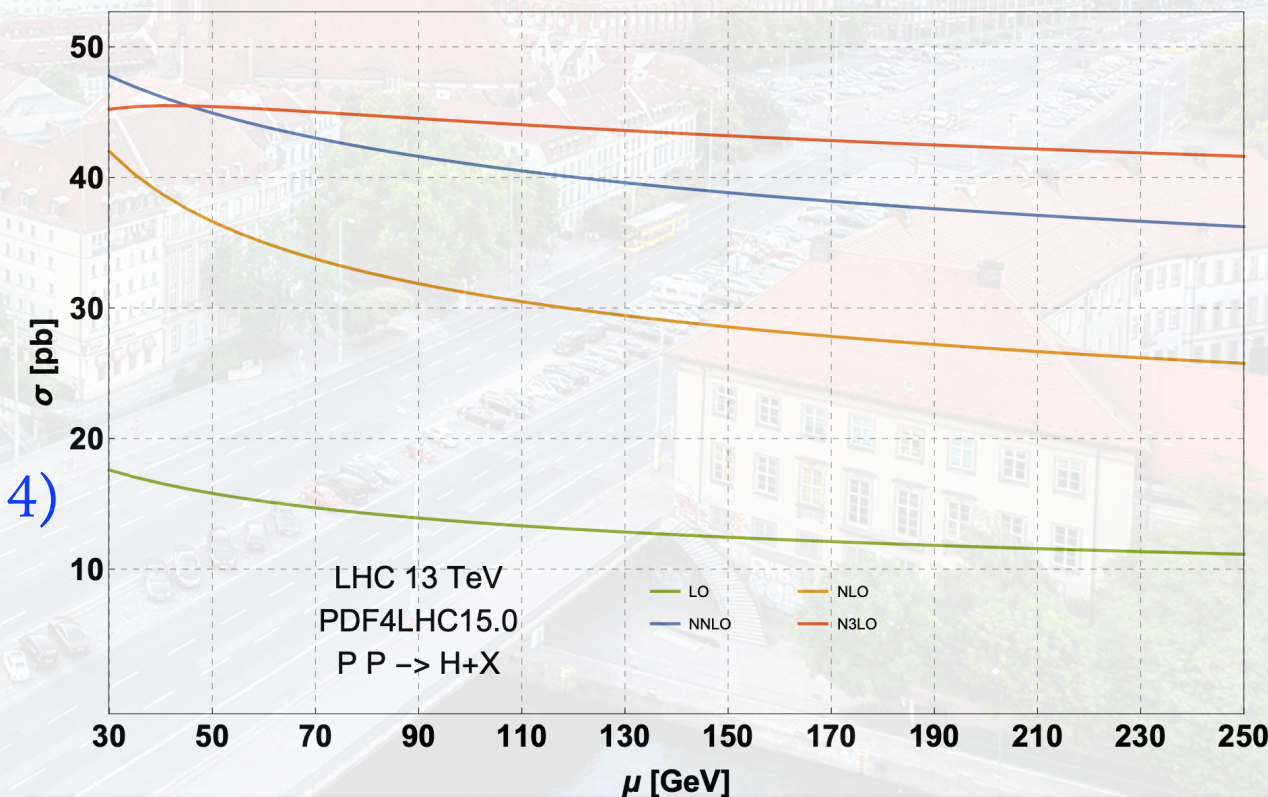
$$\frac{d\sigma}{dp_T^H}, \frac{d\sigma}{d|y^H|}, \frac{d\sigma}{dp_T^{j1}}, \frac{d\sigma}{dN_{jets}}$$
- Inclusive decay observables are reconstructed from individual decay channel
- Combined results with $\pm 30\text{-}50\%$ uncertainties
 (ATLAS 1805.10197, CMS 1812.06504, ATLAS-CONF-2019-032)
- Breakdown in production channels through Simplified Template Cross Section (STXS)
- All Higgs production and decay channels contribute
- Complexity increase from Stage
 $0 \rightarrow 1 \rightarrow 1.1 \rightarrow \dots \rightarrow 2$

SUCCESS OF HIGGS THEORY (GLUON FUSION)

$\sigma_{PP \rightarrow H+X}$	=	16.00 pb	(+32.87%)	LO, rEFT
	+	20.84 pb	(+42.82%)	NLO, rEFT
	+	9.56 pb	(+19.64%)	NNLO, rEFT
	+	1.62 pb	(+3.32%)	N ³ LO, rEFT
	-	2.07 pb	(-4.25%)	(t,b,c) corr. to exact NLO
	+	0.34 pb	(+0.70%)	$1/m_t$ corr. to NNLO
	+	2.37 pb	(+4.87%)	EWK corr.
	=	48.67 pb.		

$\delta(\text{theory})$	=	$+0.13pb$ $-1.20pb$	$(+0.28\%)$ (-2.50%)	$\delta(\text{scale})$
	+	$\pm 0.56pb$	$(\pm 1.16\%)$	$\delta(\text{PDF-TH})$
	+	$\pm 0.49pb$	$(\pm 1.00\%)$	$\delta(\text{EWK})$
	+	$\pm 0.41pb$	$(\pm 0.85\%)$	$\delta(t,b,c)$
	+	$\pm 0.49pb$	$(\pm 1.00\%)$	$\delta(1/m_t)$
	=	$+2.08pb$ $-3.16pb$	$(+4.28\%)$ (-6.5%)	
$\delta(\text{PDF})$	=	$\pm 0.89pb$	$(\pm 1.85\%)$	
$\delta(\alpha_s)$	=	$+1.25pb$ $-1.26pb$	$(+2.59\%)$ (-2.62%)	

- Total cross section with N3LO QCD corrections in heavy top limit (HTL) ([B. Mistlberger 1802.00833](#))
- QCD scale variation reduced significantly
- Public in iHixs2 code ([Dulat et al. 1802.00827](#))
- Uncertainty dominant by QCD ($\pm 4\%$) ([C. Anastasiou et al. 1602.00695](#))
- Three **short boards** of accuracy: QCD scale, PDF, α_s

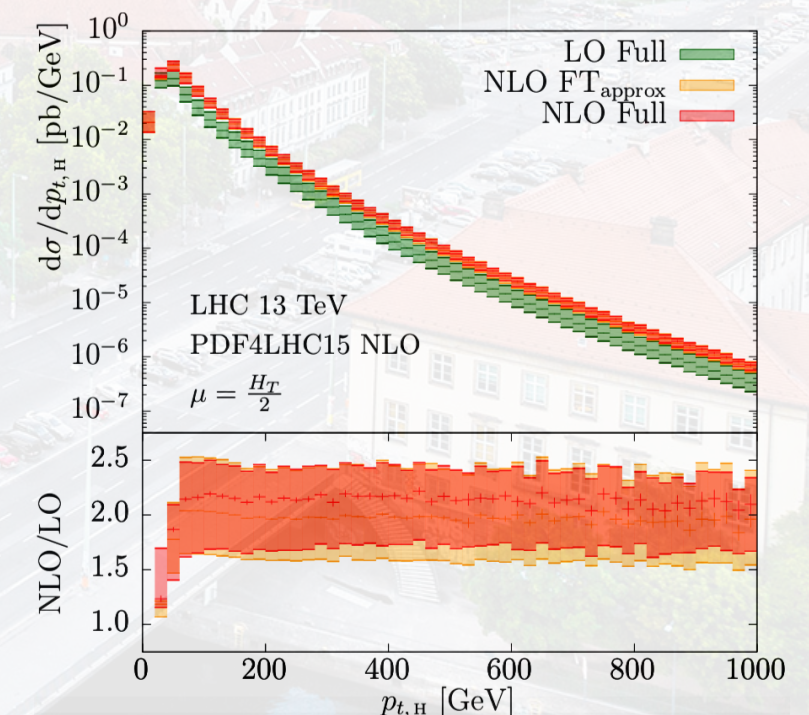
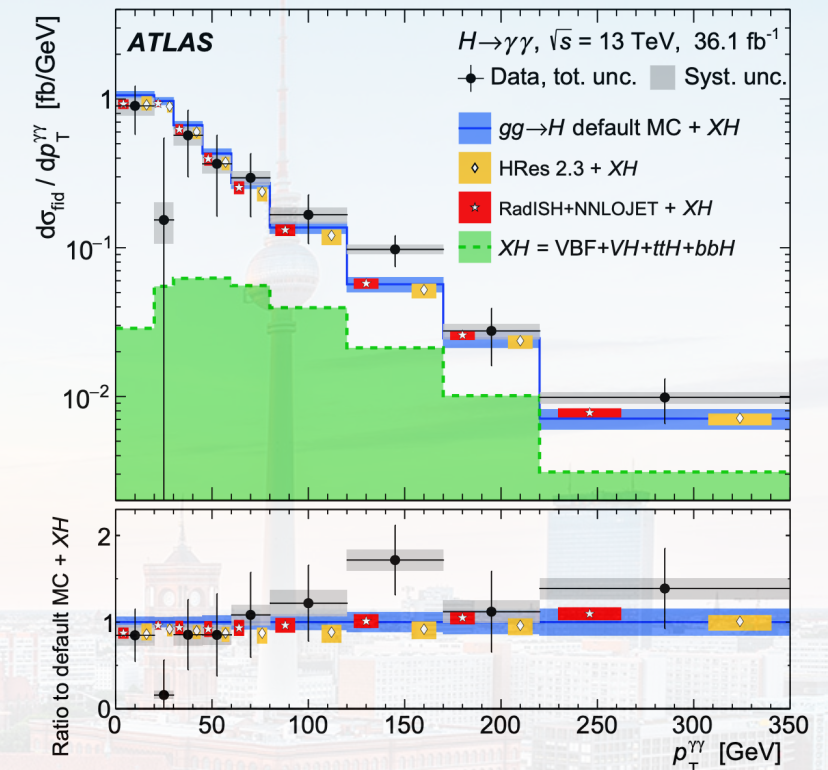


Need to attack on many fronts to further improve

- Towards N3LO PDFs ([Britzger et al. 1906.05303](#))
- Top quark mass dependence ([Davies et al. 1906.00982](#), [Davies et al 1911.10214](#))
- Bottom quark fusion at N3LO ([Duhr, Dulat, Mistlberger 1904.09990](#))
- EWK corrections ([1801.10403](#), [1811.11211](#)) ...

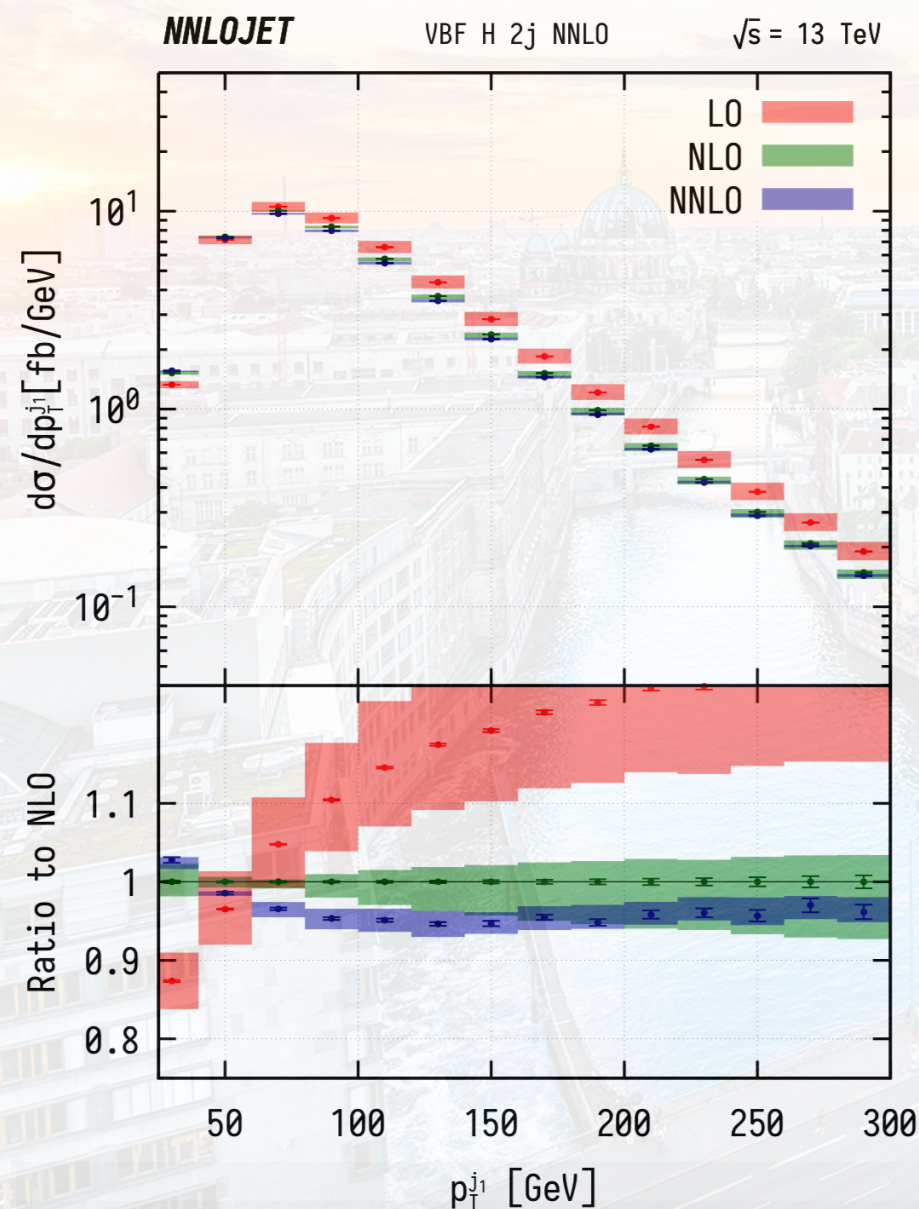
SUCCESS OF HIGGS THEORY (GLUON FUSION)

- Differential predictions advance to new precision
 - HpT (HTL) at **NNLO+N3LL accuracy** (details later)
 - Robust NNLO calculation at small pT
 - Resummation in two factorisation schemes
 - yH (HTL) at **N3LO accuracy** (details later)
 - Two methods with approximation in good agreement
 - Towards fully differential N3LO accuracy
 - H+J (full SM) at **NLO accuracy** (boosted pT region)
 - Still many aspects to improve:
 - Very time consuming at small pT (\sim **7M** CPU h)
 - Application with decay fiducial cuts
 - Join with parton shower beyond LO and LL

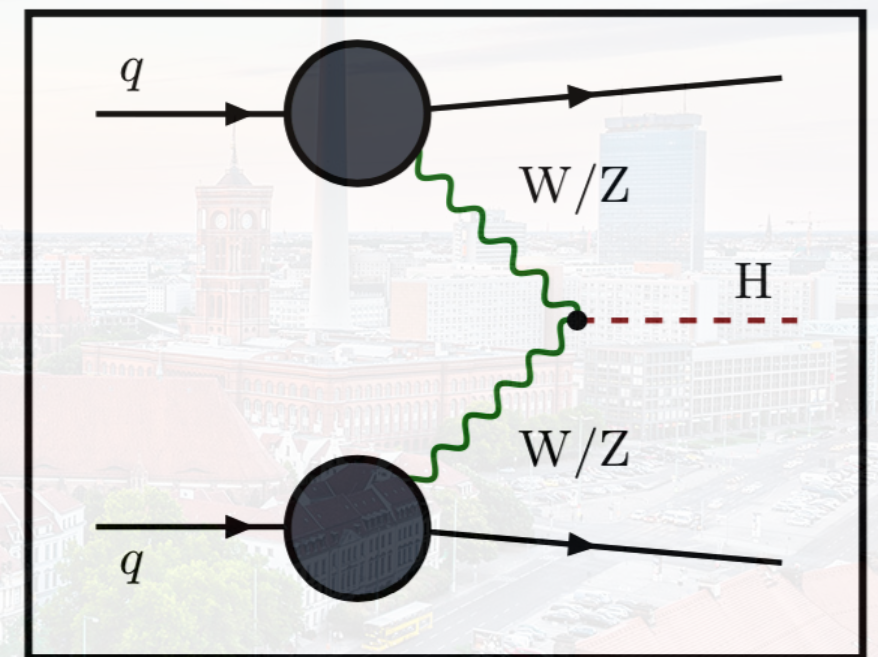


SUCCESS OF HIGGS THEORY (VECTOR BOSON FUSION)

- Differential NNLO corrections to VBFH-2J production and NLO corrections to VBFH-3J production using **structure function approach** (Cruz-Martinez et al. 1802.02445)
- Uncovered error in earlier NNLO calculation stemming from VBF-3J piece (now fixed) (Cacciari, Dreyer et al. 1506.02660) (Jager, Schissler et al. 1405.6950)



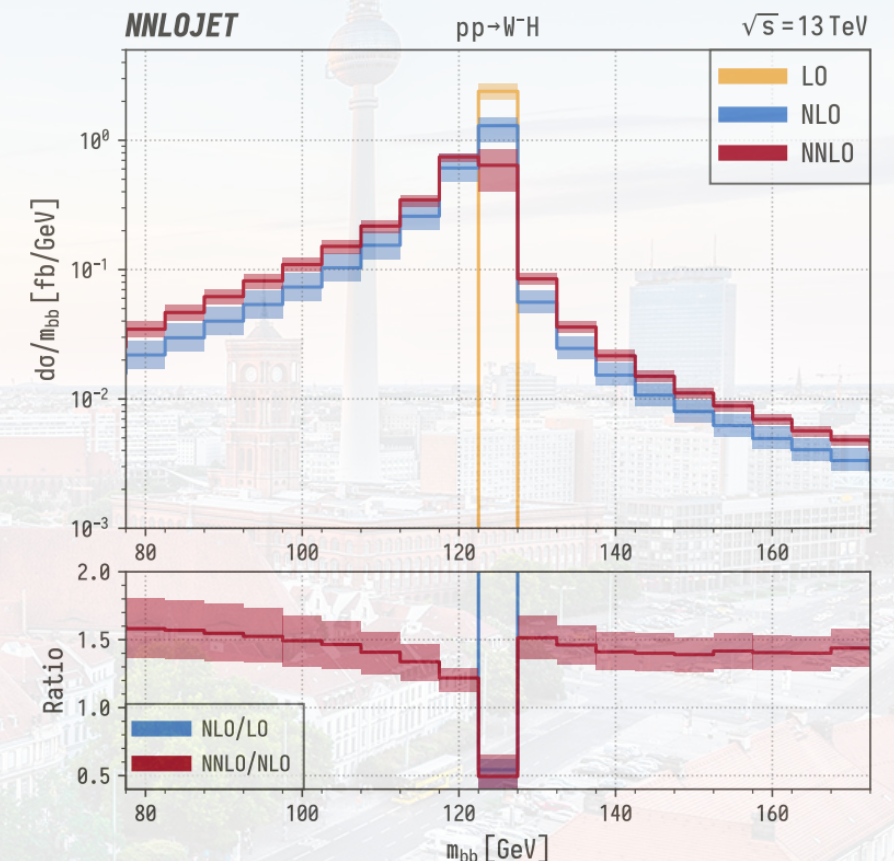
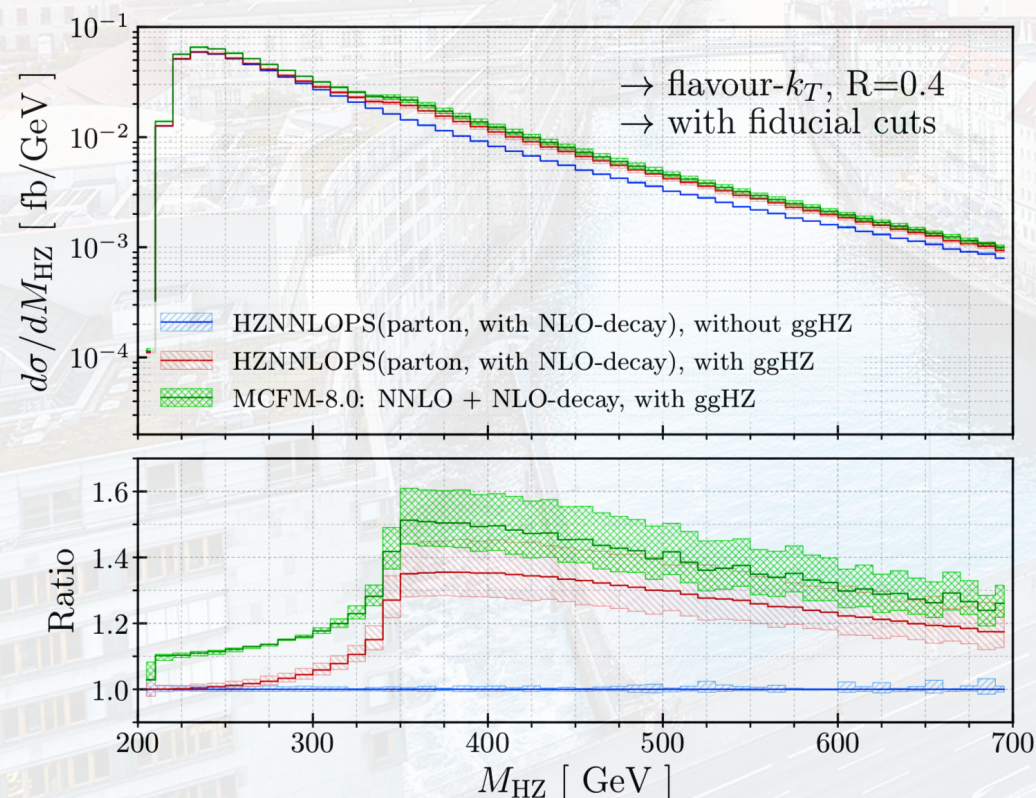
$DIS \otimes DIS$



- NNLO cross section is **-4%** compared to NLO (VBF cuts)
- Scale variation now reduced to $\pm 3\%$
- **Large overlap** in fiducial volume with gluon fusion $H+2J$
- More studies on jet radius and “VBFH-cut” via **LH19**
- Inclusive cross section at N3LO (Dreyer et al. 1606.00840)

SUCCESS OF HIGGS THEORY (VH)

- Current precision with NNLO QCD corrections in both production and decay to process $pp \rightarrow W(l\nu) + H(b\bar{b})$ with narrow width approximation and massless b quark (Ferrera et al. 1705.10304), (Caola et al. 1712.06954), (Gauld, Majer et al. 1907.05836)
- NNLO corrects NLO $H \rightarrow b\bar{b}$ decay in both below and above Higgs mass threshold regions
- New **interference** at NNLO from $H \rightarrow gg$
- N3LO $H \rightarrow b\bar{b}$ decay now available (Mondini, Schiavi, Williams 1904.08960)
- Future work with b mass and EXP flavour kT jet



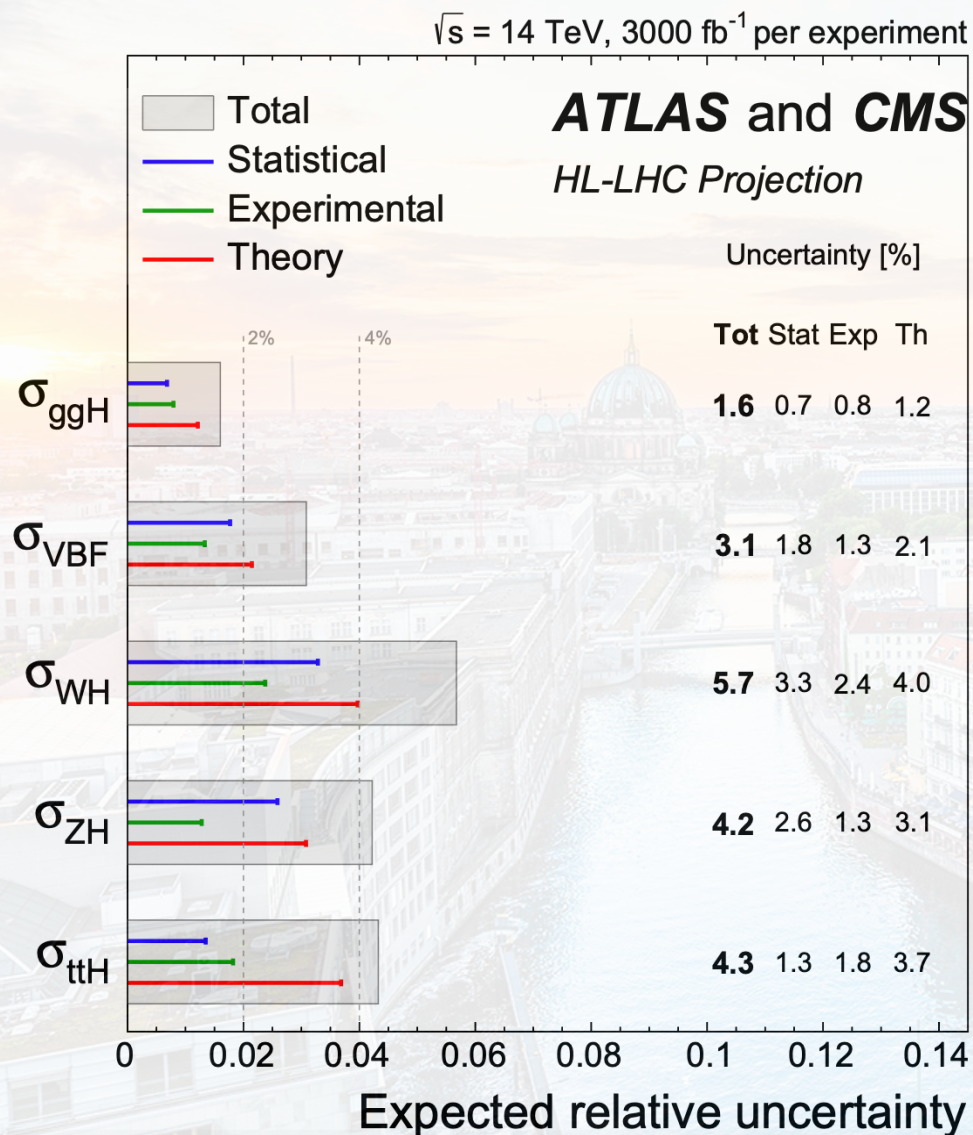
- NNLOPS accurate $pp \rightarrow Z(l^+l^-) + H(b\bar{b})$ (Astill, Bizoń et al. 1804.08141)
- Sizeable impact of loop induced $gg \rightarrow Z(l^+l^-) + H(b\bar{b})$ above top mass threshold (1-loop² at LO)
- NLO corrections includes **interference** with qg and $q\bar{q}$ channels (need two-loop massive top for a through study)

Gauld, Majer et al. 1907.05836

CHALLENGE FROM HL-LHC PROJECTION (20 YEARS)

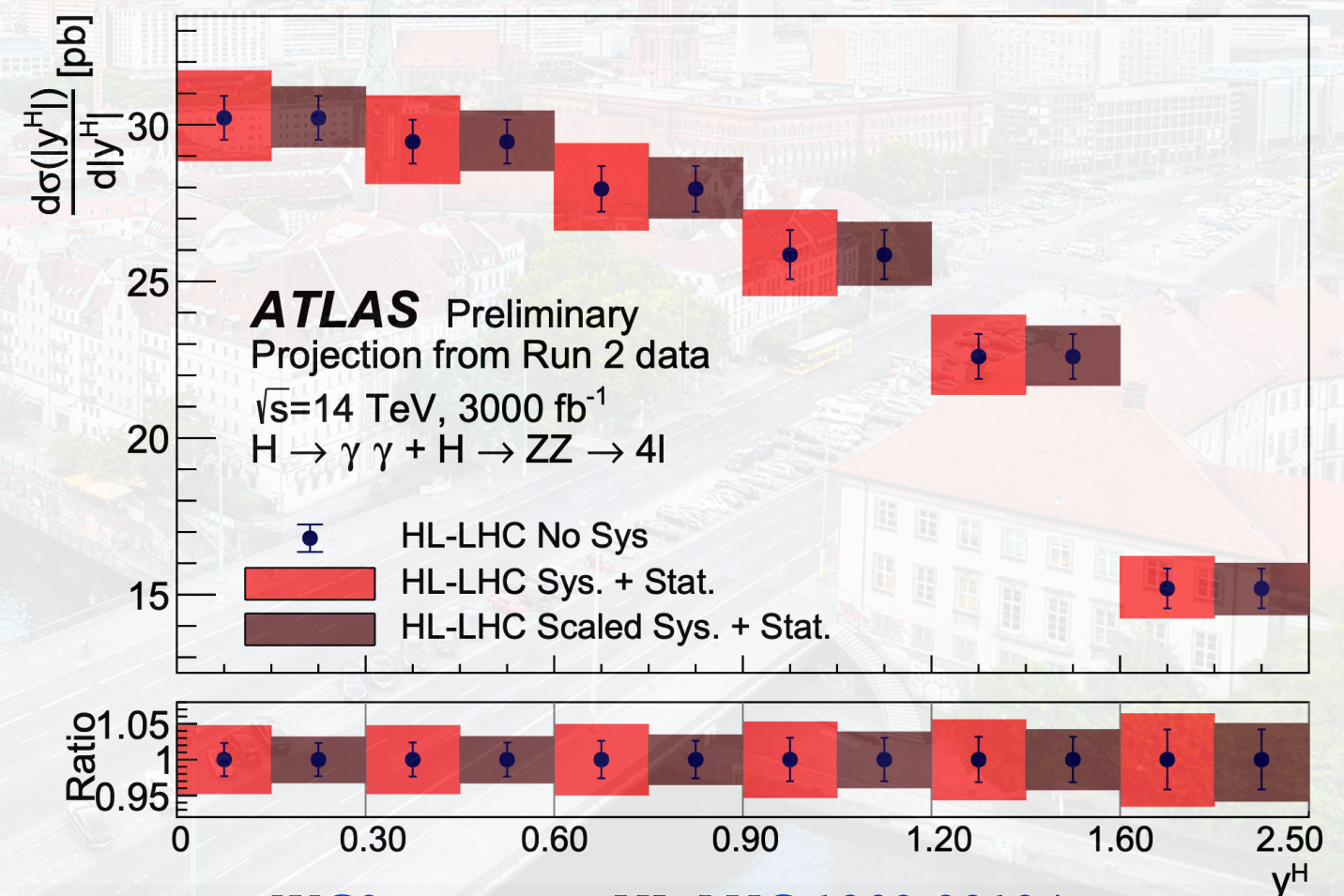
➤ Is it precise enough? **Not yet** according to HL-LHC Projections!

➤ Theory complexity scales up exponentially, EXP error scales down by $1/\sqrt{\mathcal{L}}$



➤ Differential observables (S2) HL-LHC projections:
 $y^H \pm 3\%$ $H p_T \pm 5\%$ (more details in this talk)

➤ Theory need consistent upgrade to reduce PDF and α_s uncertainties

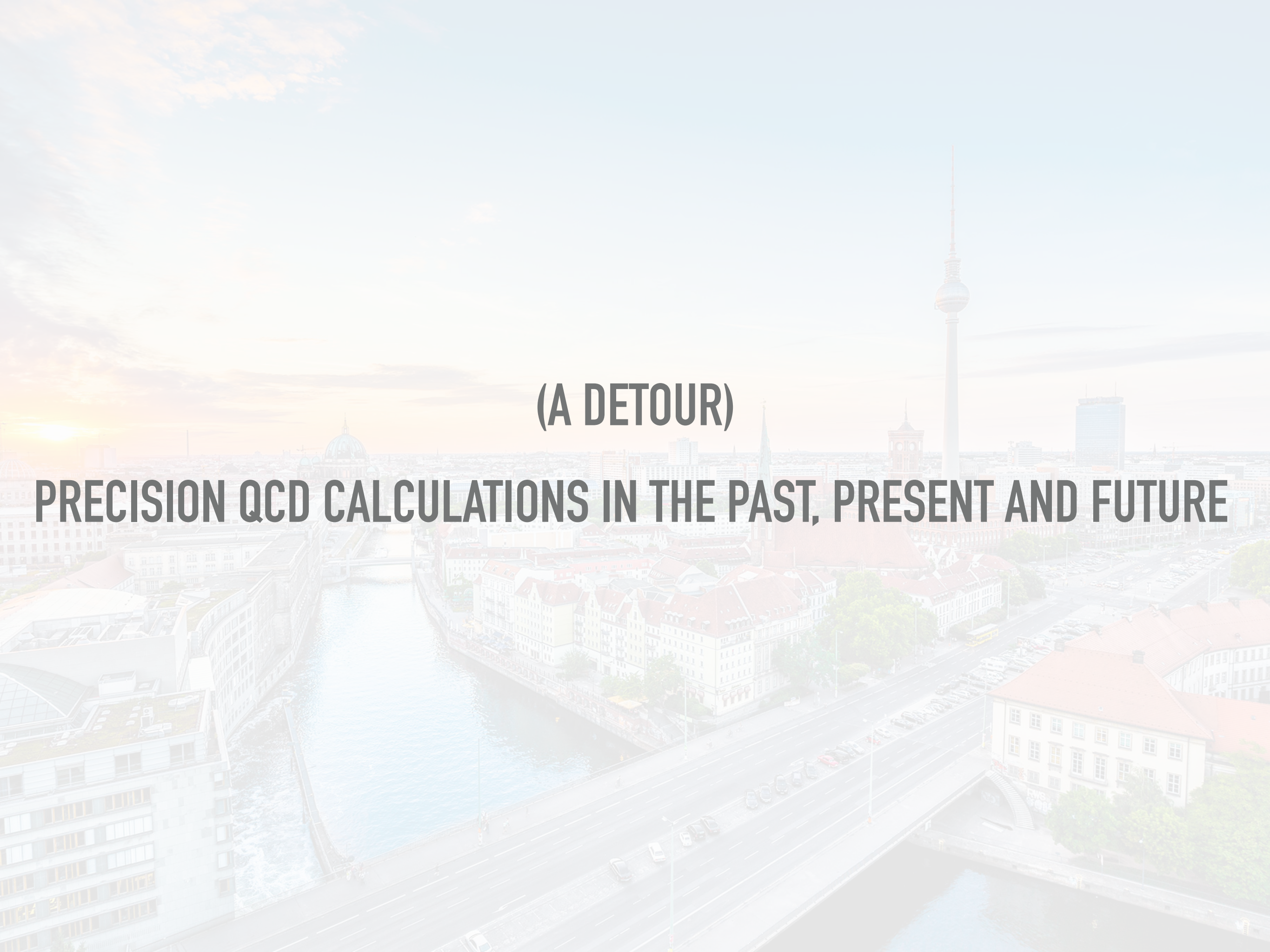


➤ HL-LHC expects $\pm 1.6\%$ in two decades

➤ Current N3LO has $\pm 4\%$ for QCD alone!

WG2 report on HL-LHC 1902.00134

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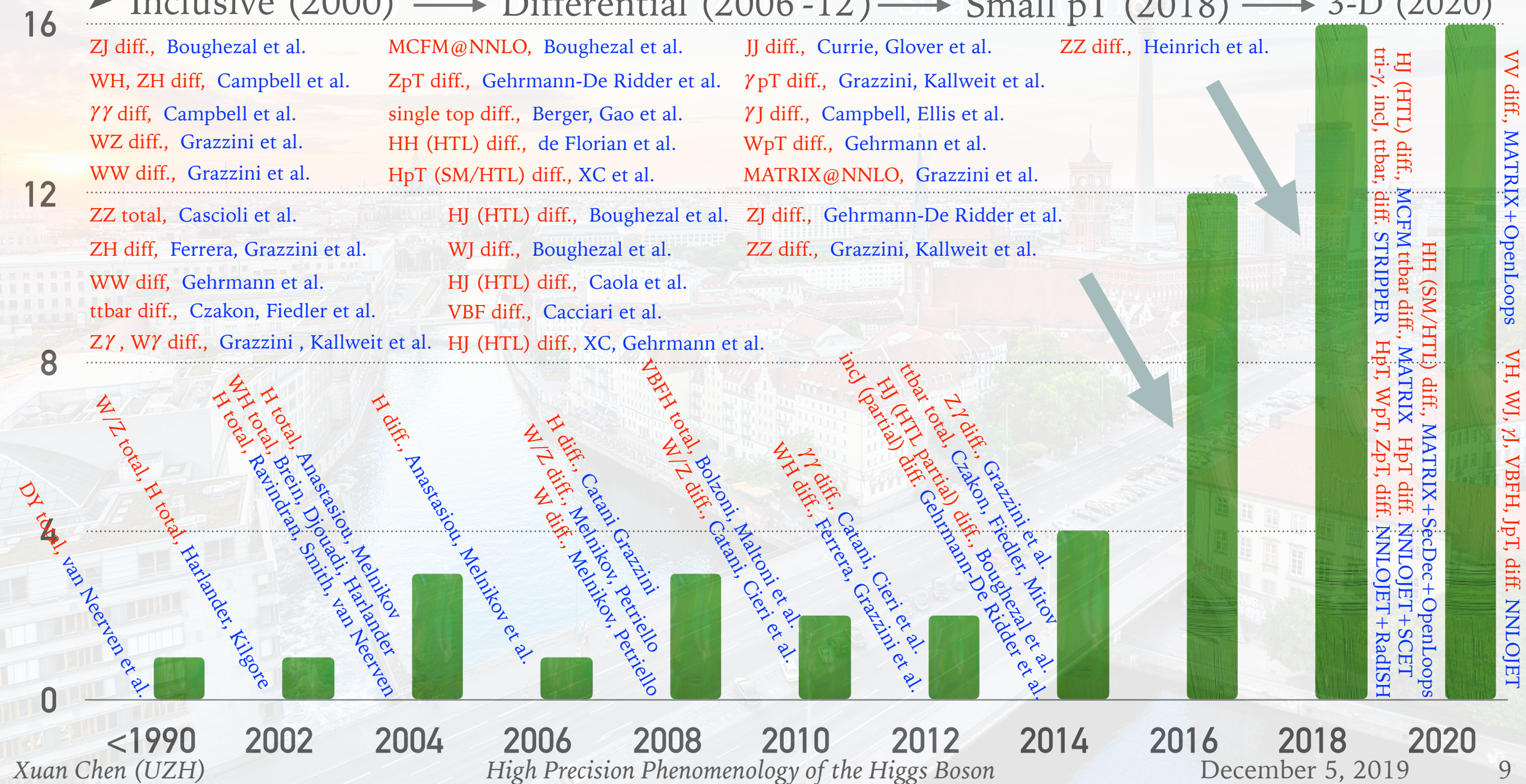
(A DETOUR)

PRECISION QCD CALCULATIONS IN THE PAST, PRESENT AND FUTURE

THE STANDARD NNLO @ LHC

- LHC processes at NNLO QCD accuracy (include secondary confirmations)
 - One colourless (2000) → Two colourless (2004) → One or two Colourful (2014)

QCD+QED ←
 - Inclusive (2000) → Differential (2006-12) → Small pT (2018) → 3-D (2020)



THE STANDARD NNLO @ LHC IN NEXT 5 YEARS

- LHC processes at NNLO QCD accuracy
 - $2 \rightarrow 2$ is well developed, $2 \rightarrow 3$ available for limited topology (VBFH-2J, $\gamma\gamma\gamma$). More differential observables in coming years.
 - Rapid progress in the calculations of 2-loop-5-point amplitudes.
LC 5-gluon: all-plus (Badger et al 1507.08797) (Gehrmann et al 1511.05409), one-plus (Badger et al 1811.11699), all-helicities (Abreu et al 1712.03946, 1812.04586), LC 5-parton: all-helicities (Abreu et al 1809.09067, 1904.00945), FC 5-gluon: all-plus (Badger et al 1905.03733) FC 5-parton: all master integrals (Chicherin et al 1812.11160), LC W+4-parton (Hartanto et al 1906.11862)
 - $\gamma\gamma\gamma$ production from STRIPPER (Chawdhry, Czakon et al 1911.00479)
(excluding small contributions from 2-loop non-planar and internal quark loop)
 γ +JJ, $\gamma\gamma$ +J, JJJ etc. productions in coming years and desire for $t\bar{t}H$
(bottleneck is the 2-loop AMP but approximations like in $\gamma\gamma\gamma$ might be acceptable)
 - Towards “NNLO revolution” (performance matters)
 - Automation of two-loop matrix elements. SecDec, OpenLoops2
 - Automation of removing IR divergence. STRIPPER, nested-soft-collinear, etc.
 - Equally important input resolving NNLO accuracy: top mass effects, $\alpha\alpha_s$ mixing, flavours of jets, resummation corrections, non-perturbative effects etc.

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THE STANDARD NNLO @ LHC IN NEXT 5 YEARS

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THE STANDARD NNLO @ LHC IN NEXT 5 YEARS

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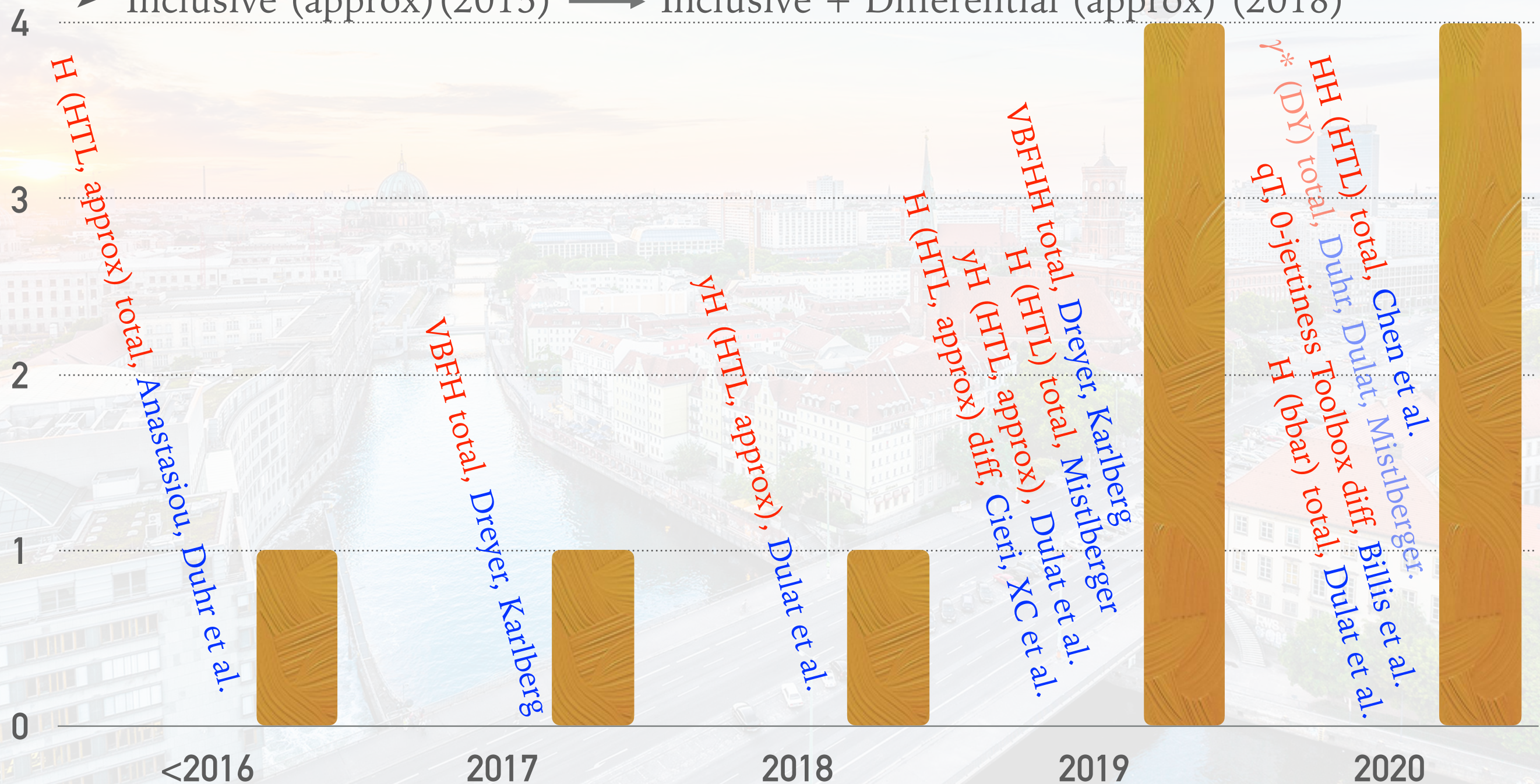
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THE CUTTING-EDGE N3LO @ LHC

- LHC processes at N3LO accuracy (include secondary confirmation)
 - N3LO at 2015 was like the early stage of NNLO in 2000's.
 - Inclusive (approx)(2015) → Inclusive + Differential (approx) (2018)



TOWARDS FULLY DIFFERENTIAL N3LO PRECISION ?

- Several cutting edge N3LO differential calculations available recently:
 - $ep \rightarrow ep$: fully differential one-jet DIS ([Currie, Gehrmann, Glover et al. 1803.09973](#))
 - $gg \rightarrow H$: in HTL **with approximation** of N3LO beam function ([Cieri, XC et al. 1807.11501](#))
 - $H \rightarrow b\bar{b}$: fully differential with massless bottom quark ([Mondini, Schiavi et al. 1904.08960](#))
- More N3LO processes could be available based on established NNLO works for LHC:
 - VBFH: using N3LO structure function (1606.00840) + NNLO two-jet DIS (1703.05977)
 - DY: N3LO qT and 0-jettiness toolbox (1909.00811) + NNLO Z+J at small qT (1805.05916)
 - W: N3LO qT and 0-jettiness toolbox (1909.00811) + NNLO W+J at small qT (1905.05171)
- However, can we call it N3LO precision? (unsolved issues at NNLO)
 - PDFs fitted at NNLO evolution but with limited NNLO hard coefficients (DIS, $p_T^Z, t\bar{t}$)
 - $\delta(\alpha_s) \sim \pm 2.6 \%$ and $\delta(\text{PDF-TH}) \sim \pm 1.16 \%$ (missing higher order uncertainty) for $\sigma_{N^3LO}^{H,tot}$
 - Non-perturbative effects fitted at NLOPS accuracy (Underlying events, γ fragmentation etc.)

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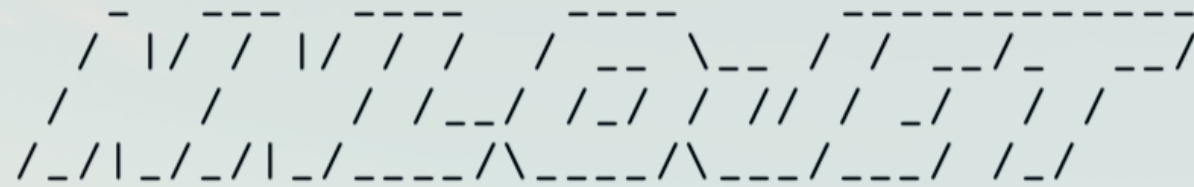
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HIGGS PRODUCTION AND DECAY PROCESSES IN NNLOJET





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* NNLOJET: A multiprocess parton level event generator at O(alpha_s^3)*
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X. Chen, J. Cruz-Martinez, J. Currie, R. Gauld, A. Gehrmann-De Ridder, T. Gehrmann, E.W.N. Glover, M. Höfer, A. Huss, I. Majer, J. Mo, T. Morgan, J. Niehues, J. Pires, R. Schürmann, D. Walker, J. Whitehead

LHC Higgs Production channels		
$H + J$ (ggF) NNLO HTL \otimes LO SM	1408.5325, 1607,08817, 1805.00736, 1805.05916	
H (ggF) N3LO HTL (approx.)	1807.11501	
$H + JJ$ (VBF) NNLO	1802.02445	
$H + V$ (VH) NNLO	1907.05836	

Higgs Decay channels		
$b\bar{b}$	NNLO	b-tagging
$WW^* \rightarrow 2l2\nu$	LO	Lepton isolation
$\tau^+\tau^-$	LO	Massive final states
$ZZ^* \rightarrow 4l$	LO	Lepton isolation
$\gamma\gamma$	LO	Photon isolation
$Z(\rightarrow 2l)\gamma$	LO	Photon + lepton iso.

- Parton level event generator with NNLO antenna subtraction method
- **NNLOJET** provides many cutting-edge predictions of the Higgs boson phenomenology.
- ggF, VBF and VH channels are linked with limited decay channels.
- Identification of EW and QCD final states using EXP algorithms.



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$b\bar{b}$	NNLO	b-tagging
$WW^* \rightarrow 2l2\nu$	LO	Lepton isolation
$\tau^+\tau^-$	LO	Massive final states
$ZZ^* \rightarrow 4l$	LO	Lepton isolation
$\gamma\gamma$	LO	Photon isolation
$Z(\rightarrow 2l)\gamma$	LO	Photon + lepton iso.



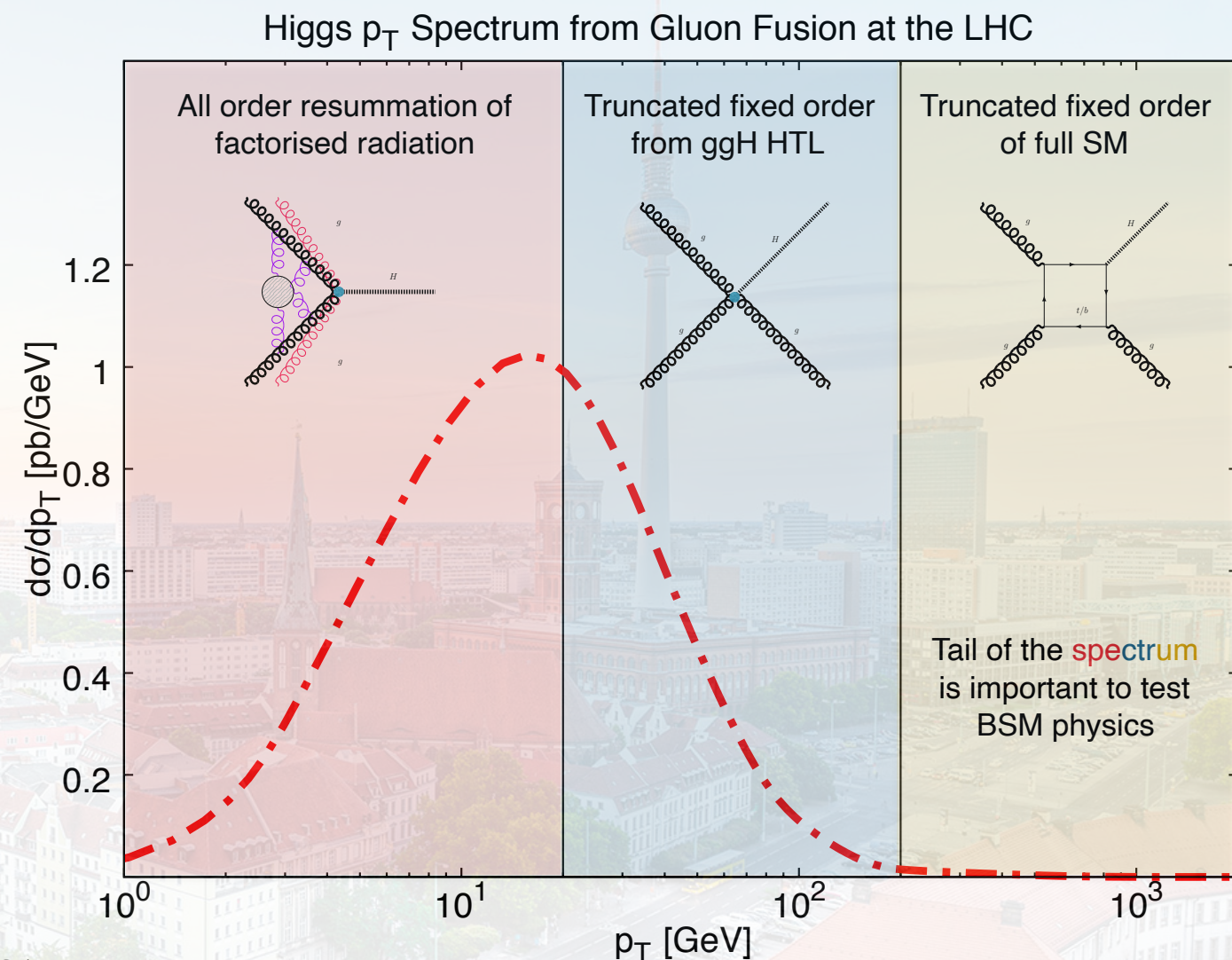
- Parton level event generator with NNLO antenna subtraction method
- **NNLOJET** provides many cutting-edge predictions of the Higgs boson phenomenology.
- ggF, VBF and VH channels are linked with various decay channels.
- Identification of EW and QCD final states using EXP algorithms.

HIGGS TRANSVERSE MOMENTUM DISTRIBUTION IN FULL SPECTRUM



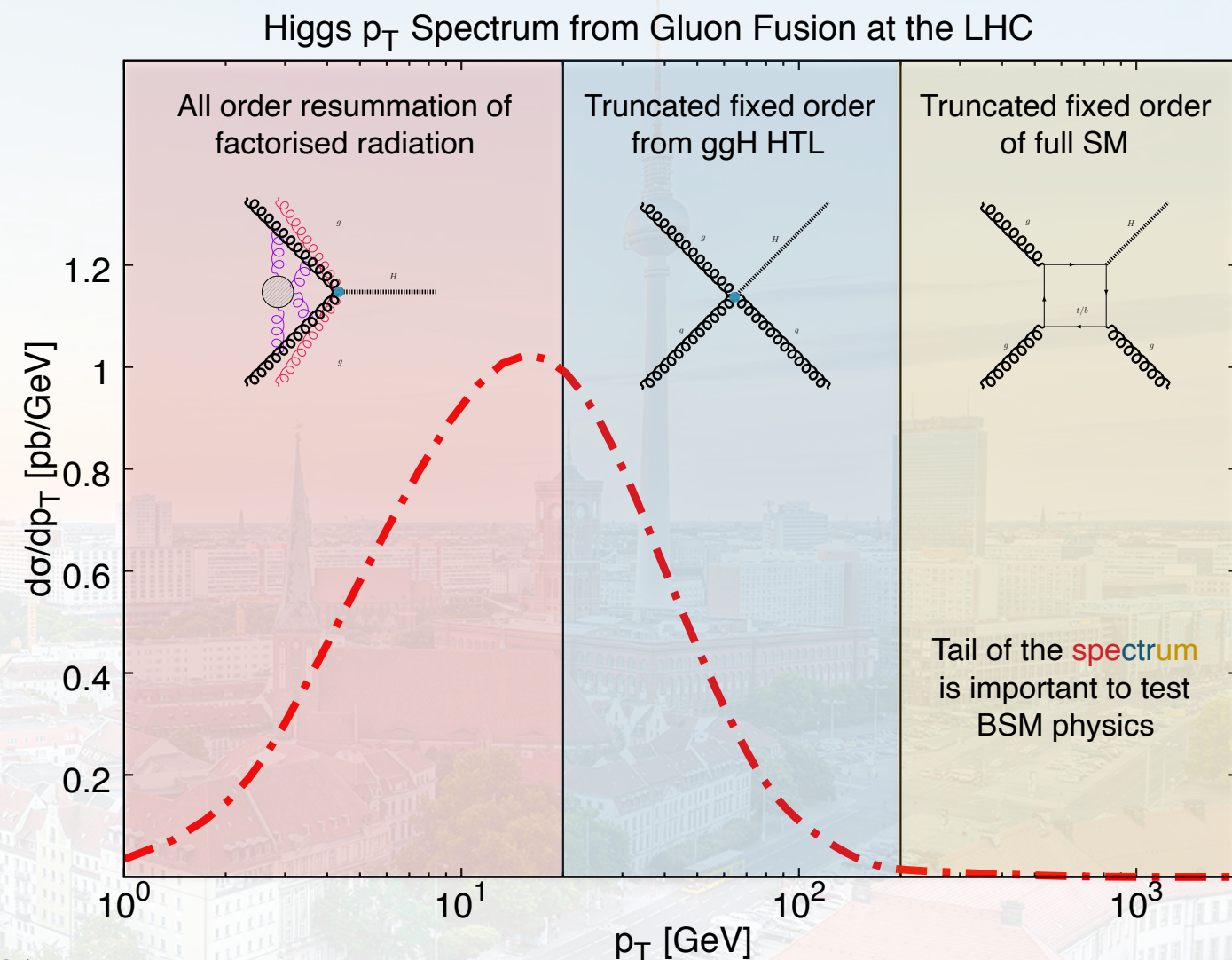
HIGGS TRANSVERSE MOMENTUM SPECTRUM

- Higgs p_T **spectrum** tests SM in various aspects
- **Small p_T region** (< 20 GeV):
 - Singular log terms spoil any reliable fixed order predictions $\ln^k(m_H^2/p_T^2)/p_T^2$
 - Resummation of log terms and match to fixed order: $d\sigma^{FO} \ominus d\sigma^S \oplus d\sigma^R$
- **Medium p_T region** ($20 \sim 200$ GeV):
 - Reliable with heavy top limit (HTL or EFT)
 - Current best precision is H+J NNLO HTL
- **Boosted p_T region** (> 200 GeV)
 - Energy scale resolve mass effect of quark loop
 - Best ggF precision is H+J at NLO SM
 - VBF, VH and ttH channels equally important
- Many other effects involved: top-bottom interference, heavy quark Yukawa couplings, resummation of logs involving quark mass etc.



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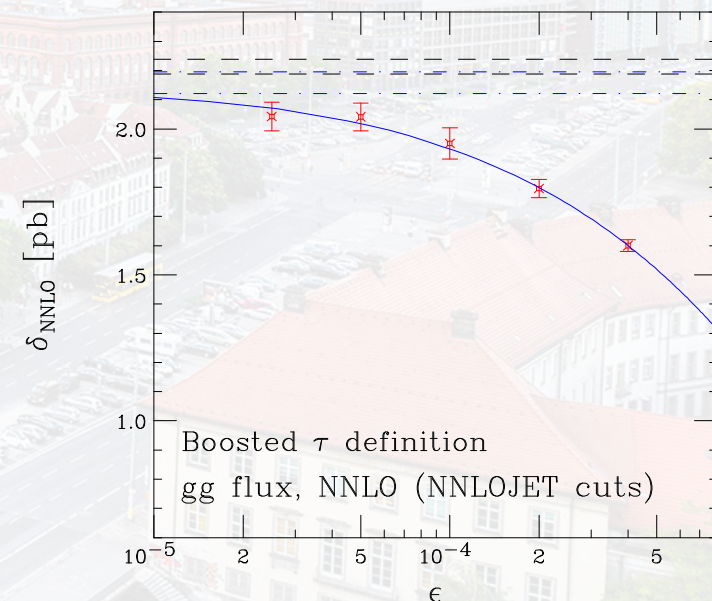
Will separately discuss the pheno in each $H p_T$ region next

HIGGS TRANSVERSE MOMENTUM AT MEDIUM PT

- H+J Computed at NNLO QCD (HTL) by 4 groups using 3 methods
 - Antenna subtraction (NNLOJET) [XC, Gehrmann, Glover et al. \(1408.5325, 1607.08817\)](#)
 - Sector improved subtraction (STRIPPER) [Boughezal, Caola, Schulze et al. \(1302.6216, 1504.07922\)](#)
 - N-Jettiness (BFGLP and MCFM) [Boughezal, Focke et al. \(1505.03893\)](#) [Campbell et al. \(1906.01020\)](#)
- It was the **battle ground for the first** LHC process with single jet + colourless @ NNLO
 - Long-standing discrepancy between N-Jettiness and other methods

	$\sigma_{H(\rightarrow\gamma\gamma)+\geq 1jet, NNLO}^{EFT}$	$\sigma_{H+\geq 1jet, NNLO}^{EFT}$	$\sigma_{H+\geq 1jet, NNLO}^{EFT}$
NNLOJET	$9.44^{+0.59}_{-0.85}$ fb	$16.8^{+0.9}_{-1.5}$ pb	$5.81^{+0.51}_{-0.62}$ pb
STRIPPER	$9.45^{+0.58}_{-0.82}$ fb	-	-
STRIPPER	-	$16.7^{+1.0}_{-}$ pb	-
BFGLP	-	-	$5.5^{+0.3}_{-0.4}$ pb

[XC, Gehrmann, Glover et al. \(1408.5325, 1607.08817\)](#)



- Finally resolved with MCFM revisit study in this year

- Jettiness cut **20 times smaller** than in BFGLP
- Extrapolate to zero (**$\sim 5\%$ @ NNLO**)
- Desire sub-leading power correction at NNLO

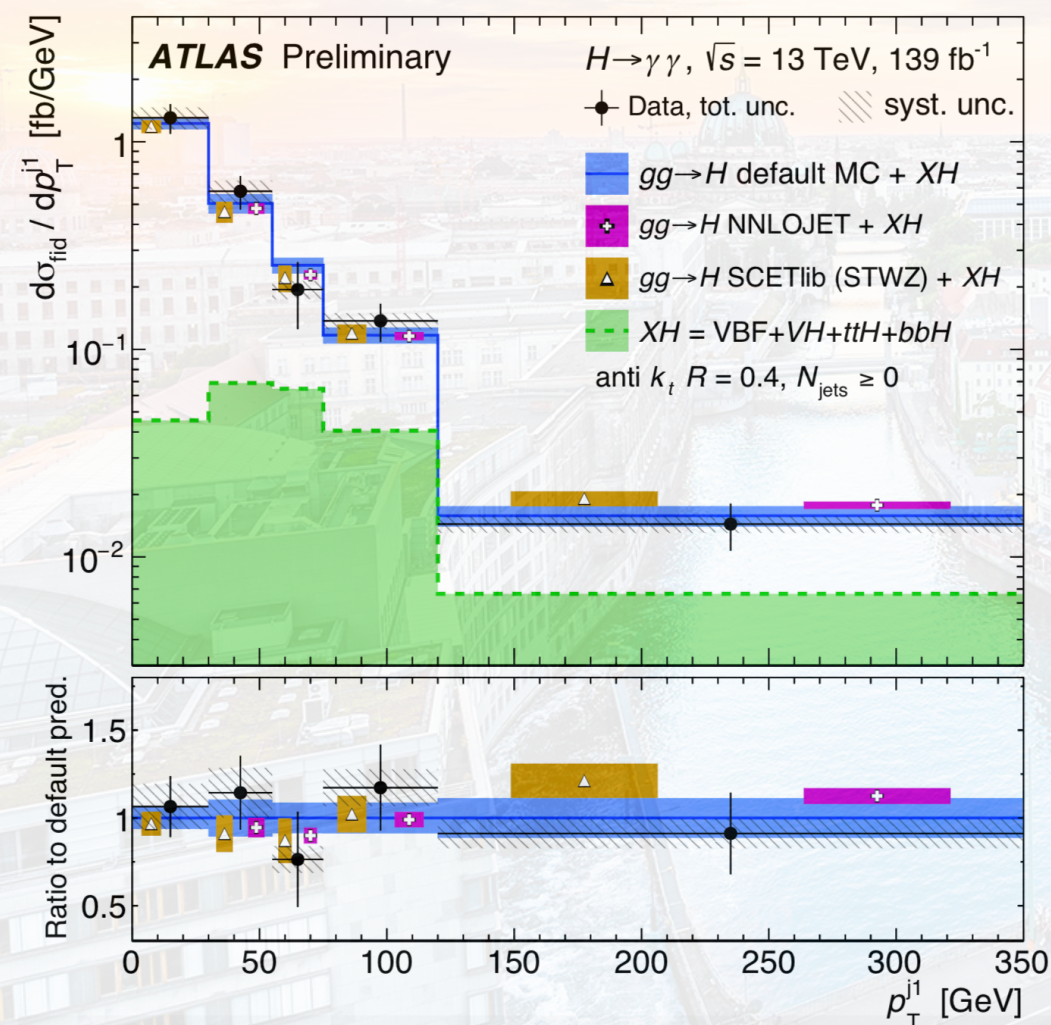
$$\sigma_{NNLO}(\text{NNLOJET}) = 16.73 \pm 0.05^{+1.00}_{-1.51} \text{ pb}$$

$$\sigma_{NNLO}(\text{MCFM, fit}) = 16.71 \pm 0.05^{+1.03}_{-1.52} \text{ pb}$$

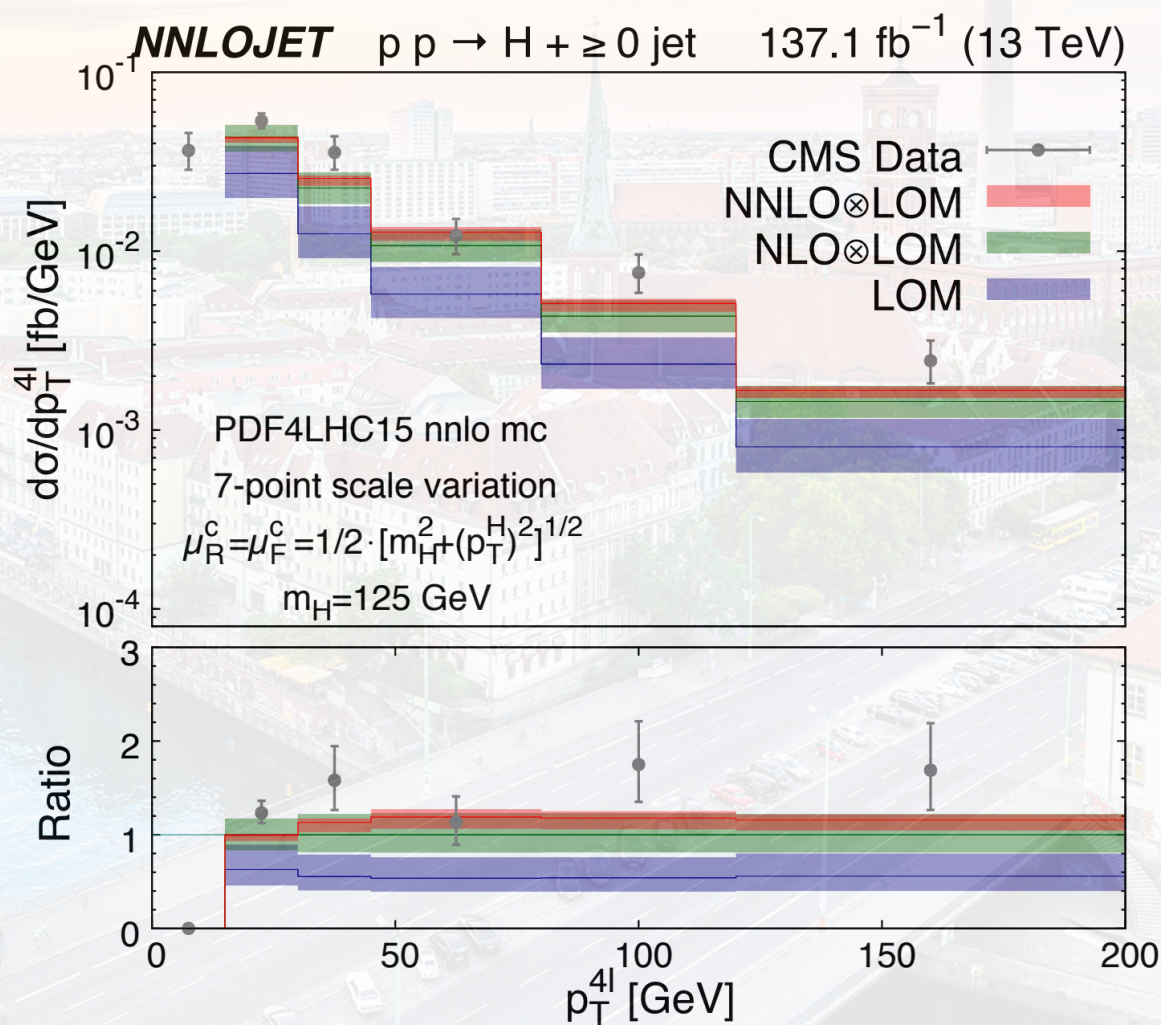
[Campbell et al. \(1906.01020\)](#)

HIGGS TRANSVERSE MOMENTUM AT MEDIUM PT

- Fiducial cross section for H+J now known at NNLO QCD for:
 - $H \rightarrow \gamma\gamma$ Caola, Melnikov, Schulze (1508.02684), XC, Gehrmann, Glover et al. (1607.08817)
 - $H \rightarrow WW^* \rightarrow 2l2\nu$ Caola, Melnikov, Schulze (1508.02684)
 - $H \rightarrow ZZ^* \rightarrow 4l$ XC, Gehrmann, Glover, Huss (1905.13738)



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Exact EXP fiducial region with:

- Photon isolation
- Lepton isolation
- Jet identification

➤ Top mass @ LO
 Good agreement!

XC, Gehrmann, Glover, Huss (1905.13738)

HIGGS TRANSVERSE MOMENTUM AT **SMALL PT**

- FO break down, where is the problem come from?

- Take $d\sigma_{NLO}^H$ as example:

$$A_{2gH}^0(\hat{g}, \hat{g}, H) + A_{3gH}^0(\hat{g}, \hat{g}, g, H) - F_3^0(\hat{g}, g, \hat{g})A_{2gH}^0(\tilde{\hat{g}}, \tilde{\hat{g}}, \tilde{H}) + A_{2gH}^1(\hat{g}, \hat{g}, H) + \mathcal{F}_3^0(\hat{g}, \hat{g})A_{2gH}^0(\tilde{\hat{g}}, \tilde{\hat{g}}, \tilde{H})$$

↓
 $\delta(p_T^H)$

↓
 p_T^H

↓
 $\delta(p_T^H)$

↓
 $\delta(p_T^H)$

↓
 $\delta(p_T^H)$

- Finite **p_T^H** region has no IR regulator → fixed order predictions break down
- How to make reliable predictions of $d\sigma/dp_T^H$ at 1 GeV?
- Use QCD factorisation to distinguish radiations from Born kinematics.

$$d\sigma = \sigma_{LO} \otimes H \otimes B \otimes B \otimes S \otimes J$$

- Replace IR subtraction by IR renormalisation (IR poles removed).
- Find and solve RGE of factorised functions to include all order effects.

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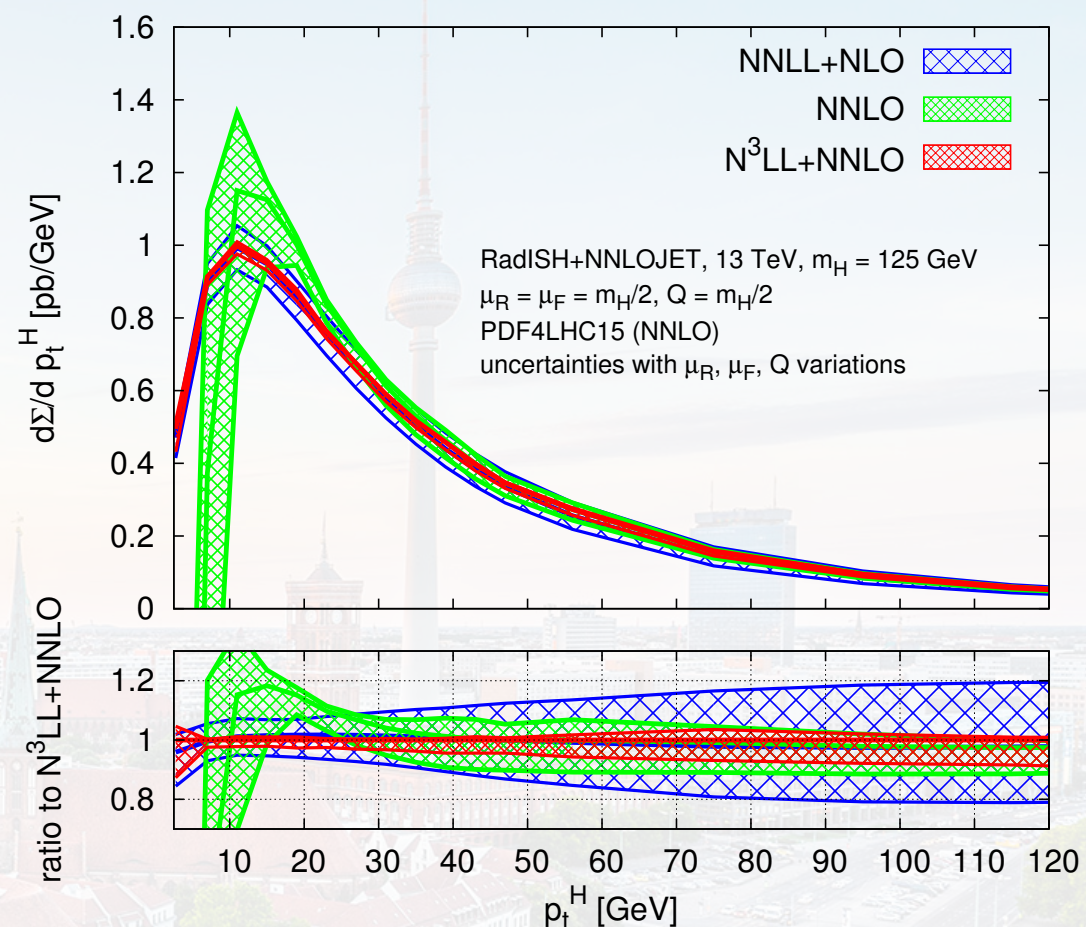
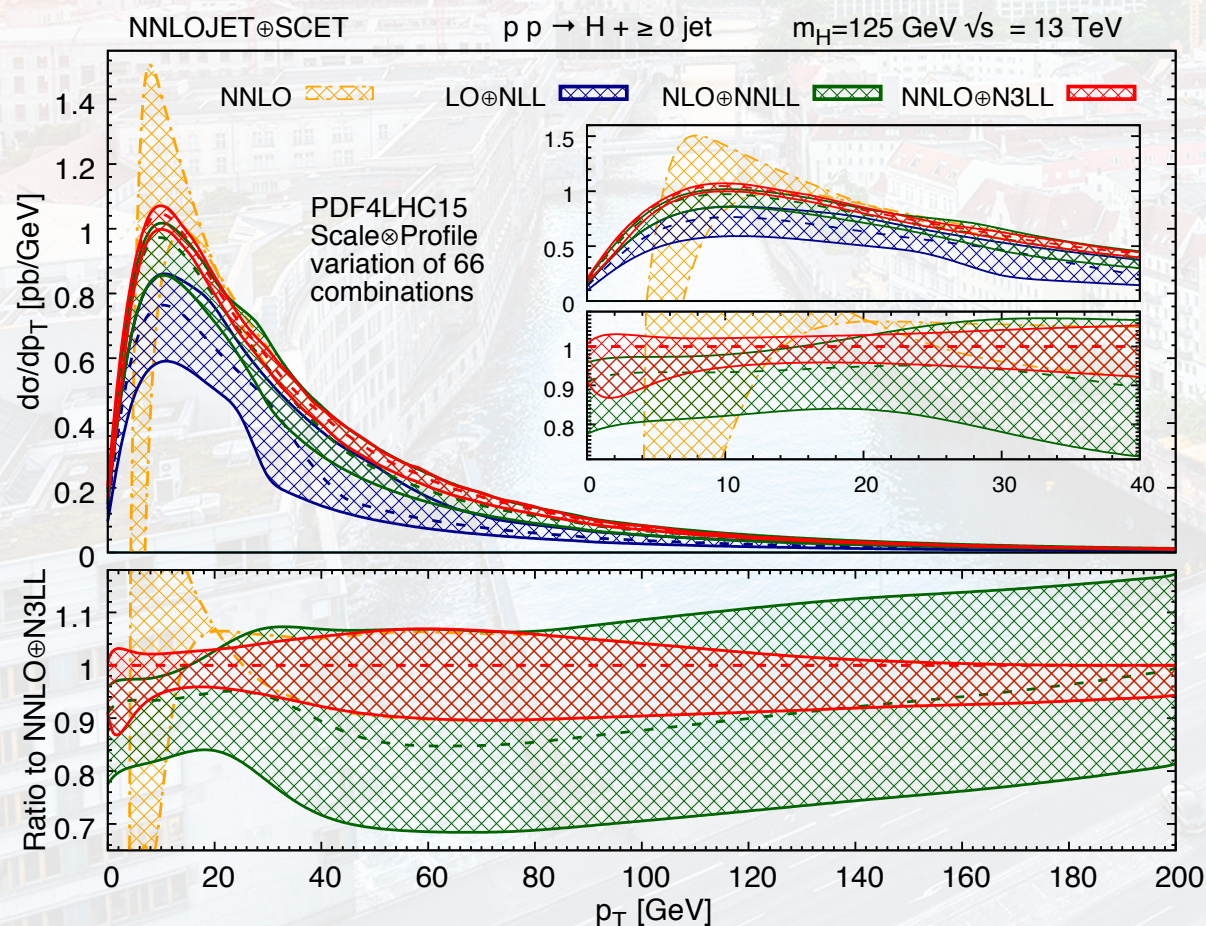
$$d\sigma = \sigma_{LO} \otimes H \otimes B \otimes B \otimes S \otimes J$$

- Replace IR subtraction by IR renormalisation (IR poles removed).
 - Find and solve RGE of factorised functions to include all order effects.

HIGGS TRANSVERSE MOMENTUM SPECTRUM (SMALL+MEDIUM)

- NNLO + N3LL Resummation with SCET and RadISH
 - RadISH + NNLOJET at N3LL + NNLO
 - Multiplicative matching to NNLO total X.S.
 - Substantial regulation from NNLO+N3LL at the peak of spectrum
 - Scale variation reduced by 60% from NLO+NNLL to NNLO+N3LL

RadISH+NNLOJET
1805.05916

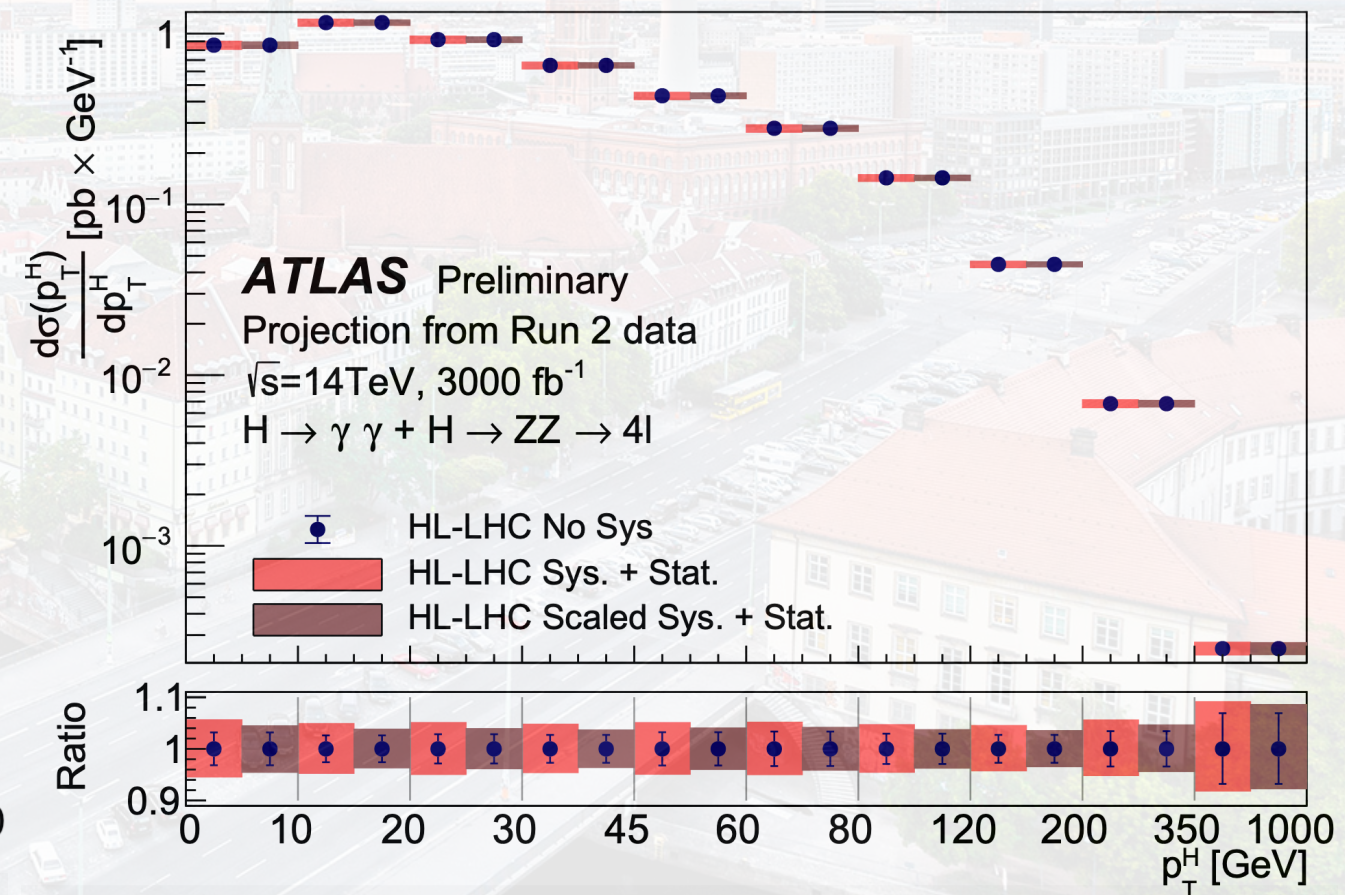
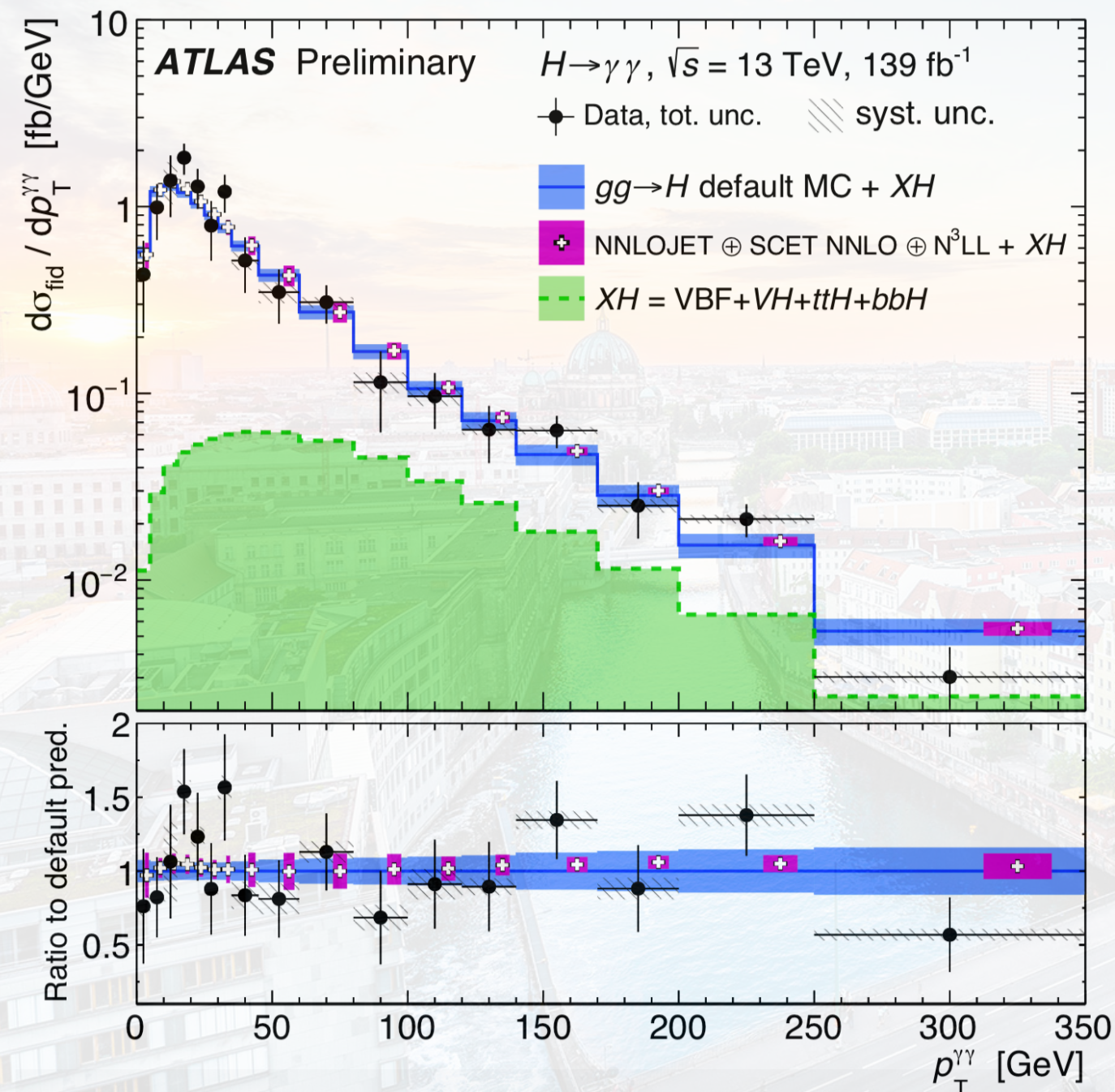


- SCET + NNLOJET at N3LL + NNLO
- Additive matching using profile functions
- Conservative uncertainty estimation involving 11 scale variation choices times 6 profile functions
- Noticeable deviation between NNLO and NNLO+N3LL starting from 30 GeV
- Future extension to include m_t and m_b effect

HIGGS TRANSVERSE MOMENTUM SPECTRUM (SMALL+MEDIUM)

► Comparison with LHC data and HL-LHC projection

- SCET + NNLOJET at N3LL + NNLO
- Consistent with LHC full Run II data
- EXP uncertainty $\pm 40\%$, TH uncertainty $\pm 8\%$
- Close to HL-LHC projection uncertainty $\pm 5\%$ (S2)



ATLAS-CONF-2019-029

WG2 report on HL-LHC 1902.00134

HIGGS TRANSVERSE MOMENTUM AT BOOSTED REGION

.....

- Expect HTL approximation fail for $p_T > 200$ GeV

- Two approaches to include top mass effects

- Expansion valid for $m_H^2, m_t^2 \ll |s| \sim |t| \sim |u|$

- Lindert, Kudashkin, et al (1703.03886); Neumann (1802.02981)

- Exact results (numerical in SecDec)

- Jones, Kerner, Luisoni (1802.00349)

- Joint effort in HH: exact numerical+expansion

- Davies, Heinrich, Jones, et al. (1907.06408)

- Large NLO/LO K-factor ~ 2

- K-factor very similar to HTL

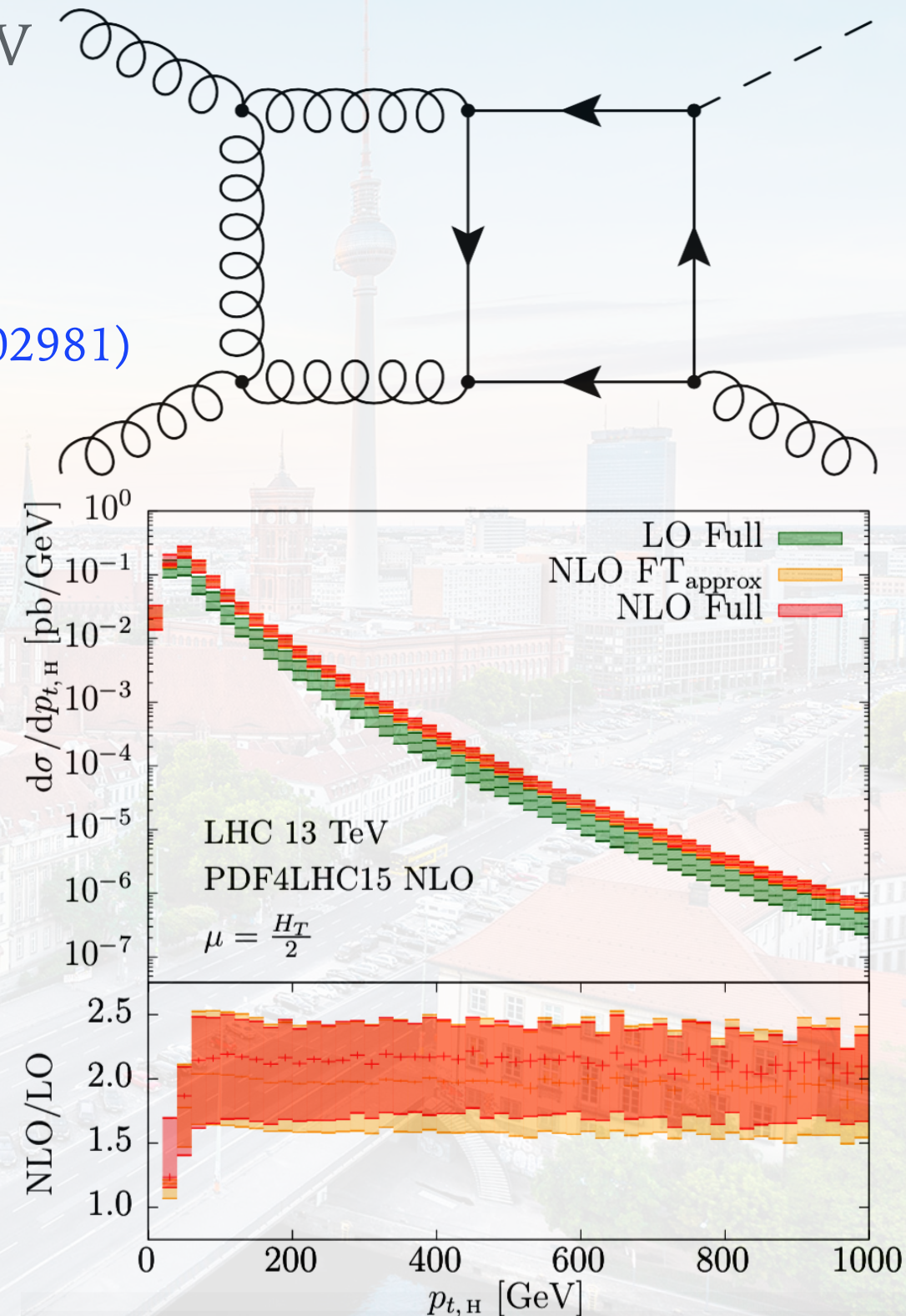
- K-factor **nearly flat** at large p_T

- Several open questions.....

- Combination with NNLO HTL

- Top-quark mass scheme uncertainty OS/MSbar

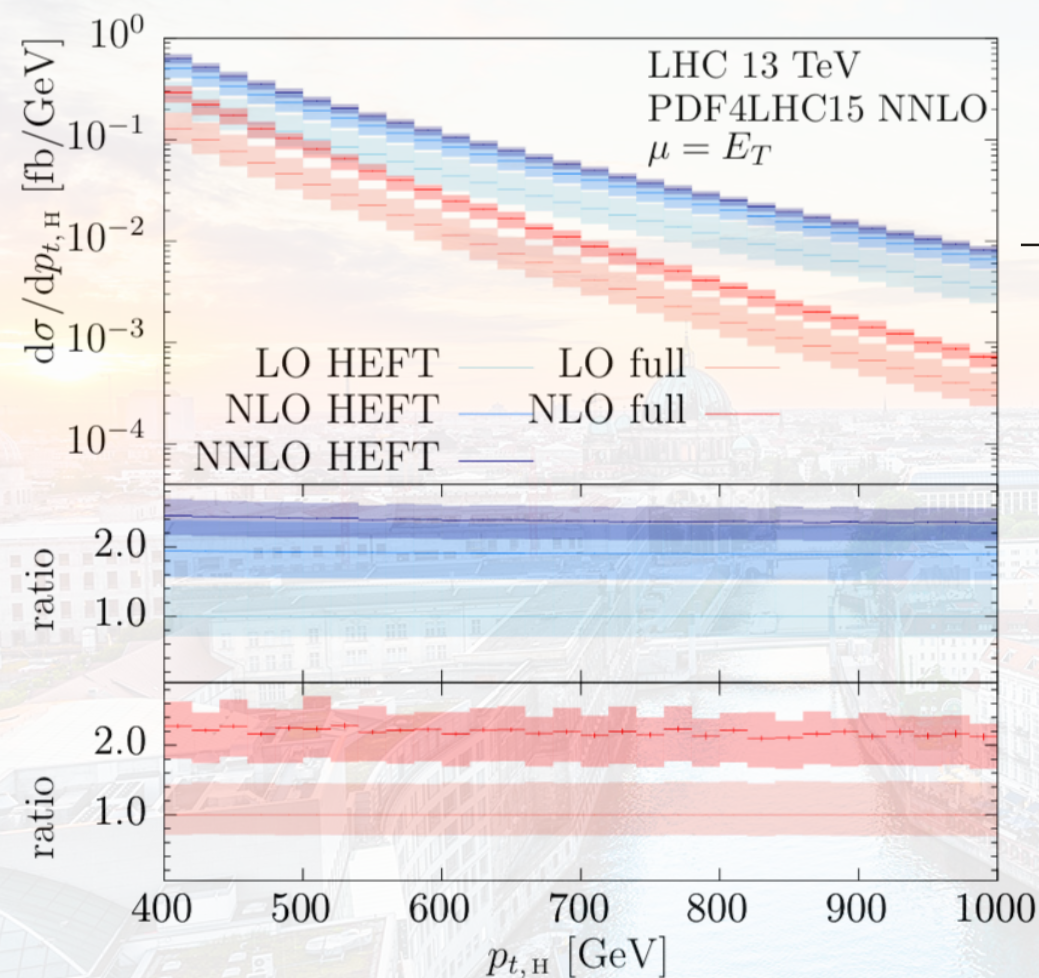
- Numerical stability of P.S. at large p_T



Jones, Kerner, Luisoni (1802.00349)

HIGGS TRANSVERSE MOMENTUM AT BOOSTED REGION

- Extension to NNLO HTL/NLO SM combined distributions in boosted region:
Rescale NLO SM by K_{NNLO}^{HTL} with the assumption of similar SM/HTL K-factors



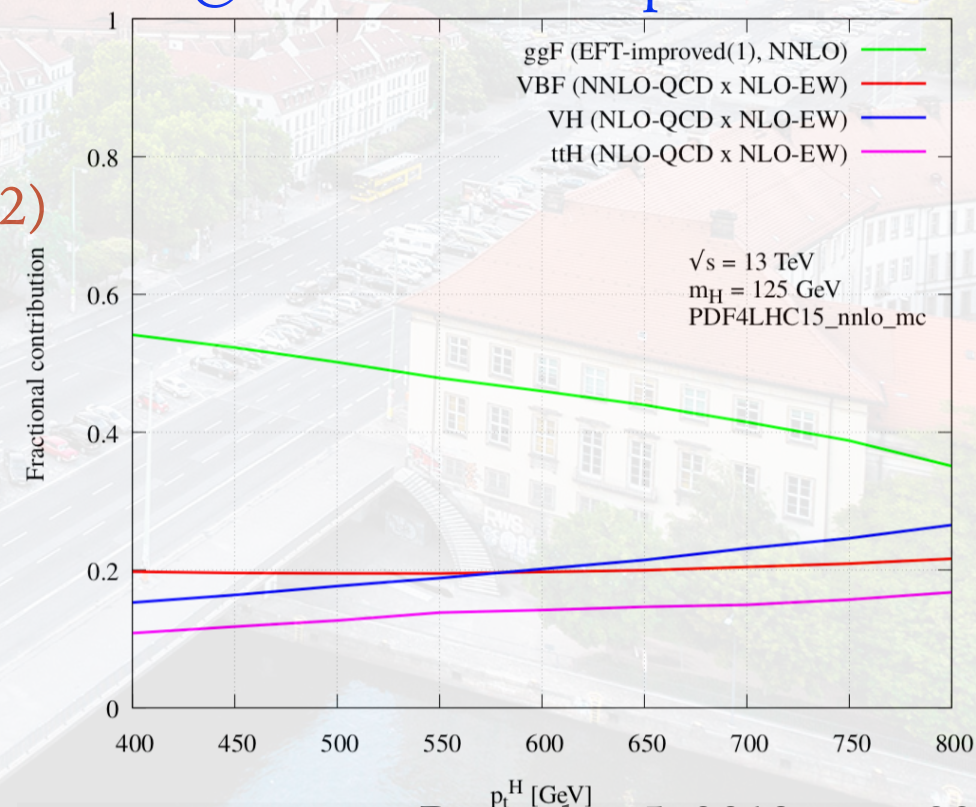
$$\Sigma^{\text{EFT-improved (1), NNLO}}(p_{\perp}^{\text{cut}}) = \frac{\Sigma^{\text{QCD, NLO}}(p_{\perp}^{\text{cut}})}{\Sigma^{\text{EFT, NLO}}(p_{\perp}^{\text{cut}})} \Sigma^{\text{EFT, NNLO}}(p_{\perp}^{\text{cut}})$$

p_T^{cut}	NNLO _{approximate quad.unc.} [fb]	HJ-MINLO [fb]	MG5_MC@NLO [fb]
400 GeV	$33.3^{+10.9\%}_{-12.9\%}$	$29^{+24\%}_{-21\%}$	$31.5^{+31\%}_{-25\%}$
430 GeV	$23.0^{+10.8\%}_{-12.8\%}$	-	$21.8^{+31\%}_{-25\%}$
450 GeV	$18.1^{+10.8\%}_{-12.8\%}$	$16.1^{+22\%}_{-21\%}$	$17.1^{+31\%}_{-25\%}$

Pier Monni @ 16th Workshop of HXSWG

Coming soon in the
LHCHSWG-2019-002(v2)

- Considerable contribution from VH, VBF and ttH
- Need state-of-the-art precision from all channels
- Sensitive to BSM models ~ new generation of quark



HIGGS RAPIDITY DISTRIBUTION AT N3LO



HIGGS PRODUCTION AT N3LO (APPROXIMATED)

- Extend qT-subtraction method to N3LO ([Cieri, XC et al. 1807.11501](#)).

In **qT (CSS)** factorisation to Higgs production at N3LO:

$$\frac{d\sigma}{dp_T^2 dy} = \frac{m_H^2}{s} \sigma_{LO}^H \int_0^{+\infty} db \frac{b}{2} J_0(bp_T) S_g(m_H, b) \sum_{a_1, a_2} \int_{x_1}^1 \frac{dz_1}{z_1} \int_{x_2}^1 \frac{dz_2}{z_2} [HC_1 C_2]_{gg:a_1 a_2} \prod_{i=1,2} f_{a_i/h_i}(x_i/z_i, b_0^2/b^2)$$

$$S_c(M, b) = \exp \left[- \int_{b_0^2/b^2}^{M^2} \frac{dq^2}{q^2} \left(A_c(\alpha_s(q^2)) \ln \frac{M^2}{q^2} + B_c(\alpha_s(q^2)) \right) \right]$$

- Apply q_T^{cut} to factorise full N3LO into two parts.

$$d\sigma_{N3LO}^H = \mathcal{H}_{N3LO}^H \otimes d\sigma_{LO}^H \Big|_{\delta(p_T)} + \left[d\sigma_{NNLO}^{H+jet} - d\sigma_{N3LO}^{H,CT} \right]_{p_T > q_T^{cut}}$$

- Above q_T^{cut} , recycle H+jet at NNLO from NNLOJET with qT counter terms (CT) to regulate IR divergence.
- Below q_T^{cut} , factorise real radiations from hard coefficient functions at $\delta(p_T)$ in HN3LO package.
- Most of the factorised components of $\delta(p_T)$ contribution are known analytically at N3LO.
- We use a constant $C_{N3} \delta_{ga} \delta_{gb} (1-z)$ to approximate the unknown pieces.
- Numerically abstract the C_{N3} coefficient using exact N3LO total cross section (1802.00833, 1802.00827).

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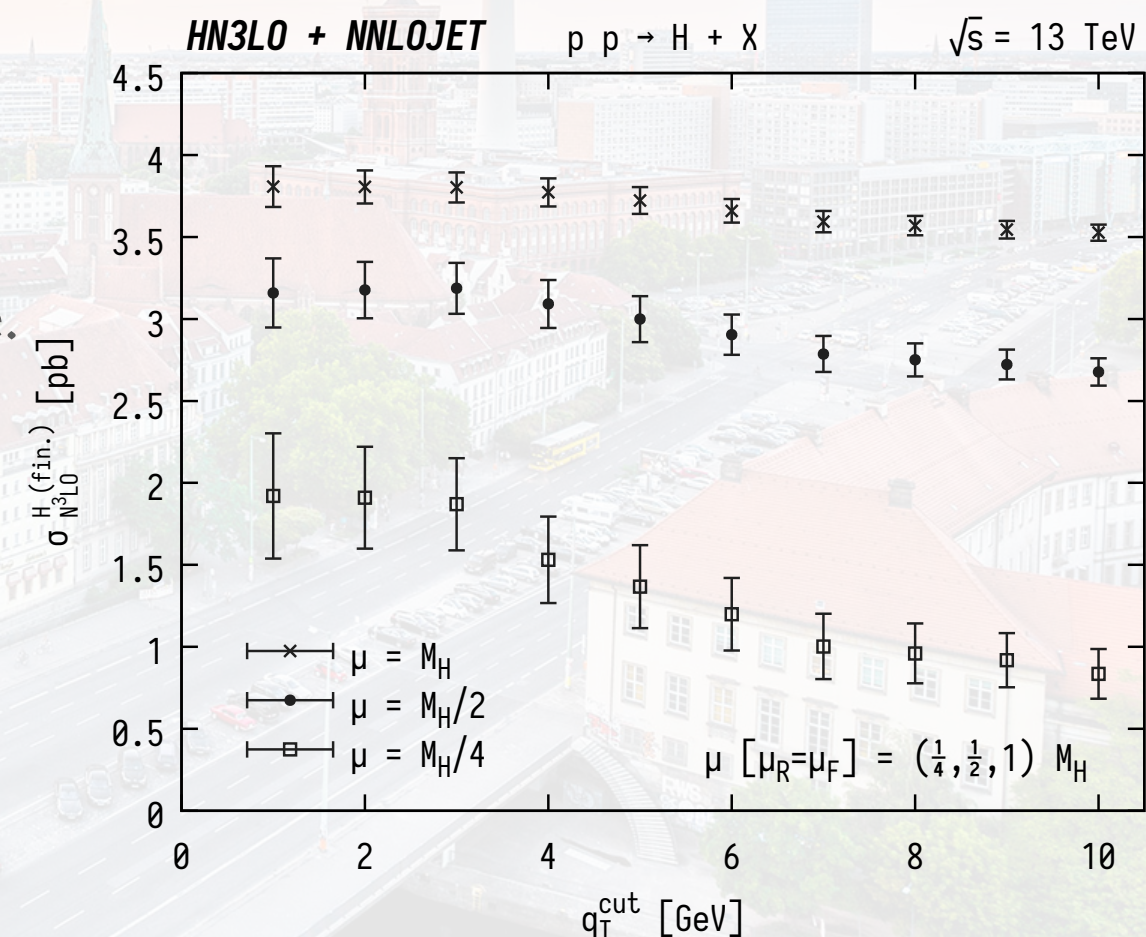
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- Apply q_T^{cut} to factorise full N3LO into two parts.

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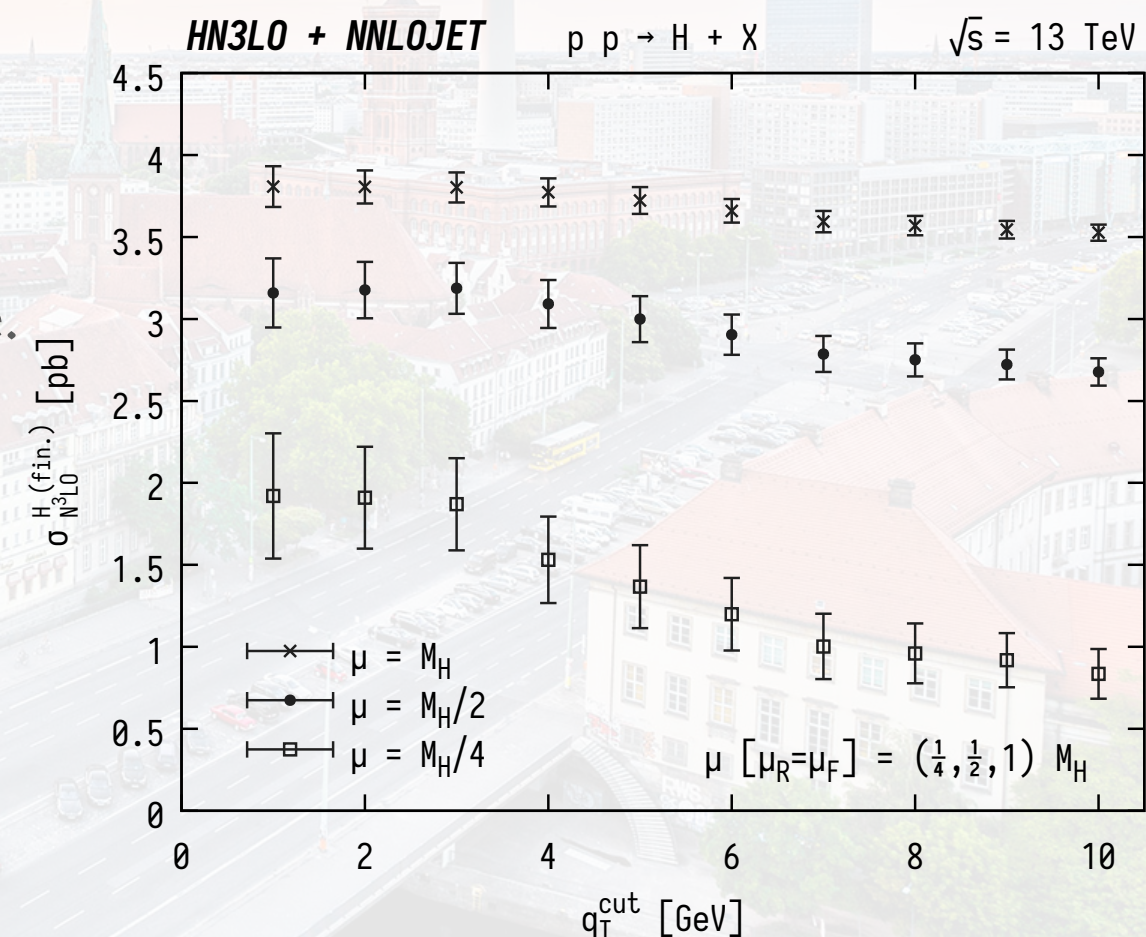
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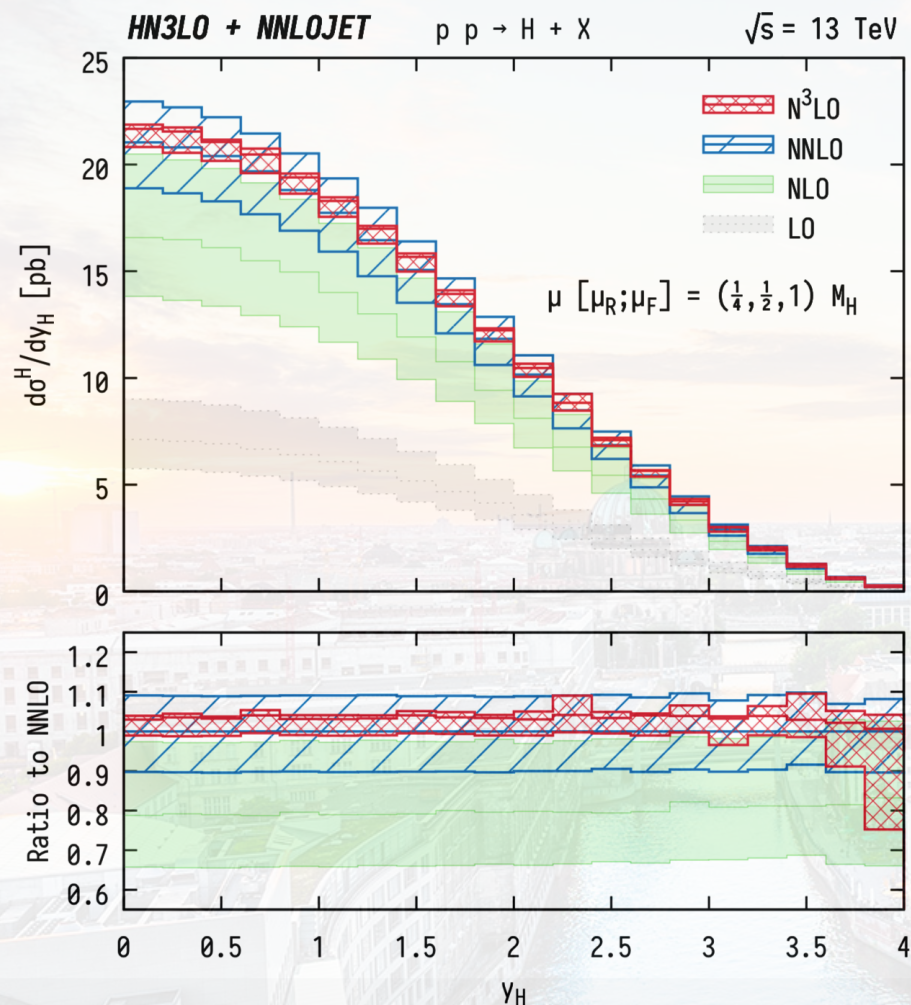
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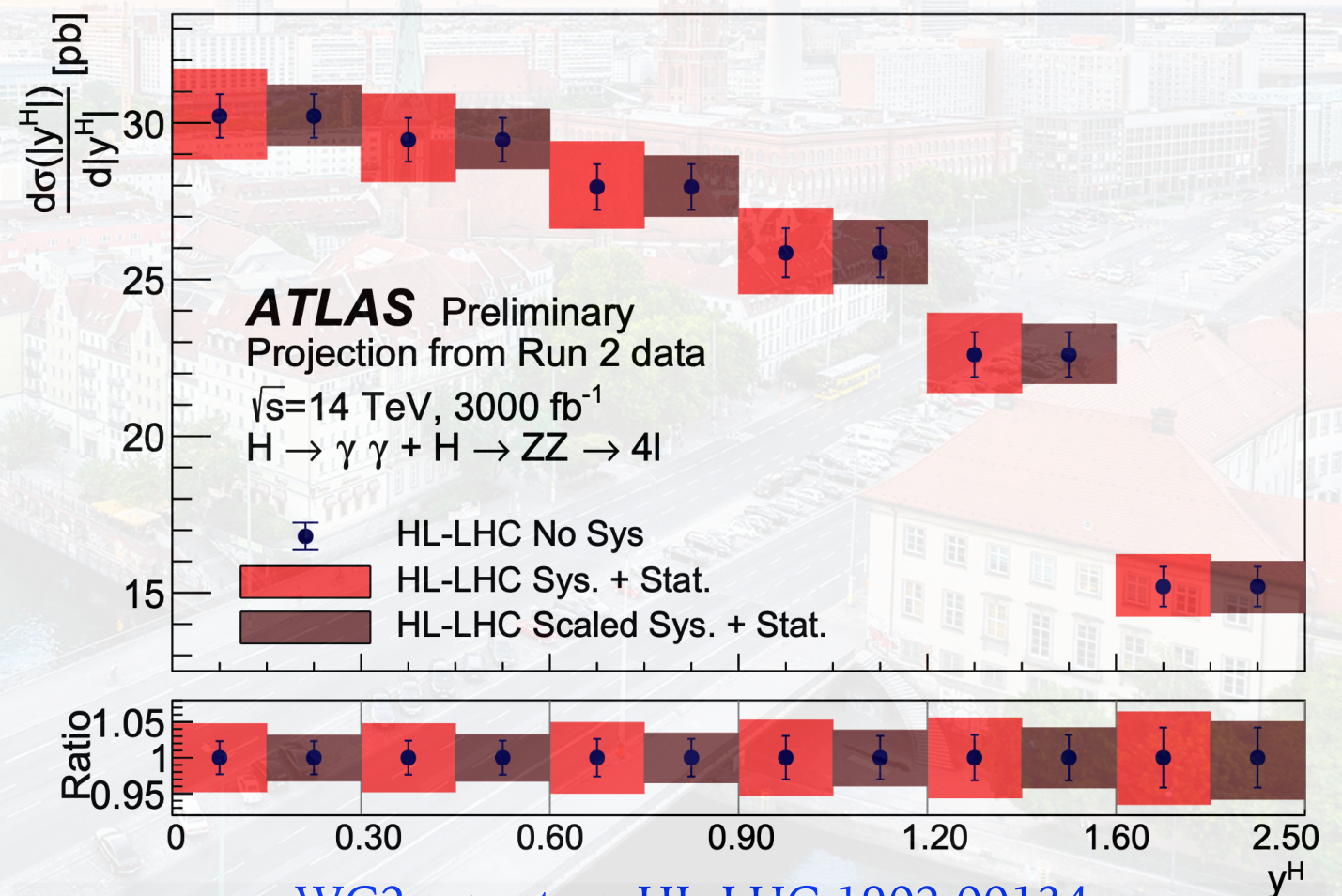


HIGGS RAPIDITY DISTRIBUTIONS AT N3LO (APPROXIMATED)

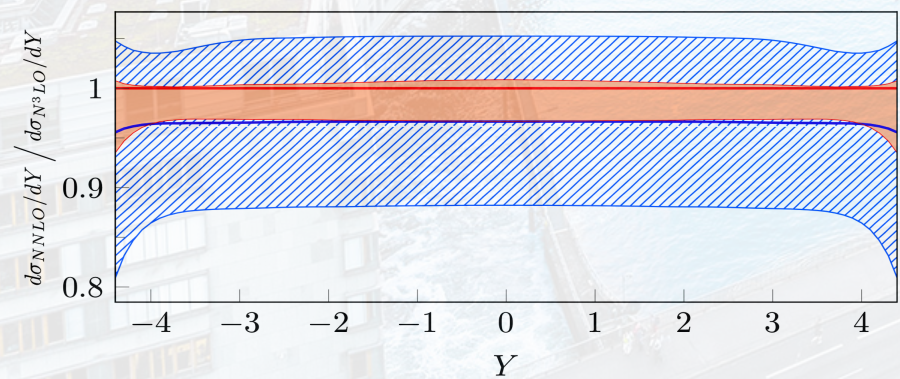
- N3LO differential observables at the LHC from qT-subtraction and threshold expansion



- Remarkably flat K-factor (as expected)
- QCD scale uncertainty reduced to $+1\%$ -3%
- Comparable to (S2) HL-LHC projections $\pm 3\%$
- Future upgrade to reduce PDF and α_s uncertainties



Cieri, XC, Gehrmann, Glover, Huss 1807.11501

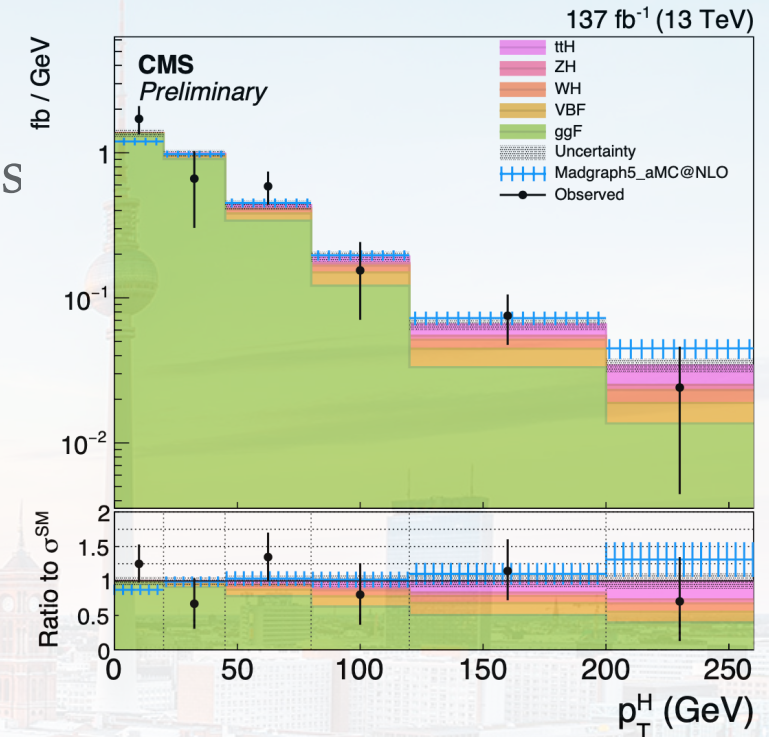


Dulat, Mistlberger, Pelloni 1810.09462

WG2 report on HL-LHC 1902.00134

FUTURE WORK

- Precision Higgs phenomenology
 - Compare and combine various production and decay channels
 - Top mass effects at large p_T region (PbP, full SM at RR)
- High precision prediction in general
 - Provide NNLO grids for PDF fitting (APLLfast)
 - Make NNLOJET public (Yes it will happen)
 - DY and W production at full differential N3LO
 - NNLO corrections of $\gamma+JJ$, $\gamma\gamma+J$, JJJ productions



$H \rightarrow 2l2\nu$ (HIG-19-002-pas)

hosted by CERN

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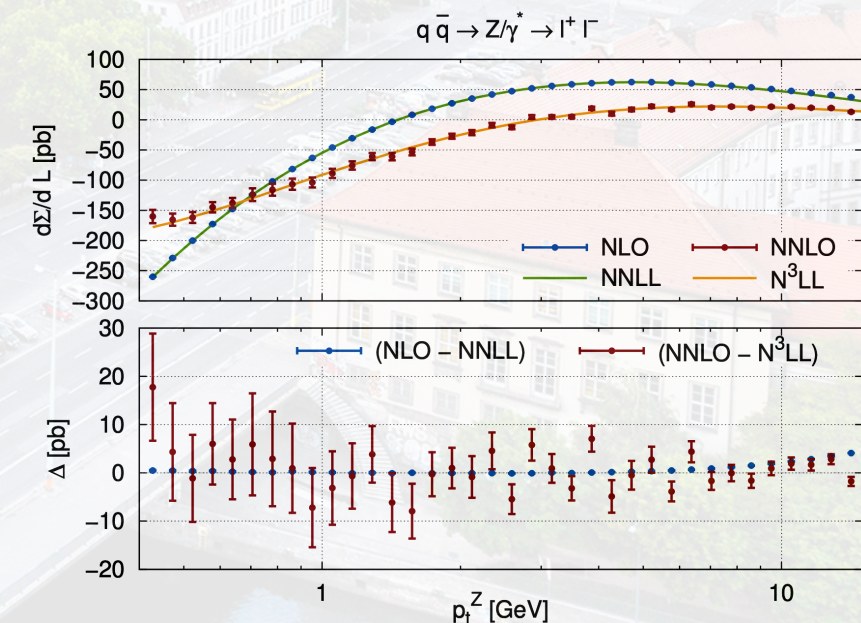
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Ploughshare allows users from the HEP community to share fast interpolation grids in a standardised way. PDF fitters and those from the experimental collaborations are able to upload their validated grids and access the grids of others quickly and with minimal fuss.

Experiment	Collision	Energy	Process	Calculation	Group	arxiv	tgz file direct link
H1	ep	300 GeV	incjets-appl	NNLOJET	APPLfast	0010054	applfast-h1-incjets-appl-arxiv-0010054
H1	ep	300 GeV	incjets-appl	NNLOJET	APPLfast	0706.3722	applfast-h1-incjets-appl-arxiv-0706.3722
H1	ep	300 GeV	incjets-appl	NNLOJET	APPLfast	0911.5678	applfast-h1-incjets-appl-arxiv-0911.5678
H1	ep	319 GeV	incjets-appl	NNLOJET	APPLfast	1406.4709	applfast-h1-incjets-appl-arxiv-1406.4709
H1	ep	319 GeV	incjets-appl	NNLOJET	APPLfast	1611.03421	applfast-h1-incjets-appl-arxiv-1611.03421
H1	ep	300 GeV	incjets-fnlo	NNLOJET	APPLfast	0010054	applfast-h1-incjets-fnlo-arxiv-0010054
H1	ep	300 GeV	incjets-fnlo	NNLOJET	APPLfast	0706.3722	applfast-h1-incjets-fnlo-arxiv-0706.3722
H1	ep	300 GeV	incjets-fnlo	NNLOJET	APPLfast	0911.5678	applfast-h1-incjets-fnlo-arxiv-0911.5678
H1	ep	319 GeV	incjets-fnlo	NNLOJET	APPLfast	1406.4709	applfast-h1-incjets-fnlo-arxiv-1406.4709
H1	ep	319 GeV	incjets-fnlo	NNLOJET	APPLfast	1611.03421	applfast-h1-incjets-fnlo-arxiv-1611.03421
ZEUS	ep	300 GeV	incjets-appl	NNLOJET	APPLfast	0208037	applfast-zeus-incjets-appl-arxiv-0208037
ZEUS	ep	300 GeV	incjets-appl	NNLOJET	APPLfast	0608048	applfast-zeus-incjets-appl-arxiv-0608048
ZEUS	ep	300 GeV	incjets-fnlo	NNLOJET	APPLfast	0208037	applfast-zeus-incjets-fnlo-arxiv-0208037
ZEUS	ep	300 GeV	incjets-fnlo	NNLOJET	APPLfast	0608048	applfast-zeus-incjets-fnlo-arxiv-0608048



<http://ploughshare.web.cern.ch>

Britzger et al. 1906.05303

Bizoń, XC, et al. 1805.05916

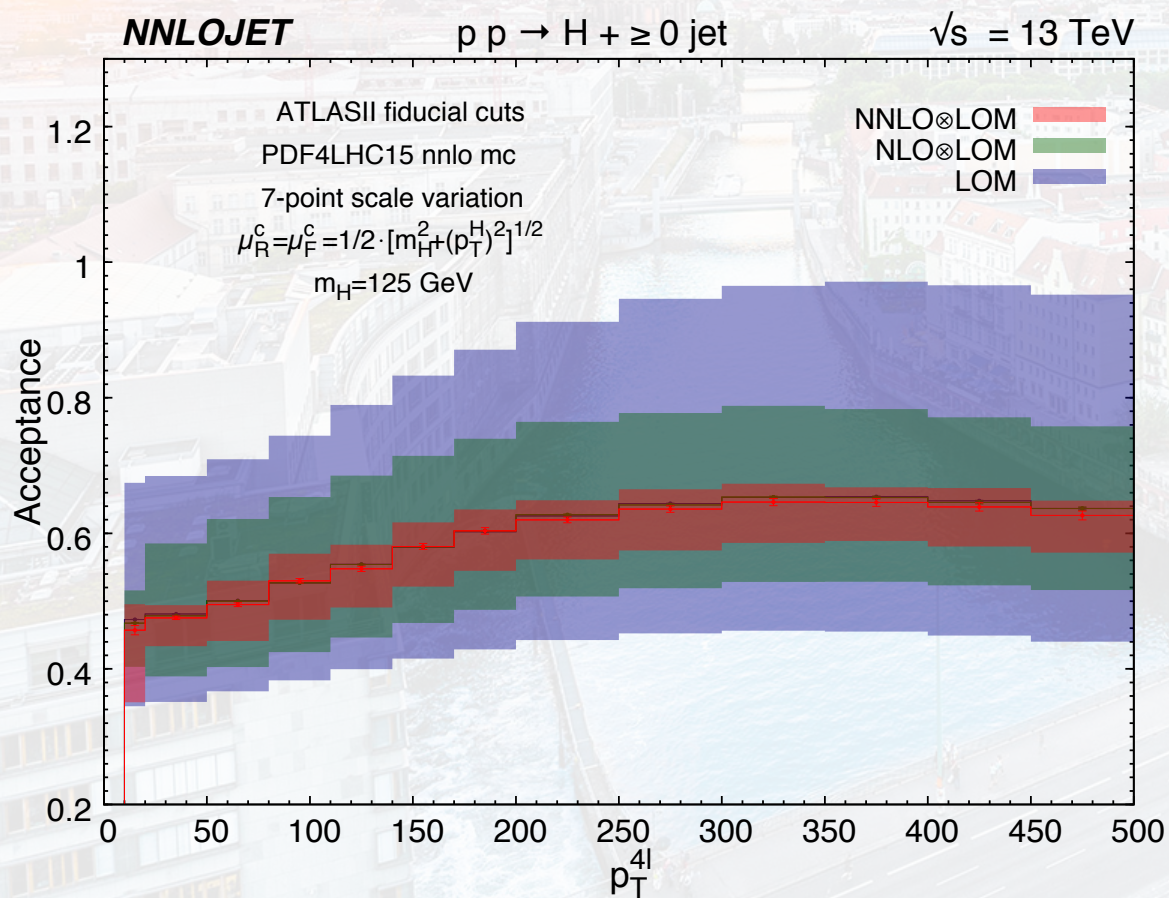
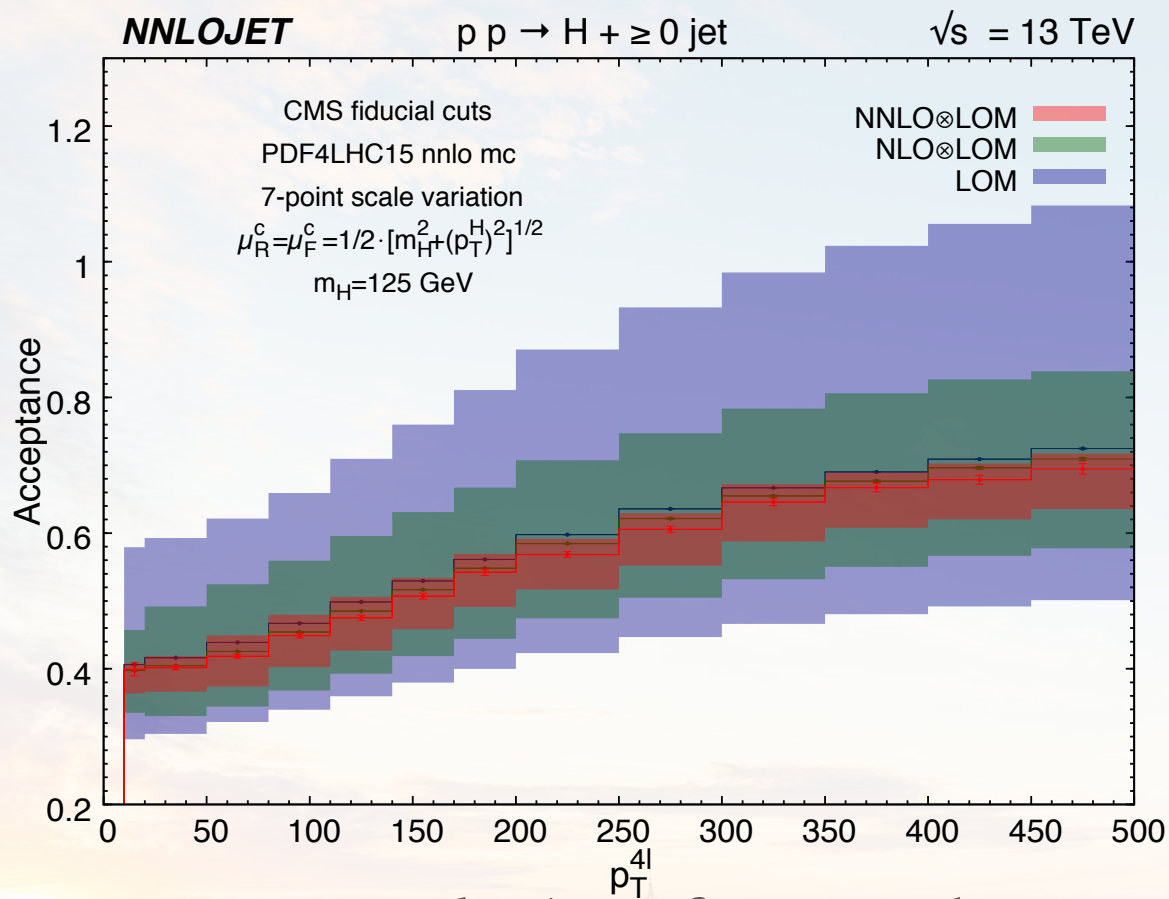
SUMMARY

- High Energy Physics is advancing to precision study at a **steady speed** and Higgs phenomenology will benefit from it. (Targets set for HL-LHC)
- Higgs boson precision **measurements focus** on differential observables and distinguishing production and decay channels
- Higgs boson precision **predictions focus** on reducing uncertainties from all sources. Major factor still from QCD
- NNLO QCD is the **new standard** for Higgs production channels, more consistent update to PDF and α_s will be available in the future
- NNLO+N3LL and N3LO predictions are available for limited observables. With realistic projection of theory progresses, we can expect **promising** precisions at HL-LHC accuracy.
- Many important studies are desired in the future: quark mass, parton shower beyond LO and LL, $\alpha\alpha_s$ mixing, interference contributions etc.



*Thank You for
your Attention*

Total time (int. dimension Of the tree level)	L0	NLO	NNLO
H	1 min (3)	30 min (6)	300h (9)
H→di-photon	1 min (3)	40 min (6)	400h (9)
H→4l (2e2mu, 4e, 4mu require at least two separate runs)	2~3 min (9)	2h (12)	1000h (15)
H+j	3 min (6)	1.5h (9)	70000h (12)
H→di-photon + jet	4 min (6)	2h (9)	90000h (12)
H→4l (2e2mu, 4e, 4mu require at least two separate runs)+jet	20 min (12)	10h (15)	600000h (18)
H_qT	20 min (6)	5h (9)	7000000h (12)



ACCEPTANCE STUDY

$$H \rightarrow ZZ^* \rightarrow 4l$$

- CMS ([1706.09936](#)) and ATLAS ([1708.02810](#)) use different lepton isolation algorithm in $ZZ^* \rightarrow 4l$

Fiducial Cuts	CMS	ATLAS
Lepton Isolation		
Cone size R^l	0.3	—
$\sum p_T^i / p_T^l \ (i \in R^l)$	< 35%	—
$\Delta R^{SF(DF)}(l_i, l_j)$	> 0.02	> 0.1 (0.2)
Jet Definition (anti-kT with R=0.4)		
$p_T^{jets} \text{ (GeV)}$	> 30	> 30
$ y^{jets} $	< 2.5	< 4.4
$\Delta R(jet, e(\mu))$	—	> 0.2 (0.1)

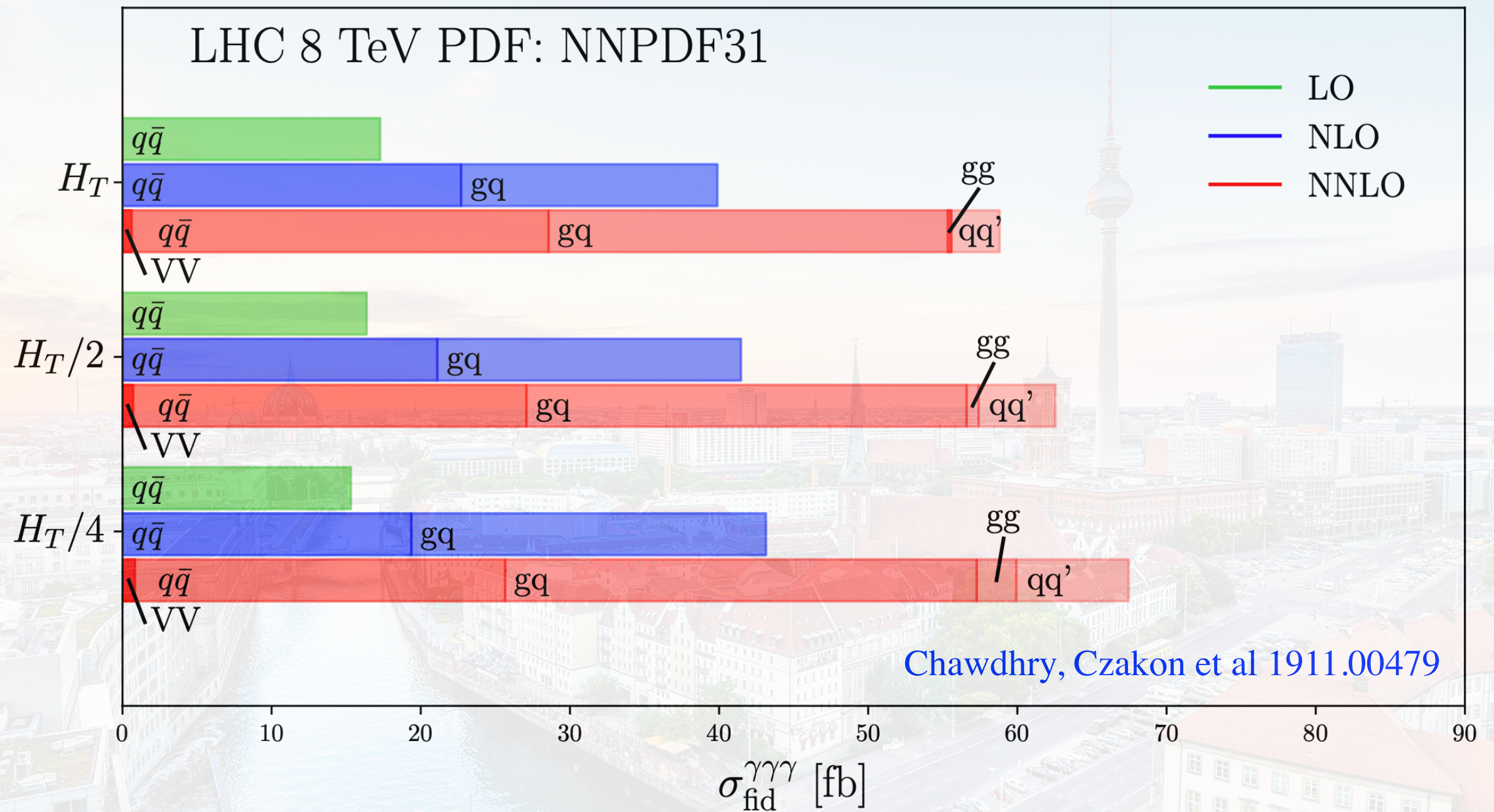
- Fixed order study of acceptance reveals detailed structures

$$A_{FO}(\mathcal{O}) = \frac{d\sigma_{FO}^{H(\rightarrow ZZ^* \rightarrow 4l) + jet} / d\mathcal{O}}{d\sigma_{FO}^{H+jet} / d\mathcal{O} \times (BR_{2e2\mu} + BR_{4\mu} + BR_{4e})}$$

Acceptance consistent for each FO

APPROXIMATION IN $pp \rightarrow \gamma\gamma\gamma$ @NNLO

central scale choice μ_0



- Anatomy of higher-order corrections to the three-photon fiducial cross-section
- VV is the scale-independent part of the two-loop finite remainder (CL without quark loop)
- The missing contributions are expected to be similar or less than current VV