Er violation in Kaons E an emerging anomaly

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Outline

CP Violation

e'/e Anatomy

NNLO calculation

Future improvements

Conclusions

Big mystery of the Universe

Very early in the Universe might expect equal numbers of baryons & anti-baryons.

However, today the Universe is matter dominated. (no evidence for anti-galaxies, etc.)



How did this happen?

Matter-antimatter asymmetry

- A. Baryon violating interactions
- B. CP violation [Andrei Skharov. '67]
- C. Thermal non-equilibrium situation

CP violation

CP violation is an essential aspect of our understanding of the Universe.

There are two places in the SM where CP violation enters:

- a. The PMNS matrix
- b. The CKM matrix

To date CP violation has been observed only in the quark sector & the SM is unable to account for the observed matter-antimatter asymmetry in the Universe.

We need more CP violation (new sources of CP violation at high energy scales)

CP violation in Kaons

Two possible explanations of CP violation in the kaon system:

A. KL is a superposition of CP states:

Indirect CP violation: parameter eK

B. CP is violated in the decay of KL: Direct CP violation: parameter e'

Defining the CP violation ratios

$$\eta_{+-} = \frac{\langle \pi^{+}\pi^{-} | \mathcal{H}_{eff} | K_{L} \rangle}{\langle \pi^{+}\pi^{-} | \mathcal{H}_{eff} | K_{S} \rangle} \qquad \eta_{00} = \frac{\langle \pi^{0}\pi^{0} | \mathcal{H}_{eff} | K_{L} \rangle}{\langle \pi^{0}\pi^{0} | \mathcal{H}_{eff} | K_{S} \rangle}$$

Indirect & Direct CP violation can be expressed

$$\varepsilon = (\eta_{00} + 2\eta_{+-})/3$$
 $\varepsilon' = (\eta_{+-} - \eta_{00})/3$

Direct CP violation

A non-zero value of Re(e'/e) signals that direct CPV exists

The measured quantity is the double ratio of the decay widths

$$R = \left| \frac{\eta_{00}}{\eta_{+-}} \right|^2 = \frac{\Gamma(K_L \to \pi^0 \pi^0) \Gamma(K_S \to \pi^+ \pi^-)}{\Gamma(K_L \to \pi^+ \pi^-) \Gamma(K_S \to \pi^0 \pi^0)}$$

(a long series of precision counting experiments)

From NA48 and KTeV collaborations:

$$\left(\frac{\varepsilon'}{\varepsilon}\right)_{\text{exp}} = (16.6 \pm 2.3) \times 10^{-4}$$

c/c in the 5M I

$$\begin{split} \langle \pi^0 \pi^0 | \, \mathcal{H}_{\mathrm{eff}} | \, K^0 \rangle &= A_0 \, \, e^{i\delta_0} + A_2 \, \, e^{i\delta_2} / \sqrt{2} \\ \langle \pi^+ \pi^- | \, \mathcal{H}_{\mathrm{eff}} | \, K^0 \rangle &= A_0 \, \, e^{i\delta_0} - A_2 \, \, e^{i\delta_2} / \sqrt{2} \\ \langle \pi^+ \pi^0 | \, \mathcal{H}_{\mathrm{eff}} | \, K^0 \rangle &= 3 A_2^+ \, \, e^{i\delta_2^+} / 2 \end{split}$$

Ao & Az: Isospin amplitudes for isospin conservation

$$A_I e^{i\delta_I} \equiv \langle (\pi\pi)_I | \mathcal{H}_{\text{eff}} | K \rangle$$

Normalise to K+ decay (w_+,a) and e_K expand in A_2/A_0 and CP violation

Ao, Az & Az+
from experiment
[Cirigliano. et. al. '11]

The CPV is parametrised as,

$$\frac{\varepsilon'}{\varepsilon} = -i \frac{\omega_{+}}{\sqrt{2} |\varepsilon_{K}|} e^{i(\delta_{2} - \delta_{0} - \phi_{\varepsilon_{K}})} \left[\frac{\text{Im} A_{0}}{\text{Re} A_{0}} (1 - \hat{\Omega}_{\text{eff}}) - \frac{1}{a} \frac{\text{Im} A_{2}}{\text{Re} A_{2}} \right]$$

[Buras, Gorbahn, Jäger, Jamin '15]

[Cirigliano et. al. '11]

e/e in the 5M II

$$\omega_{+} = a \frac{\text{ReA}_{2}}{\text{ReA}_{0}} = (4.53 \pm 0.02) \times 10^{-2}$$

From experiment [Cirigliano et. al. '03]

$$\frac{\varepsilon'}{\varepsilon} = -i \frac{(\omega_+)}{\sqrt{2(\varepsilon_K)}} e^{i(\delta_2 - \delta_0 - \phi_{\varepsilon_K})} \left[\frac{\text{Im} A_0}{\text{Re} A_0} (1 - \hat{\Omega}_{\text{eff}}) - \frac{1}{a} \frac{\text{Im} A_2}{\text{Re} A_2} \right]$$
 From experiment

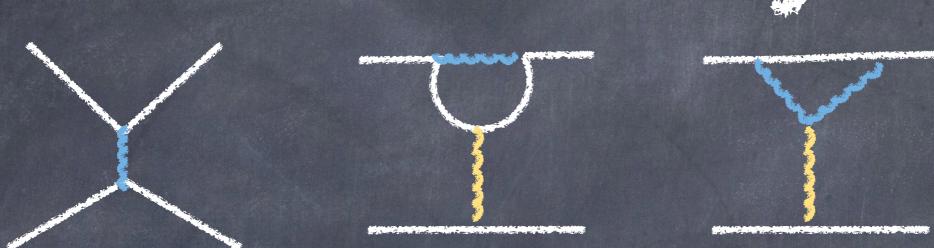
$$A_I e^{i\delta_I} \equiv \langle (\pi\pi)_I | \mathcal{H}_{\text{eff}} | K \rangle = \sum_i C_i (\langle (\pi\pi)_I | Q_i | K))$$

Leading isospin breaking [Cirigliano et. al. '03]

First-ever calculation with controlled errors

[Blum et. al., Bai et. al. '15]

Kath decays



CP symmetry is broken by the complex phase appearing in the quark mixing matrix

$$V^{\text{CKM}} = \begin{pmatrix} 1 - \lambda^2/2 & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \lambda^2/2 & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{pmatrix}$$

5-d >5 ~10-4

The CP violation is small because of flavour suppression

Weak Effective Theory

Effective Hamiltonian at $\mu < m_c$

$$\mathcal{H}_{\text{eff}} = \frac{G_F}{\sqrt{2}} V_{ud} V_{us}^* \sum_{i=1}^{10} \left(z_i(\mu) + \tau y_i(\mu) \right) Q_i$$

$$\tau \equiv -\frac{V_{td}V_{ts}^*}{V_{ud}V_{us}}$$

Perturbative Wilson coefficients

Only the imaginary part of tau is responsible for CPV (everything else is pure-real)

Theoretically very complicated multi-scale problem (weak scale, bottom, charm, QCD scale)

Operators

Current-Current:

$$Q_1 = (\bar{s}_{\alpha} u_{\beta})_{V-A} (\bar{u}_{\beta} d_{\alpha})_{V-A}, \quad Q_2 = (\bar{s}u)_{V-A} (\bar{u}d)_{V-A}$$

Large coefficients, but CP-conserving (y=0). Account for K->pipi decay rates.

QCD-Penguins:

$$Q_{3} = (\bar{s}d)_{\text{V-A}} \sum_{q} (\bar{q}q)_{\text{V-A}}, \quad Q_{4} = (\bar{s}_{\alpha}d_{\beta})_{\text{V-A}} \sum_{q} (\bar{q}_{\beta}q_{\alpha})_{\text{V-A}}$$

$$Q_{5} = (\bar{s}d)_{\text{V-A}} \sum_{q} (\bar{q}q)_{\text{V+A}}, \quad Q_{6} = (\bar{s}_{\alpha}d_{\beta})_{\text{V-A}} \sum_{q} (\bar{q}_{\beta}q_{\alpha})_{\text{V+A}}$$

$$Q_{6} = (\bar{s}d)_{\text{V-A}} \sum_{q} (\bar{q}_{\beta}q_{\alpha})_{\text{V+A}}$$

 $O(\alpha_s)$ but CP-violating (y=!0). However, isospin-0 final state only.

Operalors II

The operators Q3, Q4, Q5, $\not\in$ Q6 are pure I=1/2 operators In the isospin limit: $\langle Q_3 \rangle_2 = \langle Q_4 \rangle_2 = \langle Q_5 \rangle_2 = \langle Q_6 \rangle_2 = 0$

EW-Penguins:

$$Q_{7} = \frac{3}{2} (\bar{s}d)_{V-A} \sum_{q} e_{q} (\bar{q}q)_{V+A}, \quad Q_{8} = \frac{3}{2} (\bar{s}_{\alpha}d_{\beta})_{V-A} \sum_{q} e_{q} (\bar{q}_{\beta}q_{\alpha})_{V+A}$$

$$Q_{9} = \frac{3}{2} (\bar{s}d)_{V-A} \sum_{q} e_{q} (\bar{q}q)_{V-A}, \quad Q_{10} = \frac{3}{2} (\bar{s}_{\alpha}d_{\beta})_{V-A} \sum_{q} e_{q} (\bar{q}_{\beta}q_{\alpha})_{V-A}$$

 $O(\alpha_e)$ but can create isospin-2 state. Needed for direct CPV!

IMA2/REA2: (V-A)X(V-A)

Let us first consider only pure left-handed operators

$$Q_1 = (s_\alpha u_\beta)_{V-A} (u_\beta d_\alpha)_{V-A} Q_9 = (s_\alpha d_\alpha)_{V-A} \Sigma_q e_q (q_\beta q_\beta)_{V-A}$$

$$Q_2 = (\overline{s}_{\alpha} u_{\alpha})_{V-A} (\overline{u}_{\beta} d_{\beta})_{V-A} Q_{10} = (s_{\alpha} d_{\beta})_{V-A} \Sigma_q e_q (q_{\beta} q_{\alpha})_{V-A}$$

Fierz identities & isospin limit imply

$$\langle Q_9 \rangle_2 = \langle Q_{10} \rangle_2 = 3/2 \langle Q_+ \rangle_2$$

with $<Q_{\pm}>_{I} = (<Q_{2}>_{I} \pm <Q_{1}>_{I})/2$.

The V-A contribution to the ratio I=2

$$\left(\frac{\text{Im}A_2}{\text{Re}A_2}\right)_{V-A} = \text{Im}\tau \frac{y_9 + y_{10}}{z_+}$$
 Cancellation of matrix elements

is perturbatively calculable without non-perturbative input.

IMAO/REAO: (V-A)X(V-A)

More operators contribute to ImAo/ReAo.

Fierz relations for (V-A)x(V-A) operators give:

$$\langle Q_4 \rangle_0 = \langle Q_3 \rangle_0 + 2 \langle Q_- \rangle_0$$

Using the theoretical definition for ReAo:

$$\left(\frac{\text{Im}A_0}{\text{Re}A_0}\right)_{V-A} = \text{Im}\tau \ 2 \ \frac{y_4}{1+q} \ z_- + \mathcal{O}(p_3)$$

Where q is the only hadronic input (numerically very small)

$$q = \frac{z_{+}(\mu) < Q_{+}(\mu) > 0}{z_{-}(\mu) < Q_{-}(\mu) > 0}$$

(V-A)x(V+A) Contributions

Q6 & Q8 give the leading contribution to ImA0 & ImA2, respectively

$$\left(\frac{\text{Im}A_0}{\text{Re}A_0}\right)_6 = -\frac{G_F}{\sqrt{2}} \text{Im}\lambda_t y_6 \frac{\langle Q_6 \rangle_0}{\text{Re}A_0}$$

$$\left(\frac{\text{Im}A_2}{\text{Re}A_2}\right)_8 = -\frac{G_F}{\sqrt{2}} \text{Im}\lambda_t y_8^{\text{eff}} \frac{\langle Q_8 \rangle_2}{\text{Re}A_2}$$

To reduce the error on non-perturbative input take the real parts from CP conserving data.

state of phenomenology

[Buras, Gorbahn, Jäger, Jamin '15]
$$(\varepsilon'/\varepsilon)_{\text{SM}} = (1.9 \pm 4.5) \times 10^{-4}$$

$$(\varepsilon'/\varepsilon)_{\text{exp}} = (16.6 \pm 2.3) \times 10^{-4}$$

2.90 discrepancy

The error is completely dominated by the non-perturbative sector

[Blum et. al., Bai et. al. '15]

Perturbative error are only estimates

Quantit	Error	Quantity	Error
B ₆ (1/2)	4.1	$m_d(m_c)$	0,2
NNLO	1,6	q	0,2
$\hat{\Omega}_{ ext{eff}}$	0,7	B8(1/2)	0,1
9 3	0,6	772	0,1
B ₈ (3/2)	0,5	1 270	0.1
p _s	0.4	$\alpha_s(M_Z)$	0.1
ms(mc)	0,3		
me(me)	0,3	All unites i	in 10-4

Why does a single matrix element dominate the error?

Reao & Rear known from CP-conserving data

Fierz Identities
7 independent
operators

Better control over <Qi>2 on lattice

EWP suppressed in I=0 (α/α_s)

QCDP cannot create I=2

Colour hierarchies
between
matrix elements,
Wilson coefficients

QCDP Dominate ImAo IMA2 due to EWP Broken by

QED & mu =! md

Estimated separately

Miny e/e is so small?

The prediction of e'/e very sensitive to interplay between QCD (Q_6) \neq electroweak (Q_8) penguin operators

$$\varepsilon'/\varepsilon = 10^{-4} \left[\frac{\text{Im}\lambda_t}{1.4 \times 10^{-4}} \right] \left[a(1 - \hat{\Omega}_{\text{eff}})(-4.1(8) + 24.7 B_6^{(1/2)}) + 1.2(1) - 10.4 B_8^{(3/2)} \right]$$

[Blum et. al., Bai et. al. '15]

(B6=0.57(19) & B8=0.76(5))

Cancellation between QCD & EW penguin operators.

Electroweak operators are very sensitive to new physics.

Is New Physics there

Are we missing important contributions in the SM?

New physics might not be the reason of the tension

 $\langle Q_i \rangle$ off

Missing SM ...

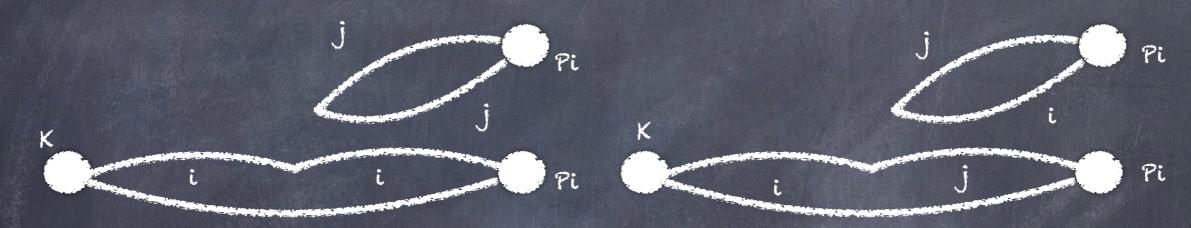
QCD corrections

Missing SM ... EW corrections Missing ...
QED corrections

Deeper understanding of the SM is crucial

Long distance Inc

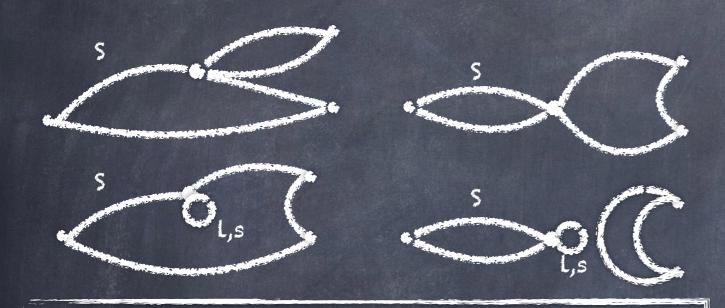
There are only three operators which contribute to Az and only two types of diagrams



The major challenge here it is to ensure that the pions have physical momenta

Long distance Iso

The calculation of Ao is more challenging than the evaluation of Az



 $C_{K,\pi\pi}^{i}(t_{K},T_{Q},T_{\pi\pi}) = \langle 0 | J_{\pi\pi}(t_{\pi\pi}) | Q_{i}(t_{Q}) | J_{K}(t_{K}) | 0 \rangle$

Challenges

Vacuum subtraction Ground-state two-pion energy

ππ phase shift from 2015 results: δ0=(23.8±4.9±2.2)=

Compared with dispersion theory result 34°

Puzzle resolved by adding more interpolating operators for $\pi\pi$ states $\delta_0=(30.0\pm1.5\pm3)^2$

Why is important to compute e'/e at NNLO?

The theory prediction for e'/e only at NLO at the moment. \$\pi\$ higher order dimensional operators are not included in the error estimate (expected to be small)

$$\mathcal{O}(p^2/m_c^2) = (m_K - 2m_\pi)^2/(2m_c)^2$$

- 1. Prospects for improvement on <@i> are good. Controlling other sources of uncertainties will become important soon.
 - 2. Higher order corrections could have a huge impact on e'/e.
- 3. The convergence of perturbation theory at mois not clear.

status of e/e at NNLO

Energy	Fields	Order	Paper
	a. Y. W. Z. h	NNLO Q1-Q6, Q89	[Misiak, Bobeth, Urban]
μw	9, 8, W, Z, h u, d, s, c, b, t	NNLO EWP	[Gambino, Buras, Haisch]
RGE	9, 8, u, d, s, c, b,	NNLO Q1-Q6, Q89	[Gorbahn, Haisch]
μь	9, 8, u, d, s, c,	NNLO Q1-Q6	[Gorbahn, Brod]
RGE	9, 8, u, d, s, c	NNLO Q1-Q6, Q89	[Gorbahn, Haisch]
μ _c	9, 8, u, d, s, c	NLO Q1-Q10	[Buras, Jamin, M.E.L]
RGE	9, 8, u, d, s	NNLO Q1-Q6, Q89	[Gorbahn, Haisch]
µ lattice	g, u, d, s	NLO Q1-Q10	[Blum et. al., Bai et. al. '15]

MMLO corrections

NNLO weak Hamiltonian only known above bottom mass.

(from B->Xs gamma)

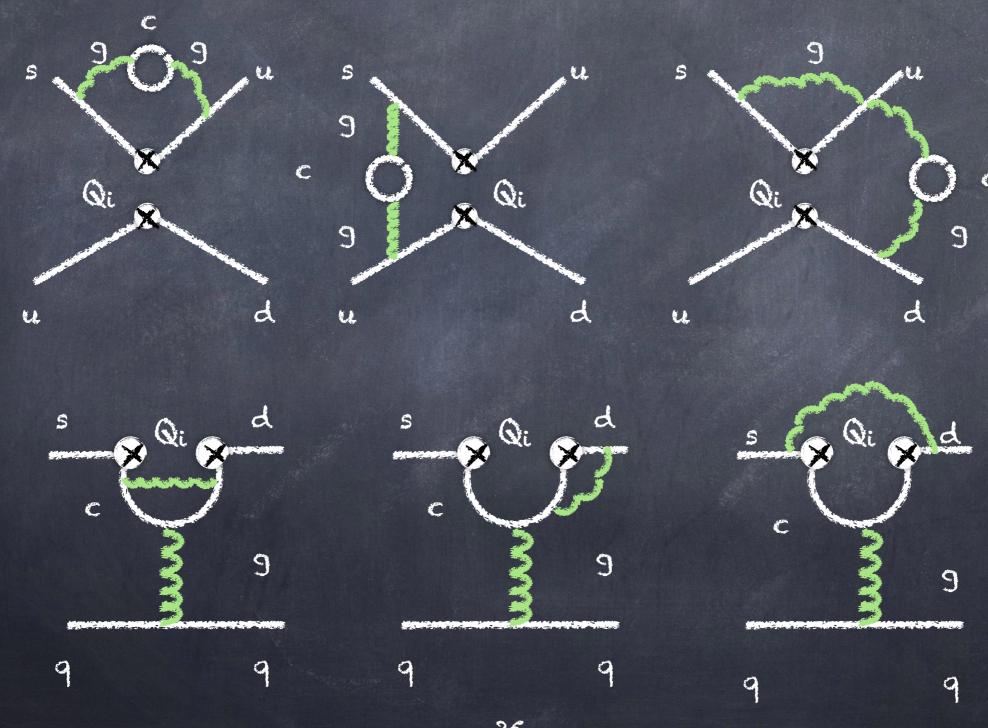
Analysis of e'/e requires bottom & charm threshold corrections & also NNLO mixing of QCD into EWP.

These threshold corrections are determined through a matching of the effective theories with nf and nf+1 flavours.

Aeff(nf+1) = Aeff(nf)

Charm malching at NNLO

Calculation of two-loop diagram with inserted operators



Operator basis for NNLO

The traditional basis requires the calculation of traces with ys

Issues with the treatment of the Y_5 in D-dimensions Higher order calculations can be significantly simplifies if we use a different operator basis

$$0s = (s_i \ y_{\mu} \ y_{\nu} \ y_{\rho} \ P_L \ d_j)_{\nu-A} (q_K \ y^{\mu} \ y_{\nu} y_{\rho} \ q_L)$$

$$s \quad 0s \quad d \quad s \quad 0s \quad d$$

$$c \quad y_{\rho} \quad y_{\rho}$$

Relation to traditional basis not trivial in D-dimensions

To work in dimensional regularisation

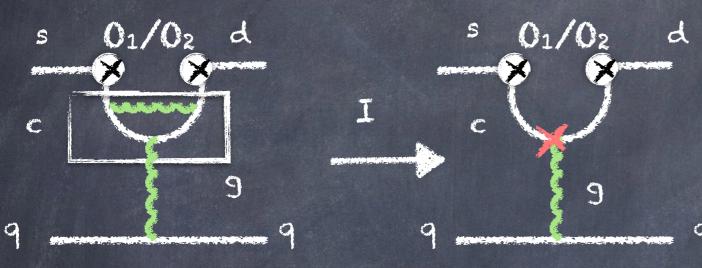
To renormalise the theories in the MS-bar scheme

To expand the external momenta up to $O(k^2)$ To set the mass of the light quarks to zero

This introduces Infrared Divergences in the nf+1 theory amplitude which have to be cancelled by the Ultra-Violet divergences in the nf flavour theory

Renormalisation

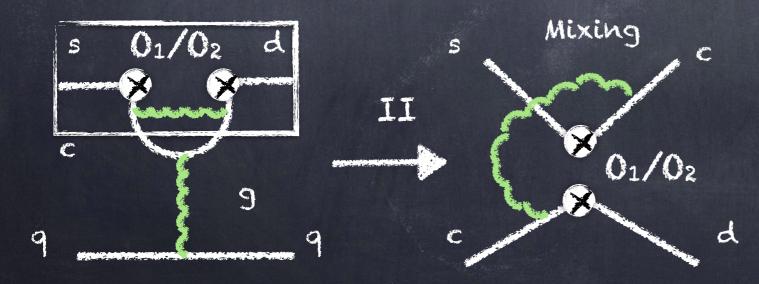
2-loop diag.: 1/eps2 & 1/eps poles



STEP I:

eps² pole is cancelled Vereps² is not fully cancelled

One-loop diag with inserted counter-term



STEP II:

Mixing of cc required to get a finite result

CUMULAG

Matrix elements are computed in the 3-flavour theory & the perturbative corrections have the factorised structure:

$$C^{(3)}(\mu_L) = U^{(3)}(\mu_L, \mu_c) \cdot M^{(34)}(\mu_c) \cdot U^{(4)}(\mu_c, \mu_b) \cdot M^{(45)}(\mu_b) \cdot U^{(5)}(\mu_b, \mu_W) \cdot C^{(5)}(\mu_W)$$

NNLO for the isospin-0 amplitude now complete

The short-distance contributions are $\mu-$ and scheme-dependent But, observables do not depend on $\mu-$ scale or the scheme used.

$$C_i(3)(\mu_L)(3)(\mu_L)$$
 Cancellation!!

 $<Q_i>>(µ_L)$ are needed in the same scheme and for the same scale or ideally as a function of µ.

Conversion to the MS scheme

Perturbation theory is easiest and most transparent in dimensional regularisation with minimal subtraction.

What about the matrix elements?

STEP I: <Qi> are renormalised non-perturbatively in the RI-SMOM scheme.

STEP II: Match to the traditional operator basis in the continuum MS-bar renormalisation scheme using NDR:

$$\langle Q_i \rangle^{\overline{\mathrm{MS}}} (\mu_L) = \left[T^{(0)} + \alpha_s(\mu_L) T^{(1)} \right]_{ij} \langle Q_j \rangle^{\mathrm{RI-SMOM}}$$

Unknown master Feynman integrals from two loops.

More complicated than perturbative Wilson coefficients.

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Definition of the renormalised operators consistent with the scheme used in the calculation of the Wilson coefficients.

NDR-scheme, & Hooft and Vellman-scheme, RI-scheme

In some cases, the differences between different schemes may be numerically large

To avoid all these problems, it is convenient to introduce a renormalisation group invariant definition of Wilson coefficients and composite operators

This relies on the fact that, $U(\mu,\mu_0)=u(\mu)u(\mu_0)-1$

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 $<Q_{7}^{(3)}(\mu_{L})C^{(3)}(\mu_{L})=<Q_{7}(\mu_{L})U^{(3)}(\mu_{L},\mu_{c})M^{(34)}(\mu_{c})U^{(4)}(\mu_{c},\mu_{b})$ $\times M^{(45)}(\mu_{b})U^{(5)}(\mu_{b},\mu_{W})C^{(5)}(\mu_{W})$

The contribution of running, $U(\mu,\mu_0)$, and matching, $M(\mu_q)$, can be factorised in terms of scheme & scale independent quantities:

$$\langle Q \rangle^{(3)}(\mu_L) \ C^{(3)}(\mu_L) = \langle \hat{Q} \rangle^{(3)} . \hat{M}^{(34)} . \hat{M}^{(45)} . \hat{C}^{(5)}$$

where,

$$\langle \hat{Q} \rangle = \langle Q \rangle (\mu_L) \,. \, u^{(3)}(\mu_L), \qquad \hat{M}^{(34)} = u^{(3)-1}(\mu_c) \,. \, M^{(34)}(\mu_c) \,. \, u^{(4)}(\mu_c)$$
$$\hat{C}^5 = u^{(5)-1}(\mu_W) \,. \, C^{(5)}(\mu_W), \qquad \hat{M}^{(45)} = u^{(5)-1}(\mu_b) \,. \, M^{(45)}(\mu_b) \,. \, u^{(5)}(\mu_b)$$

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In the RGI scheme:

- 1. halted matrix elements satisfy d=4 Fierz identities missing $O(\alpha_s)$ corrections for the Fierz identities are also included.
- 2. All halted quantities & also their products

$$\hat{C}^{(3)} = \hat{M}^{(34)} \cdot \hat{M}^{(35)} \cdot \hat{C}^{(5)}$$

are formally scheme and scale independent.

But they show residual μ dependence that is expected to reduce order by order # that is of the size of higher order corrections.

Results at NNLO

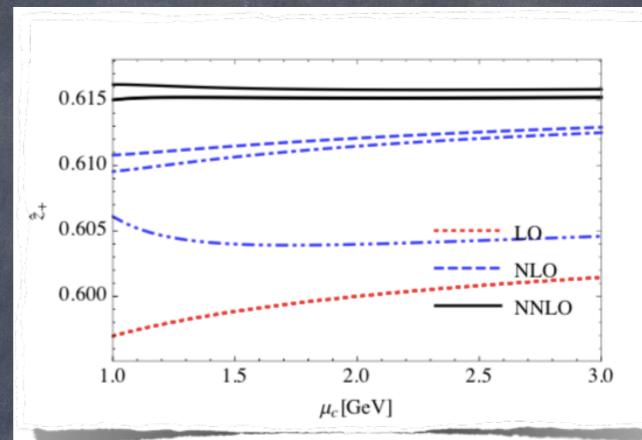
The real part of Ao & Az is dominated by z+ & z-

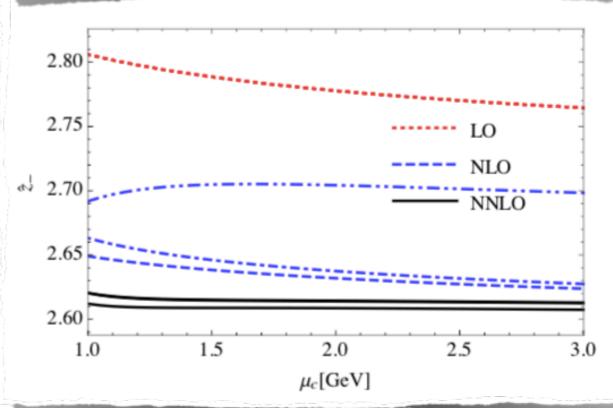
$$\begin{aligned} \operatorname{ReA}_2 &= \hat{z}_+ \langle \hat{Q}_+ \rangle_2 \\ \operatorname{ReA}_0 &= \hat{z}_+ \langle \hat{Q}_+ \rangle_0 + \hat{z}_- \langle \hat{Q}_- \rangle_0 \end{aligned}$$

The residual μ_c dependence reduces order by order

At NLO there is still a dependence on the implementation of α_s running

Shift probably due to running down from Mz



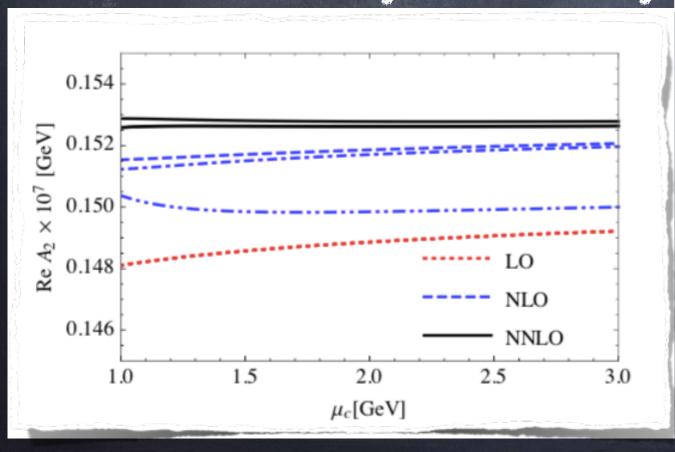


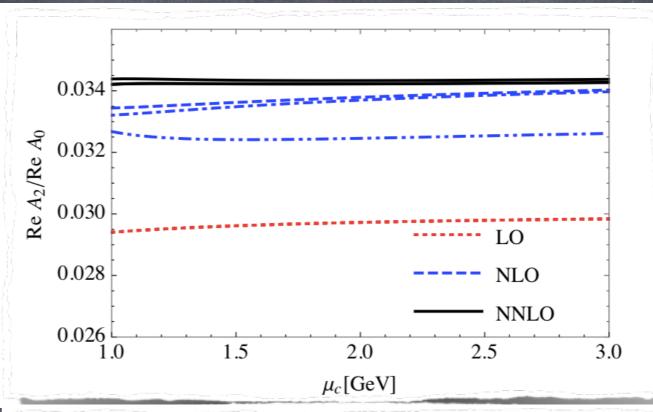
Impact onto Real

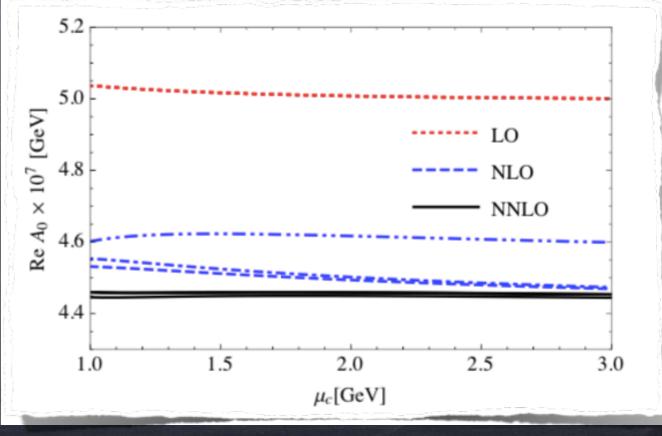
 $ReA_2 = 1.48 \times 10^{-8} GeV$

 $ReA_0 = 33.2 \times 10^{-8} GeV$

Lattice input to ReAO has still 20%/25% stat/sys. uncertainty

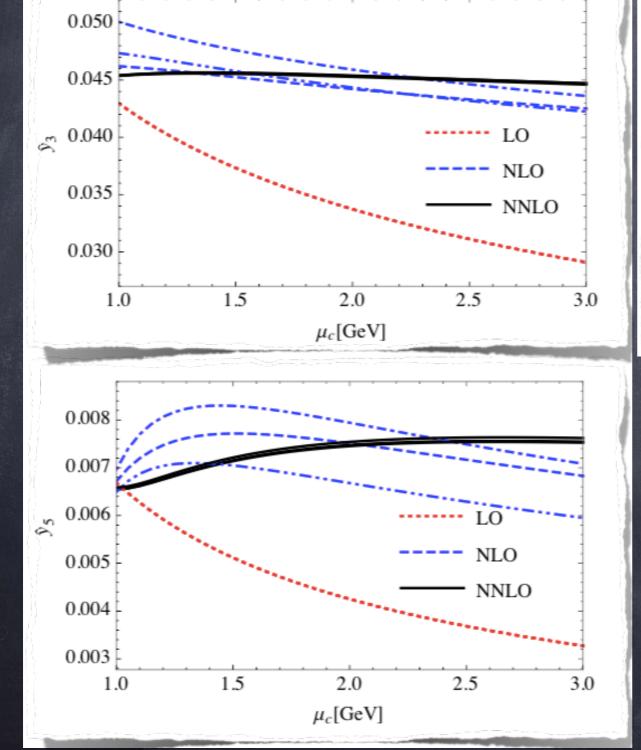


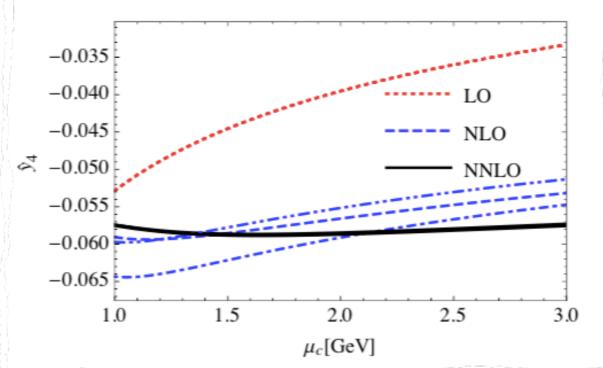


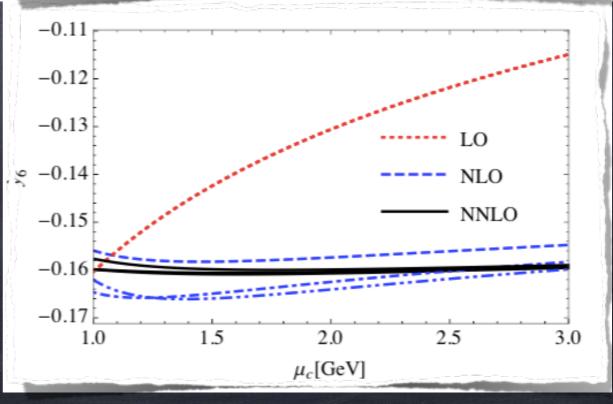


Results at NNLO

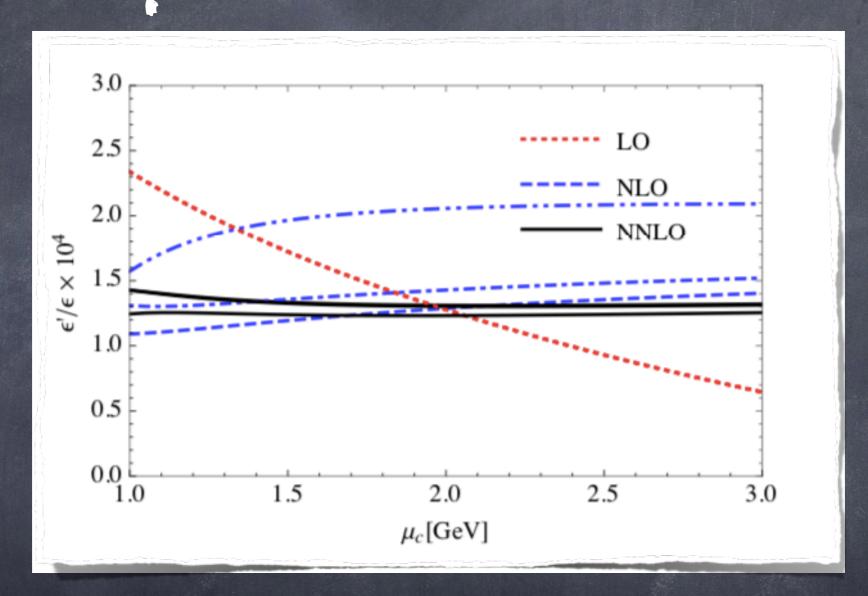
NNLO accuracy of ~2% for the most important coefficient y6.







Impact onto e/e



Uncertainty is significantly reduced by going to NNLO.

Tiny scale variation suggests negligible N3LO QCD effects.

There are still improvements: better as implementation & better incorporation of sub-leading corrections.

Dynamical Charm

No evidence for a failure of perturbation theory at the charm scale.

Non-perturbative Virtual-charm effects



From our computed threshold corrections, we can provide an estimation of the four-flavour matrix elements.

$$(\hat{Q})^{(3)} \hat{C}^{(3)} = \langle \hat{Q} \rangle^{(3)} . \hat{M}^{(34)} . \hat{C}^4 = \langle \hat{Q} \rangle^{(4)} . \hat{C}^{(4)}$$

C(4) Available at NNLO (cc, QCDP) & NLO (EWP)

Phenomenology at infat

The formula for e'/e has to be modified at the 4-flavour theory.

There are two new operators, $Q_1^c \notin Q_2^c$, \notin the penguin operators contain charm quark.

The I=2 amplitude ratio is unchanged in form.

The I=0 ratio depends explicitly on the new operators:

$$\begin{split} \frac{\mathrm{Im} A_{0}}{\mathrm{Re} A_{0}} &= \mathrm{Im} \tau \left[\frac{(2 \ y_{4} - \frac{1}{2} [3y_{9} - y_{10}](1 + 2q_{-}^{c})}{z_{-}(1 + \tilde{q})} - \frac{q_{-}^{c}}{1 + \tilde{q}} \right. \\ &+ \frac{\frac{3}{2} [y_{9} + y_{10}](1 + q_{+}^{c})\tilde{q}}{z_{+}(1 + \tilde{q})} - \frac{q_{+}^{c}\tilde{q}}{1 + \tilde{q}} + \frac{(y_{3} + y_{4} - \frac{1}{2} [y_{9} + y_{10}])\tilde{p}_{3}}{z_{-}(1 + \tilde{q})} \\ &+ \frac{G_{F}}{\sqrt{2}} \frac{V_{ud}V_{us}^{*}}{\mathrm{Re} A_{0}} \left(\langle Q_{6} \rangle_{0} (y_{6} + p_{5}y_{5} + p_{8g}y_{8g}) + \langle Q_{8} \rangle_{0} (y_{8} + p_{70}y_{7} + p_{70\gamma}y_{7\gamma}) \right) \right] \\ \mathbf{39} \end{split}$$

Isospin Breaking effects

The isospin limit is not very good: O(10%) corrections

Pions are not exact I=1 states

#

Electromagnetic effects cannot be neglected

This corrections are introduced via the parameters $\Omega_{\rm eff}$ & a A. The phases $\delta_{0,2}$ are still defined in the isospin limit. Watson's theorem is only valid when isospin is conserved

B. One matches a QCDxQED evolution to a pure QCD lattice calculation

Electromagnetism in Lattice

Complicated, particularly QED effects (IR subtractions, real emission, lattice matching, ...)

A. Do not respect the two-amplitude structure

B. Violate Watson's theorem

Now conceptually understood on the lattice in QED perturbation theory. In practice need to

- A. Define QED expansion of matrix element ratios
- B. Carefully define ξ express observable at $O(\alpha_e)$
- C. Disentangle QED RG evolution from matrix matrix element expansion, for matching short-distance and Lattice

Conclusions & Outlook

e'/e at NLO perturbation theory with RBC-UKQCD matrix elements shows a tension with the data.

Lattice results with improved stat, and syst. errors will be published soon.

New NNLO calculation of the non-EW-penguin part of the weak Hamiltonian removes large part of the perturbative uncertainty in e'/e.

e'/e can be expressed in terms of RGI objects, to achieve a fuller factorisation between perturbative and non-perturbative pieces.

Fullure goals

From a phenomenological perspective, the most important goal is reducing the error on $<Q_{670}$.

If phenomenology is done appropriately, none of the other <0> contribute above 1/4 or below of the current experimental error.

Apart from this, calculation of isospin breaking on the lattice, and interfacing with perturbation theory will be important.

Formalism can be extended to nf=4 dynamical quarks.

EW NNLO including systematic treatment of $O(\alpha_e)$ (as well as m_u =! m_d) about the isospin limit are the next steps on perturbative side

"and now here is my secret, a very simple secret: It is only with the heart that one can see rightly; what is essential is invisible to the eye"

-Le petite prince (Antoine de Saint-Exupéry)

backer

What if RBC-UKQCD results are right?

- a. SM value deviates by almost 30 from experimental world average: (e'/e)sm << (e'/e)exp.
- b. Destructive new-physics effects in e'/e are disfavoured.

 this puzzle requires a NP contribution

 even larger than the SM contribution
- c. The large factor $1/\omega_+$ multiplying ImA2 renders e'/e sensitive to new physics in the $\Delta I=3/2$ transitions.

However, it is difficult to place a large effect into e' without overshooting ex.

Main constraint: ex

The SM contributions to direct and indirect CPV depend on the CKM combination τ as

e'SM & Int and exSM & Int2

In new physics scenarios, with new sources of CPV replace τ with δ

 $e'NP \propto Im\delta$ and $eKNP \propto Im\delta^2$

For super-heavy new physics entering through loops, effects can only be relevant if $|\delta| >> |\tau|$

But ex^{NP} >> exSM in contradiction with the experimental value. Need clever ideas to suppress ex!!

Possible New physics explanations

[Cirigliano et al., '16]

WR coupling

Generic Z'models

[Buras et al., '15]

Chromo-magnetic Operator

[Buras et al., '99]

[Bauer et al., '09]

[Constantinou et al., '14]

SUSY

[Kitahara et al., '16]

[Endo et al., '16]

[Crivellin et al., '17]

L' Macdels

General models with tree-level Z and Z' flavour violating exchanges.

The correlations of e'/e with other flavour observables allow to differentiate between models in which e'/e can be enhanced

Z-scenarios: Enhancement of e'/e, eK, $Br(K_L->\pi^\circ \ V\ V)$ &purple &purple

Z'-scenarios: the size of NP effects \ddagger the correlation between Br(K_L-> π° V V) \ddagger Br(K⁺-> π^{+} V V) depends strongly on whether QCDP or EWP dominate NP contributions to e'/e

MC COUPLING

The enhancement in e'/e originates from right-handed charged-current interactions. (Tree level)

$$\mathcal{L}_{SM} + \frac{g}{\sqrt{2}} \left[\xi_{ij} \ \bar{u}_R^i \gamma^\mu d_R^j \ W_\mu^+ \right] (1 + \frac{h}{v})^2 + \text{h.c.}$$

To assume that Eud and Eus have complex phases.

Right-handed scale of O(102 TeV) to explain the discrepancy.

Correlation with hadronic and atomic electric dipole moments.

Chromo-magnetic

Chromo-magnetic penguins

$$C_{\gamma,g}^{\mathrm{SM}} \sim \frac{\alpha_W(M_W)}{M_W} \frac{m_s}{M_W}$$
 $C_{\gamma,g}^{\mathrm{NP}} \sim \frac{\alpha_s(M_{NP})}{M_{NP}} \delta_{LR}$

can give large corrections to e'/e of form:

$$(\varepsilon'/\varepsilon)_{8g} = 3 B_{8g} \operatorname{Im} \left(C_{8g} - C'_{8g} \right) / (G_F m_K)$$

= 520 $B_{8g} \operatorname{Im} (C_{8g} - C'_{8g}) \operatorname{TeV}$

However, an enhancement of the SM by a factor of order 500 is necessary for a sizeable impact on e'/e

e/e in MSSM

The MSSM has the required ingredients to explain e' without conflict with ex despite $\delta >> \tau$. [Kitahara et al., '16]

Mechanism

a. Enhancement of ImA2 due to strong isospin-breaking contributions. "Trojan penguin" [Grossman et al., '99]

(coupling differently to up and down quarks)

b. Suppression of the K-K mixing amplitude thanks to the Majorana nature of the gluinos [Crivellin et al., '10]

This is possible with squark and gluino masses in the range 3-7 TeV, far above the reach of LHC.