Rethinking the QCD axion

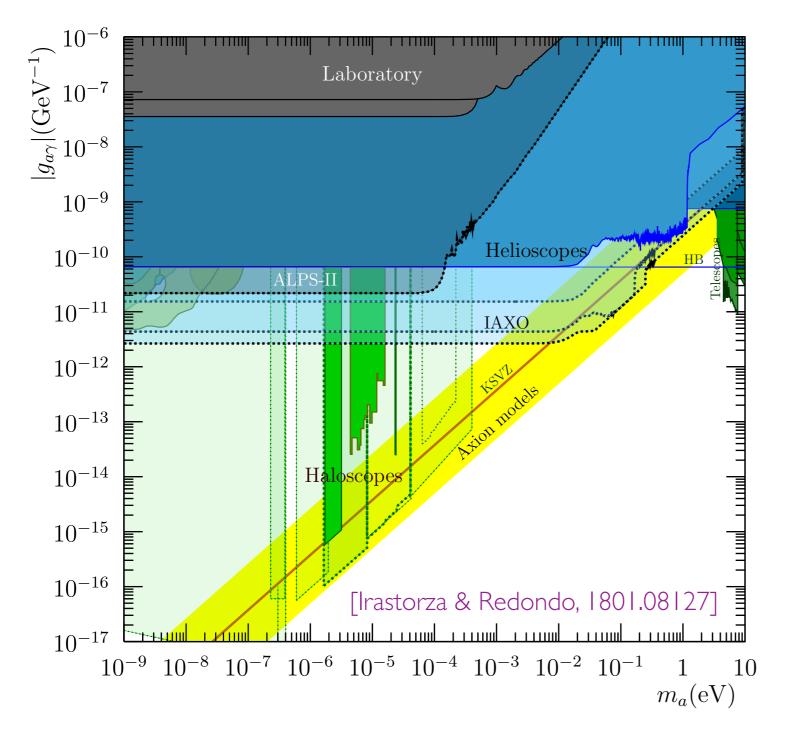
DESY-HU Theorie-Seminar - 15.11.18

Luca Di Luzio





In 10 years from now ?



A great opportunity to discover the QCD axion !

★ Time <u>now</u> to get prepared and rethink the QCD axion



- I. Strong CP problem
- 2. QCD axion
- 3. Current limits and search strategies
- 4. Beyond standard axion scenarios

Based on: LDL, Mescia, Nardi 1610.07593 (PRL) + 1705.05370 (PRD) LDL, Mescia, Nardi, Panci, Ziegler 1712.04940 (PRL) + work in progress

• CP violation in QCD

$$\mathcal{L}_{\text{QCD}} = \sum_{q} \overline{q} \left(i \not{\!\!D} - m_{q} e^{i\theta_{q}} \right) q - \frac{1}{4} G^{\mu\nu}_{a} G^{a}_{\mu\nu} - \theta \frac{\alpha_{s}}{8\pi} G^{\mu\nu}_{a} \tilde{G}^{a}_{\mu\nu} \qquad \left(\tilde{G}^{a}_{\mu\nu} = \frac{1}{2} \epsilon_{\mu\nu\rho\sigma} G^{a,\rho\sigma} \right)$$

• CP violation in QCD

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- GGtilde is a total derivative (<u>no effects in PT</u>)
- QCD vacuum structure

[Belavin, Polyakov, Schwarz, Tyupkin PLB59 (1975), 't Hooft PRL37 + PRD14 (1976), Callan, Dashen, Gross, PLB63 (1976), ...]

$$Z = \int \delta G \, e^{-\frac{1}{4} \int G G - i\theta \frac{\alpha_s}{8\pi} \int G \tilde{G}} \sim e^{-\frac{8\pi}{g_s^2}} e^{i\theta} \xrightarrow{\mathrm{I} + \mathrm{AI}} e^{-\frac{8\pi}{g_s^2}} \cos\theta$$

- dominated by "large instantons" of size $\rho \sim 1/\Lambda_{QCD}$ (semi-classical approx. breaks down)

need chiral Lagrangian for quantitative statements

• CP violation in QCD

$$\mathcal{L}_{\text{QCD}} = \sum_{q} \overline{q} \left(i D - m_{q} e^{i\theta_{q}} \right) q - \frac{1}{4} G^{\mu\nu}_{a} G^{a}_{\mu\nu} - \theta \frac{\alpha_{s}}{8\pi} G^{\mu\nu}_{a} \tilde{G}^{a}_{\mu\nu}$$

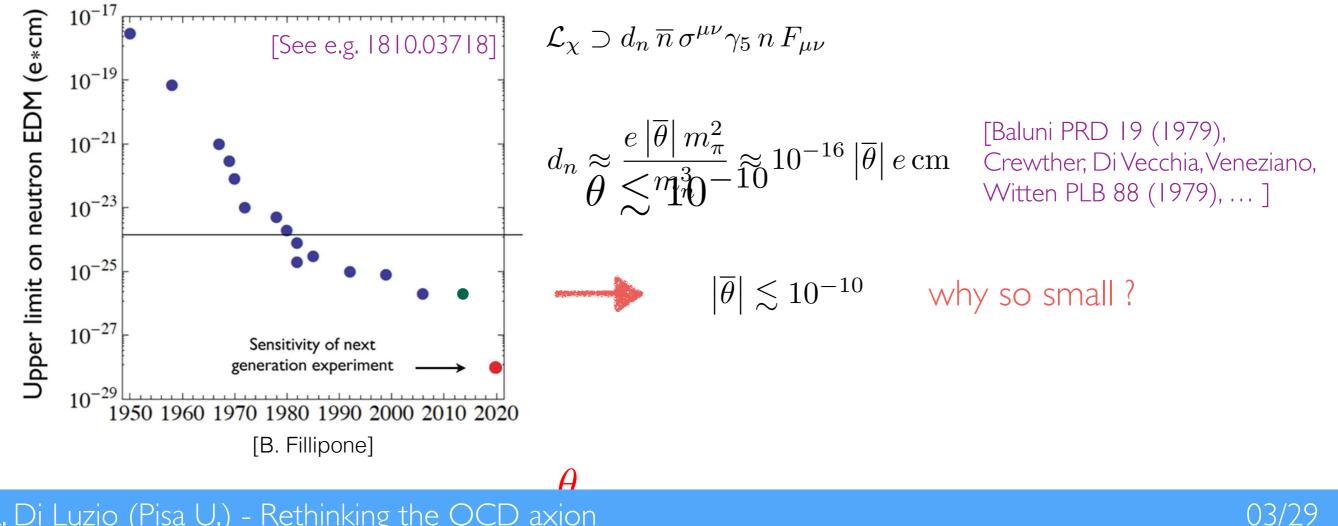
• Non-trivial role of quark fields: under a chiral transformation

 $= \theta - \arg \det (Y_u Y_d)$ (generalization to an arbitrary chiral transf. in the EW theory)

CP violation in QCD

$$\mathcal{L}_{\text{QCD}} = \sum_{q} \overline{q} \left(i D - m_{q} e^{i \theta_{q}} \right) q - \frac{1}{4} G^{\mu\nu}_{a} G^{a}_{\mu\nu} - \theta \frac{\alpha_{s}}{8\pi} G^{\mu\nu}_{a} \tilde{G}^{a}_{\mu\nu}$$

• Non-zero neutron $EDM_n \approx 3.6 \times 10^{-16} \theta \ e \ cm$



• Strong CP: <u>qualitatively different</u> from other small value problems of the SM

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I. theta is radiatively stable (unlike $m_H^2 \ll \Lambda_{
m UV}^2$)

[Ellis, Gaillard NPB 150 (1979), Khriplovich, Vainshtein NPB 414 (1994)]

$$\overline{\theta} \sim \frac{1}{(4\pi)^{14}} g^{\prime 2} \left[Y^2(u_R) - Y^2(d_R) \right] J_{\text{CKM}} \log \Lambda_{\text{UV}}$$

$$\downarrow$$

$$J_{\text{CKM}} = \text{Im Det} \left[Y_U Y_U^{\dagger}, Y_D Y_D^{\dagger} \right] \approx 10^{-29}$$

- expect to arise at 7-loops



Fig. 9. Generic topology of a class of divergent *CP* violating 14th-order diagrams in the Kobayashi-Maskawa model [21,22].

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nuclear physics and BBN practically unaffected for $\overline{ heta} \lesssim 10^{-2}$ [Ubaldi, 0811.1599]

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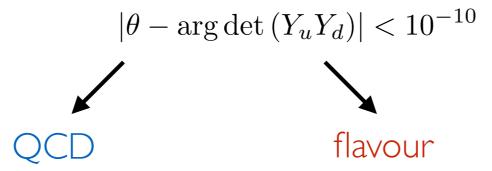
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[Ubaldi, 0811.1599]

• More than a small value problem ?



(imagine a theory of flavour generating Yukawas: would expect O(1) phases like CKM)

- Do we really understand QCD vacuum structure ?
 - e.g. confinement might screen theta term [Polyakov...]
 - attempts in this directions often fail to solve eta' problem !

 $m_{\eta'} \approx 958 \,\mathrm{MeV}$ $m_{\eta'} < \sqrt{3}m_{\pi}$ [Weinberg sum-rule for pNGB]

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- Spontaneous CP (or P) violation

[Nelson PLB 136 (1983), PLB 143 (1984)] [Barr PRD 30 (1984)]

- $\overline{\theta} = 0$ in the CP limit
- need to generate CKM (and CP violation for BAU) without inducing a too large $\overline{\theta}$
- non-trivial model building + no clear experimental signature

- Do we really understand QCD vacuum structure ?
- A massless quark would make the theta term unphysical (excluded at 20 σ by Lattice)
- Spontaneous CP (or P) violation
- PQ mechanism

[Peccei, Quinn PRL 38 (1977), PRD 16 (1997)]

- assume a global $U(1)_{PQ}$: i) QCD anomalous and ii) spontaneously broken

- axion: pNGB of $U(1)_{PQ}$ breaking

[Weinberg PRL 40 (1978), Wilczek PRL 40 (1978)]

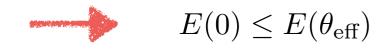
$$a(x) \to a(x) + \delta \alpha f_a$$

θ -dependence of QCD vacuum

• Ground state energy in Euclidean V₄

[Vafa, Witten PRL 53 (1984)]

$$e^{-V_4 E(\theta_{\text{eff}})} = \int \mathcal{D}\varphi \, e^{-S_0 + i\theta_{\text{eff}}\{G\tilde{G}\}} = \left| \int \mathcal{D}\varphi \, e^{-S_0 + i\theta_{\text{eff}}\{G\tilde{G}\}} \right| \le \int \mathcal{D}\varphi \, \left| e^{-S_0 + i\theta_{\text{eff}}\{G\tilde{G}\}} \right| = e^{-V_4 E(0)}$$



• theta term dynamically relaxed to zero on the axion ground state $\langle a(x) \rangle = -\overline{\theta} f_a$

- aGGtilde not a total derivative (effects in PT)

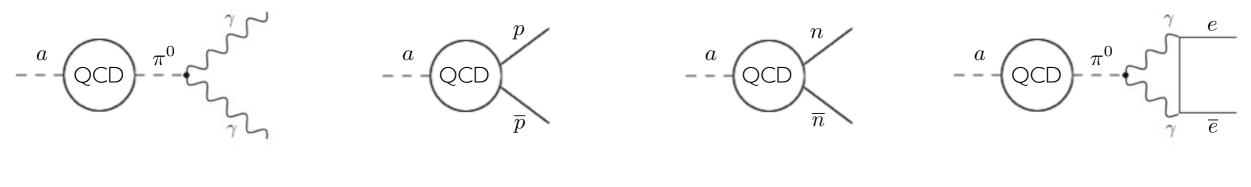
Axion properties [EFT]

- Consequences of $\frac{a}{f_a} \frac{\alpha_s}{8\pi} G^{\mu\nu}_a \tilde{G}^a_{\mu\nu}$
 - generates axion mass

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- generates "model independent" axion couplings to photons, nucleons, electrons, ...



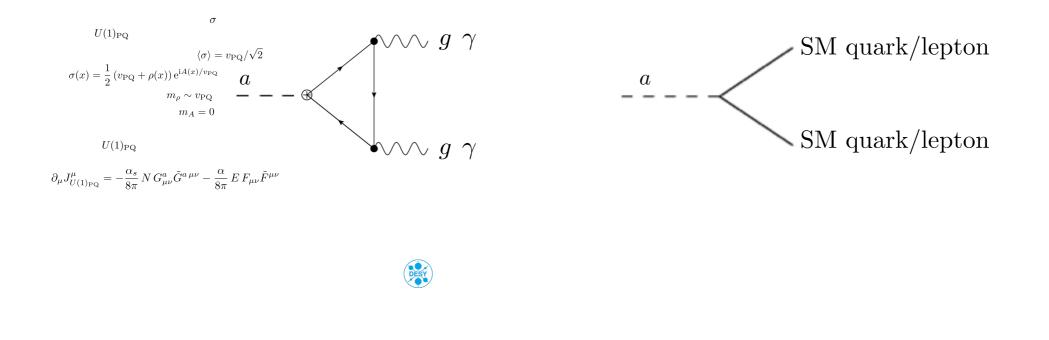
 $C_{\gamma} = -1.92(4)$ $C_p = -0.47(3)$ $C_n = -0.02(3)$ $C_e \simeq 0$

$$\frac{\alpha}{8\pi} \frac{C_{\gamma}}{f_a} a F_{\mu\nu} \tilde{F}^{\mu\nu} \qquad C_{\Psi} m_{\Psi} \frac{a}{f_a} [i\overline{\Psi}\gamma_5 \Psi] \qquad \left(\Psi = p, n, e\right) \qquad \begin{bmatrix} \text{From NLO Chiral Lagrangian,} \\ \text{Grilli di Cortona et al., 1511.02867} \end{bmatrix}$$

Axion properties [EFT]

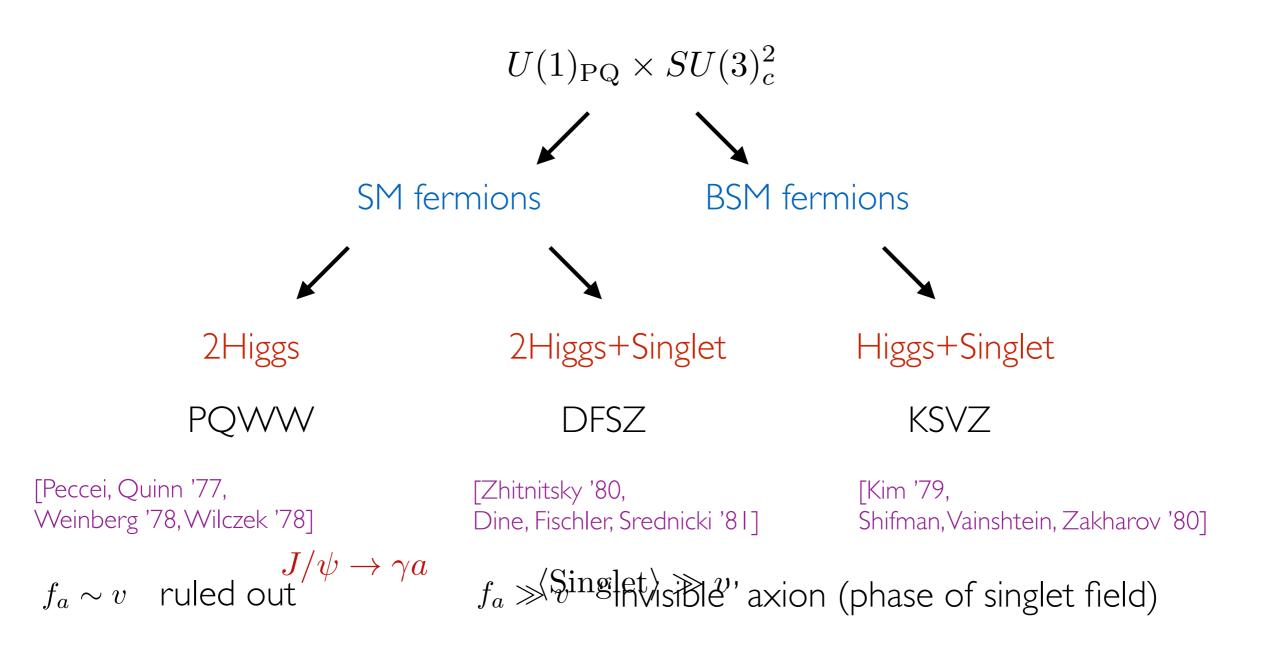
- Consequences of $\frac{a}{f_a} \frac{\alpha_s}{8\pi} G^{\mu\nu}_a \tilde{G}^a_{\mu\nu}$
 - EFT breaks down at energies of order fa

UV completion can still affect low-energy axion properties !



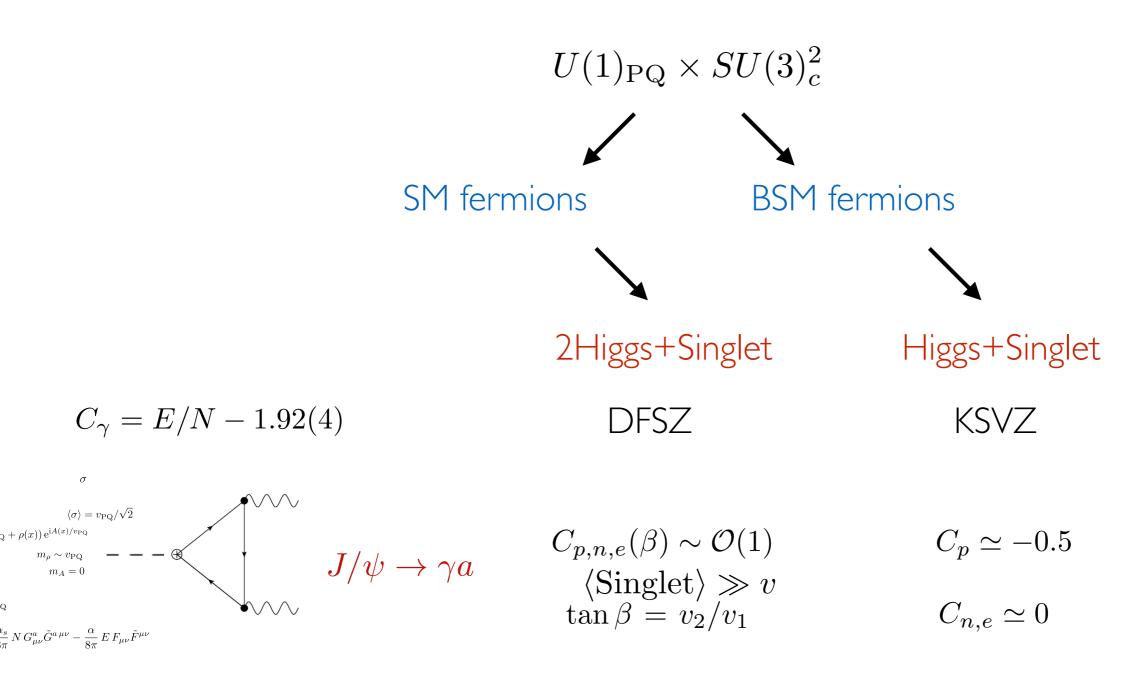
Axion models [UV completion]

• anomalous PQ breaking (fermion sector) + spontaneous PQ breaking (scalar sector)



Axion models [UV completion]

• anomalous PQ breaking (fermion sector) + spontaneous PQ breaking (scalar sector)



Heavy particle vs. light scalar field

(WIMPs)

(Axions)

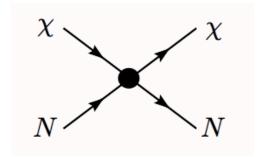
search for single particle scattering

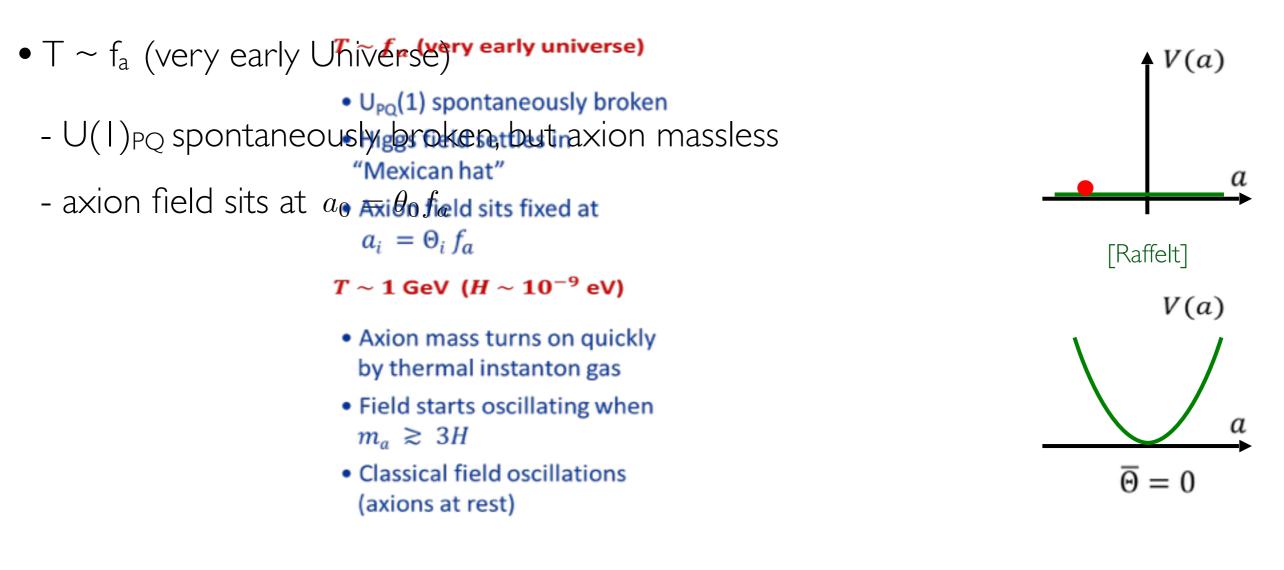
search for coherent effects of the entire field, not particle scattering

(e.o.m. in a FRW background)

$$\ddot{a} + 3H\dot{a} + m_a^2(T)f_a \sin\left(\frac{a}{f_a}\right) = 0$$

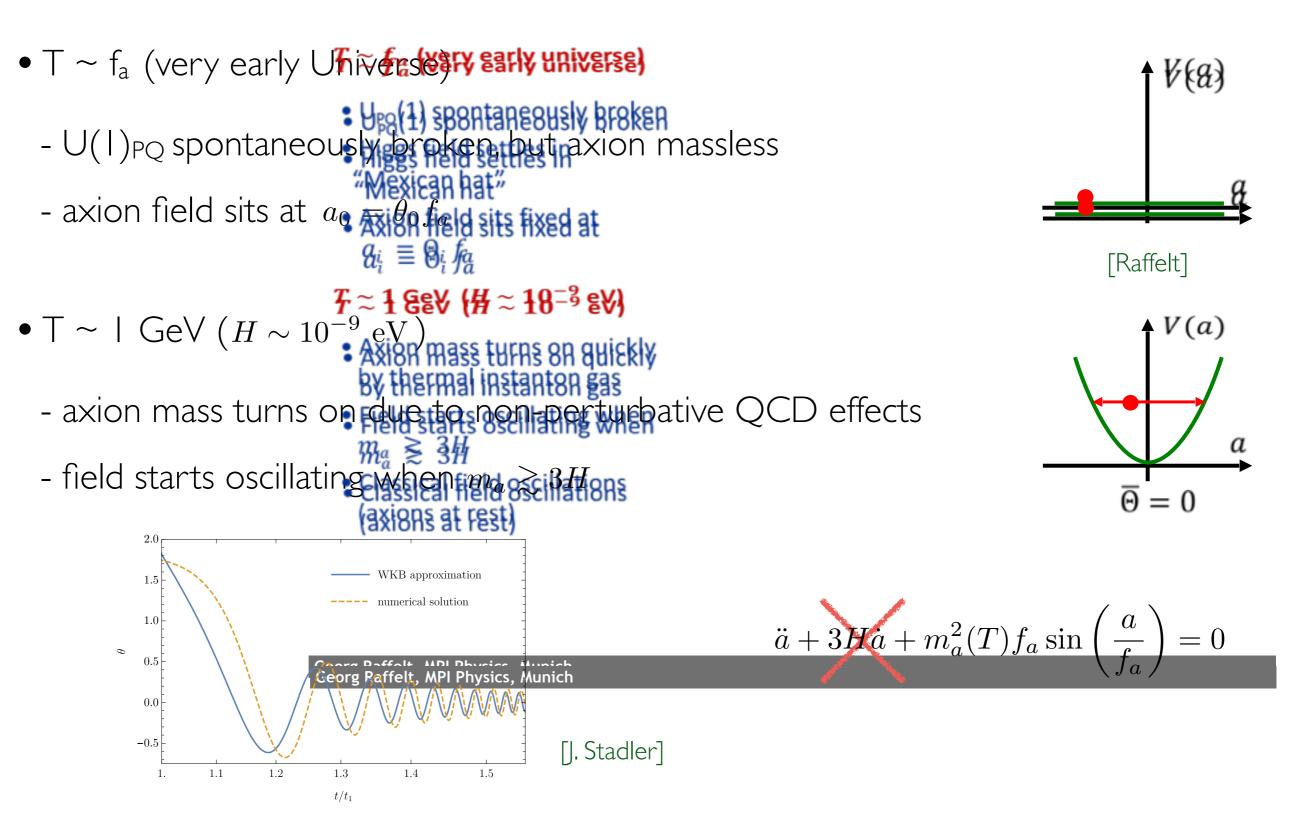


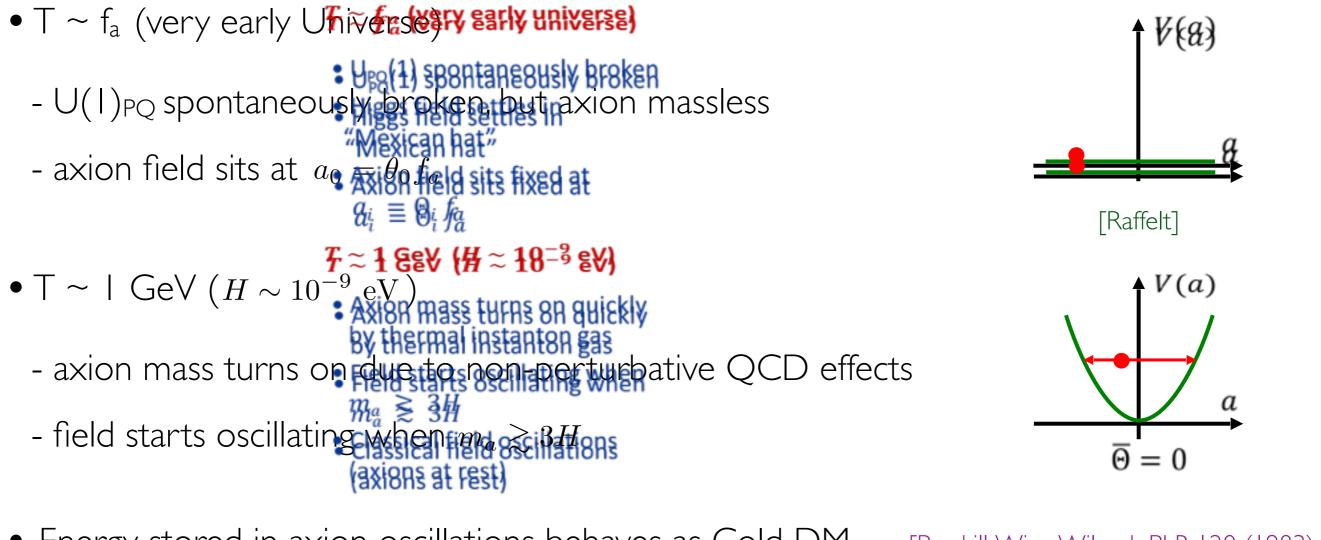




$$\ddot{a} + 3H\dot{a} + m_a^2(T)f_a \sin\left(\frac{a}{f_a}\right) = 0$$

Georg Raffelt, MPI Physics, Munich





Energy stored in axion oscillations behaves as Cold DM

[Preskill, Wise, Wilczek PLB 120 (1983), Abott, Sikivie PLB 120 (1983), Dine, Fischler PLB 120 (1983)]

Georg Raffelt, MPI Physics, Munich

 $a(t) = a_0 \cos\left(m_a t\right)$

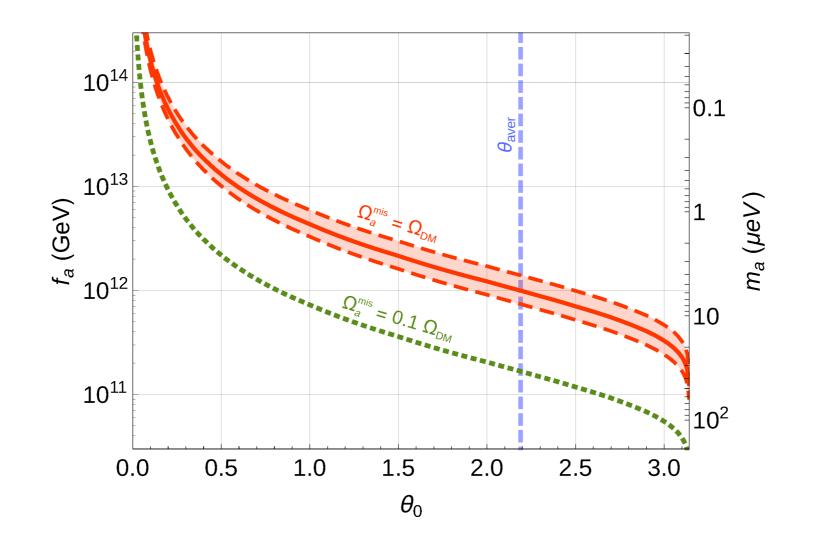


depends on the initial condition: misalignment mechanism

Relic abundance

• From lattice QCD simulations: $f_a \lesssim 10^{11 \div 12}$ GeV for $\theta_0 = \mathcal{O}(1)$

[Bonati et al. 1512.06746, Petreczky et al. 1606.03145, Borsanyi et al. 1606.07494, ...]



Relic abundance

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post-inflationary PQ breaking	pre-inflationary PQ breaking
$f_a < \max\{H_I, T_R\}$	$f_a > \max\{H_I, T_R\}$
θ_0 averaged over several Universe patches	θ_0 arbitrary
$\langle \theta_0 angle = \pi/\sqrt{3}$ $\Omega_a^{\rm mis} < \Omega_{\rm DM}$ $f_a \lesssim 5 \cdot 10^{11} { m GeV}$	misalignment contribution unique, but depends on initial conditions
	$f_a \gg 10^{12} { m ~GeV}$ only for $\theta_0 \ll 1$
+ contribution from topological defects	
[See e.g. Ringwald, Saikawa 1512.06436 Gorghetto, Hardy, Villadoro 1806.04677]	

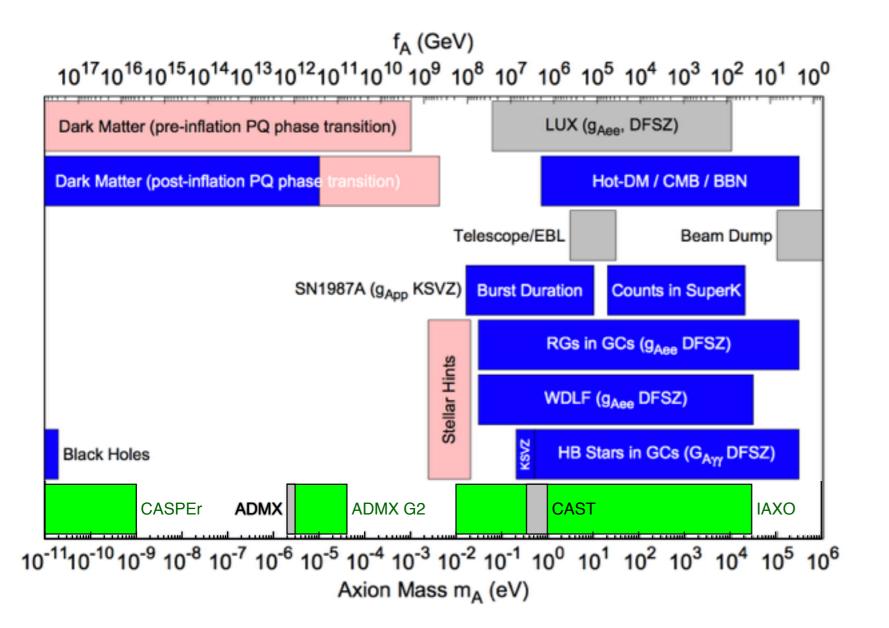
Astro bounds

- Stars as powerful sources of <u>light</u> and <u>weakly coupled</u> particles [see e.g. Raffelt, hep-ph/0611350]
 - light: $m_a \lesssim 10 T_{\star}$ (e.g. typical interior temperature of the Sun ~ 1 keV)
 - weakly coupled (otherwise we would have already seen them in labs)

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 - weakly coupled (otherwise we would have already seen them in labs)
- constraints from "energy loss", relevant when more interacting than neutrinos

neutrino interactions (d=6 op.)axion interactions (d=5 op.)
$$G_F m_e^2 \simeq 10^{-12}$$
 $\frac{m_e}{f_a} \simeq 10^{-12} \left(\frac{10^8 \text{ GeV}}{f_a}\right)$ \blacktriangleright axions are a perfect target ! $m_a \sim \Lambda_{\rm QCD}^2/f_a \simeq 0.1 \text{ eV} \left(\frac{10^8 \text{ GeV}}{f_a}\right)$



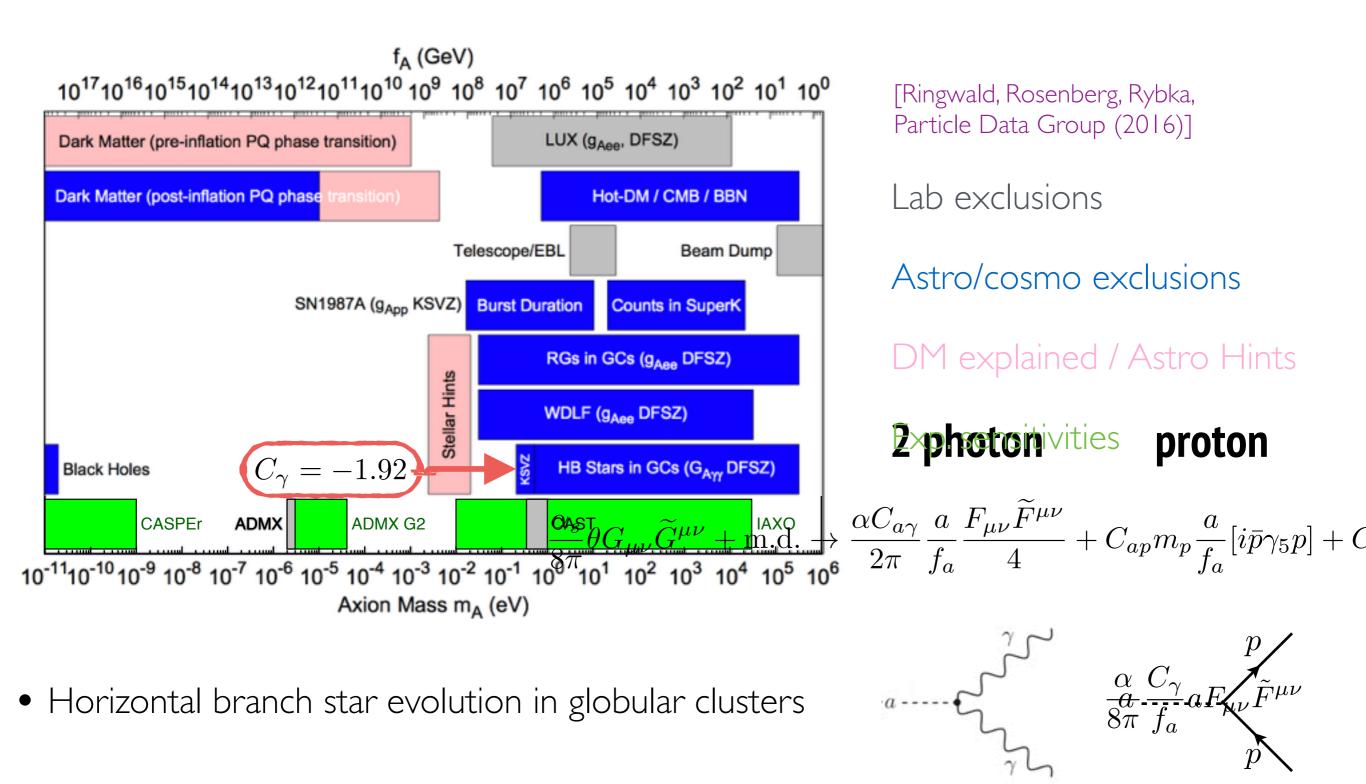
[Ringwald, Rosenberg, Rybka, Particle Data Group (2016)]

Lab exclusions

Astro/cosmo exclusions

DM explained / Astro Hints

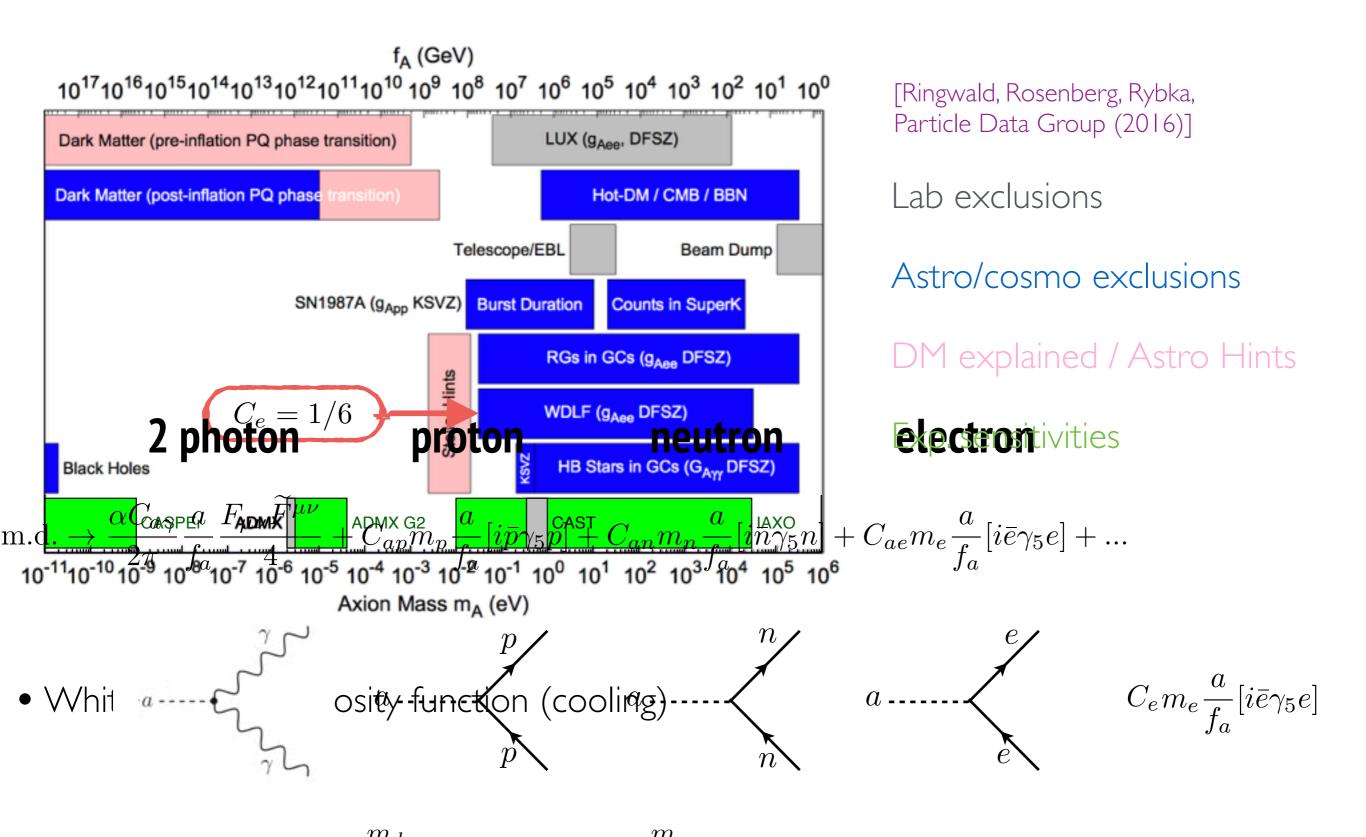
Exp. sensitivities

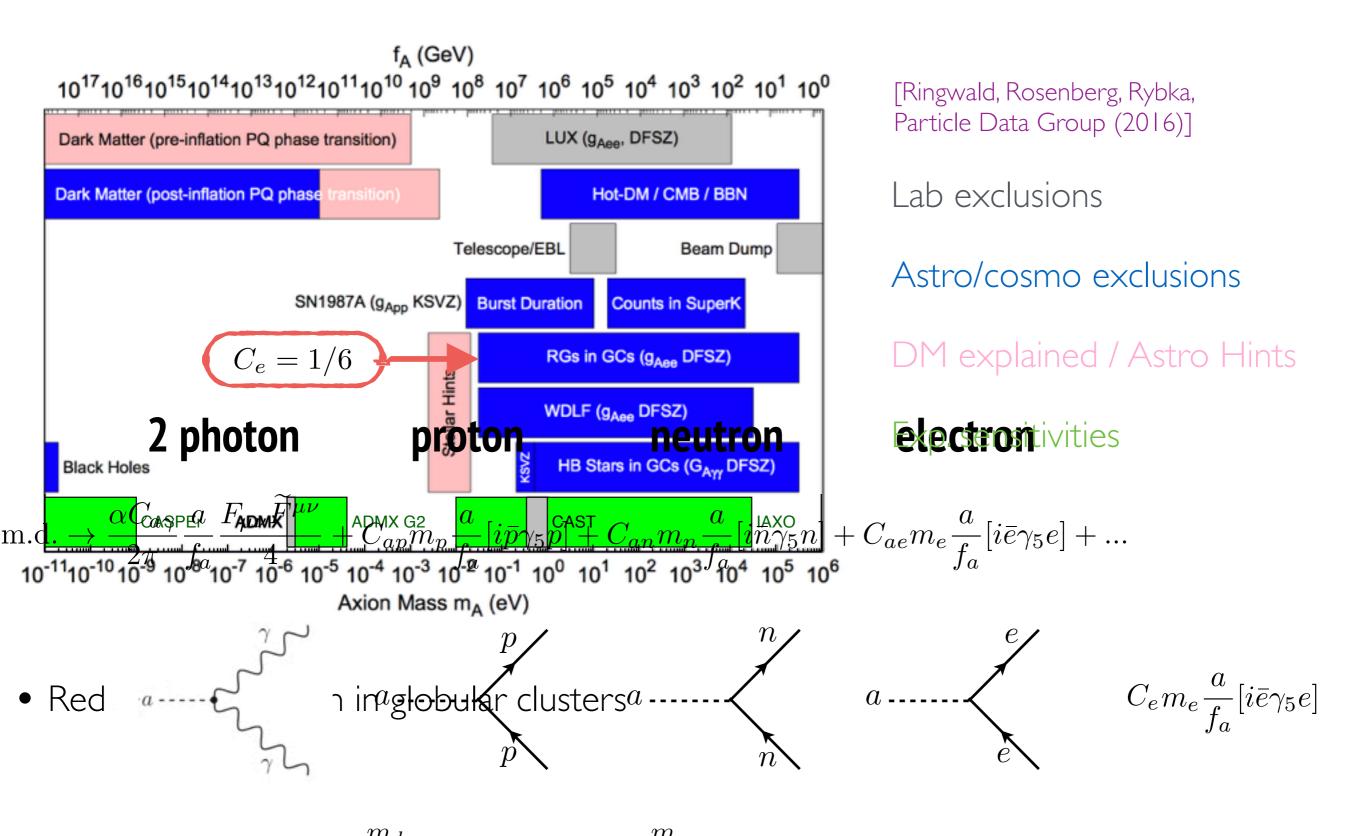


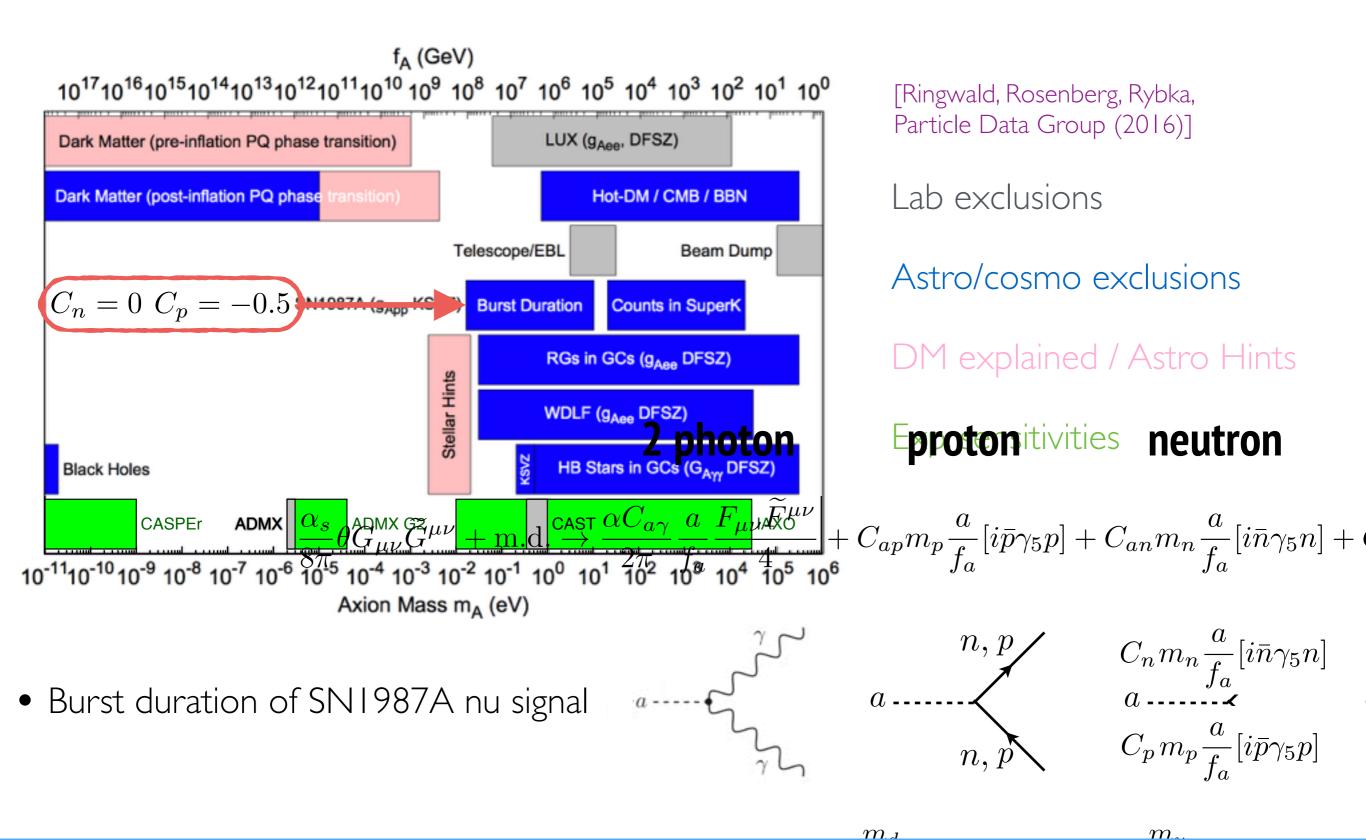
L. Di Luzio (Pisa U.) - Rethinking the QCD axion

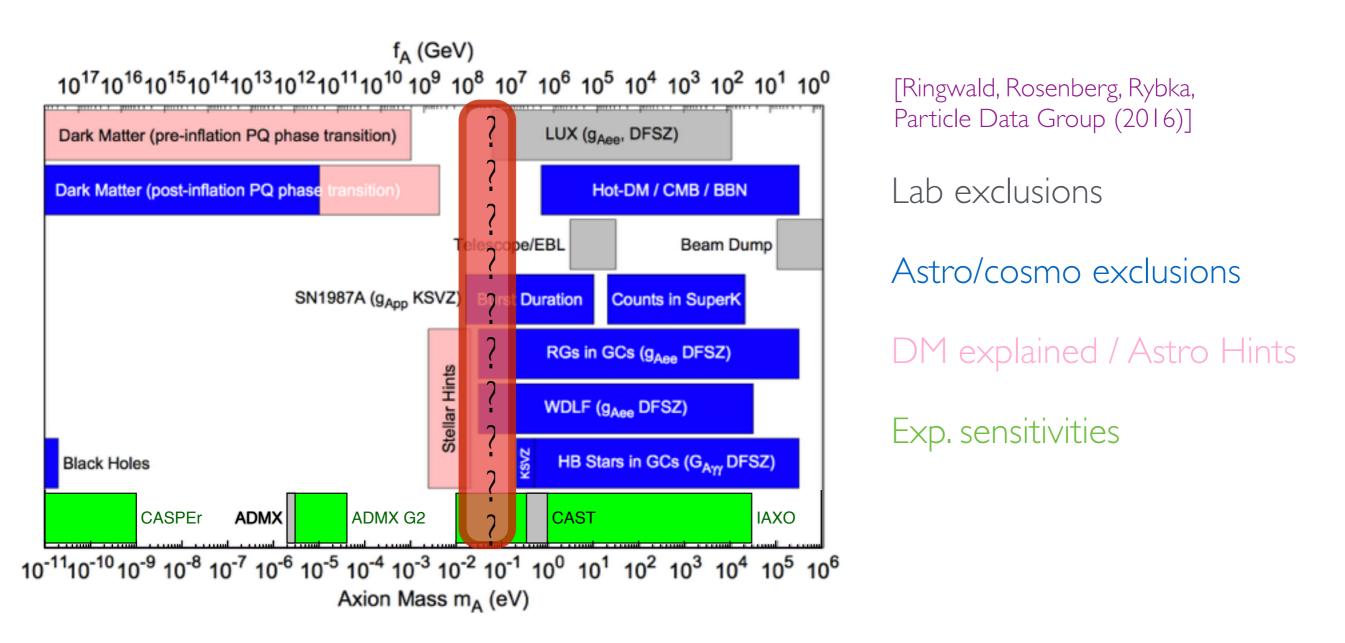
12/29

 m_{-1}









• Bound on axion mass is of <u>practical</u> convenience, but misses model dependence !

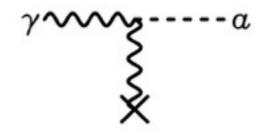
Search strategies

• Most laboratory search techniques are sensitive to $g_{a\gamma\gamma}$

Primakoff effect: axion-photon transition in external static E or B field

$$\mathcal{L}_{a\gamma\gamma} = -\frac{1}{4} g_{a\gamma\gamma} \, a \, F \cdot \tilde{F} = g_{a\gamma\gamma} \, a \, \mathbf{E} \cdot \mathbf{B}$$

- Light Shining through Walls
- Haloscopes (axion Dark Matter)
- Helioscopes (axions from the Sun)



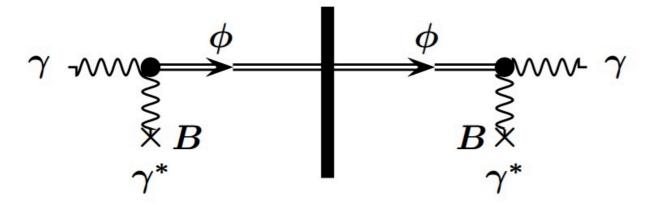
Georg Raffelt, MPI Physics, Munich

[See e.g. Redondo, Ringwald hep-ph/10113741]

[Sikivie PRL 51 (1983)]

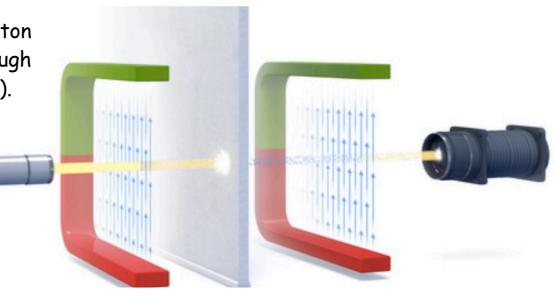
Light Shining through Walls (LSW)

- Any Light Particle Search (DESY): ALPS-1 (2007-2010) and ALPS-II (2013-...)



Schematic view of axion (or ALP) production through photon conversion in a magnetic field (left), subsequent travel through a wall, and final detection through photon regeneration (right).

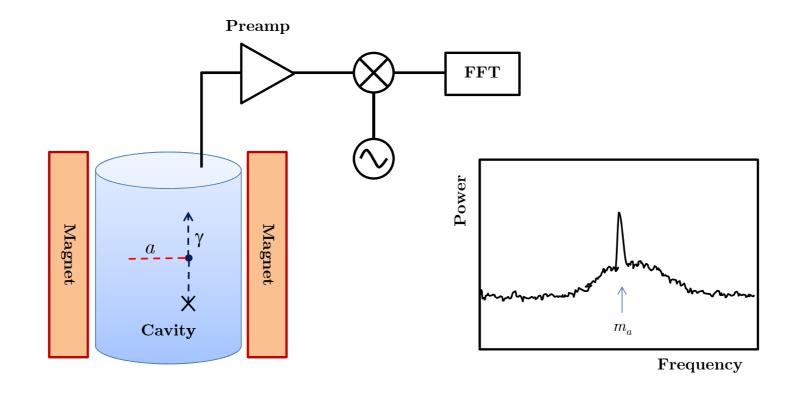
Artist view of a light shining through a wall experiment



- LSW experiments pay a $g_{a\gamma\gamma}^4$ suppression

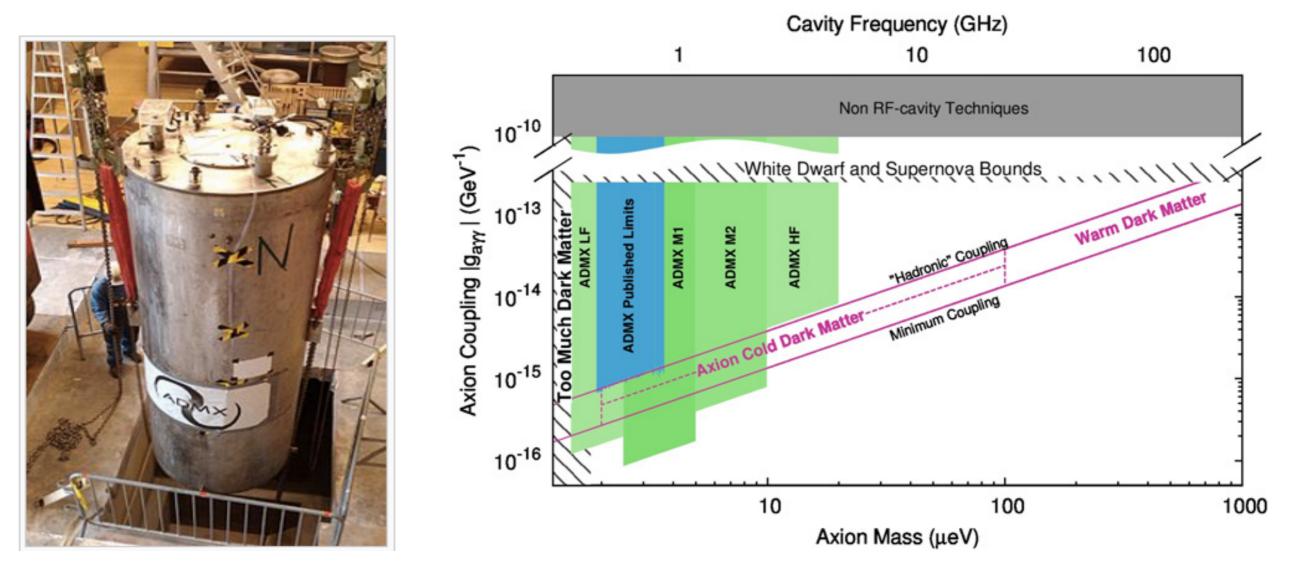


- Look for DM axions with a microwave resonant cavity
 - power of axions converting into photons in an EM cavity $P_a = Cg_{a\gamma\gamma}^2 V B_0^2 \frac{\rho_a}{m_a} Q_{\text{eff}}$
 - resonance condition: need to tune the frequency of the EM cavity on the axion mass



Haloscopes

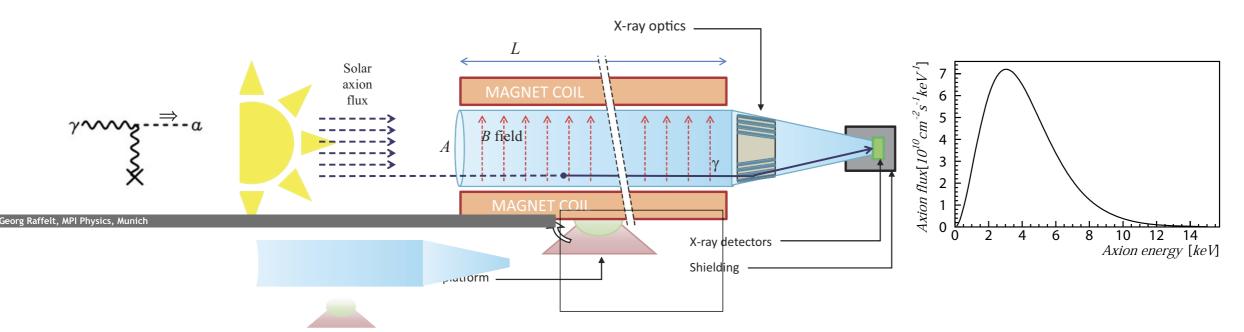
- Look for DM axions with a microwave resonant cavity
- Axion Dark Matter eXperiment (ADMX) (U. of Washington)



[ADMX Collaboration, Phys. Dark Univ. 4 (2014)]

Helioscopes

• The Sun is a potential axion source



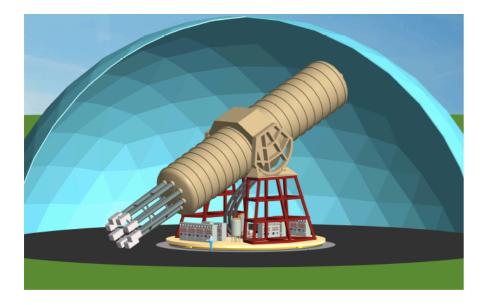
- macroscopic B-field can provide a coherent axion-photon (x-ray) conversion rate over a big volume

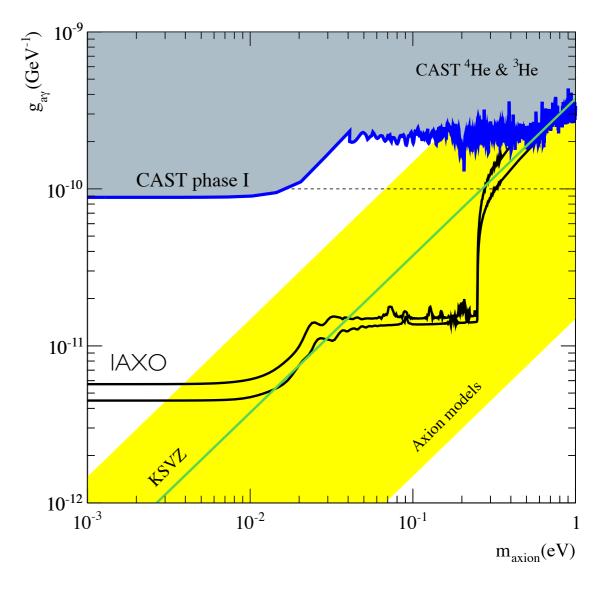
Helioscopes

- The Sun is a potential axion source
- CERN Axion Solar Telescope (CAST)



- International AXion Observatory (IAXO)





[IAXO "Letter of intent", CERN-SPSC-2013-022]



PHYSICAL REVIEW X 4, 021030 (2014)

Proposal for a Cosmic Axion Spin Precession Experiment (CASPEr) Dmitry Budker,^{1,5} Peter W. Graham,² Micah Ledbetter,³ Surjeet Rajendran,² and Alexander O. Sushkov⁴

PRL 113, 161801 (2014)PHYSICAL REVIEW LETTERSweek ending
17 OCTOBER 2014

Resonantly Detecting Axion-Mediated Forces with Nuclear Magnetic Resonance

Asimina Arvanitaki¹ and Andrew A. Geraci^{2,*}

PRL 117, 141801 (2016)

PHYSICAL REVIEW LETTERS

week ending 30 SEPTEMBER 2016

week ending

3 MARCH 2017

Broadband and Resonant Approaches to Axion Dark Matter Detection

Yonatan Kahn,^{1,*} Benjamin R. Safdi,^{2,†} and Jesse Thaler^{2,‡}

PRL 118, 091801 (2017)

PHYSICAL REVIEW LETTERS

Dielectric Haloscopes: A New Way to Detect Axion Dark Matter

Allen Caldwell,¹ Gia Dvali,^{1,2,3} Béla Majorovits,¹ Alexander Millar,¹ Georg Raffelt,¹ Javier Redondo,^{1,4} Olaf Reimann,¹ Frank Simon,¹ and Frank Steffen¹ (MADMAX Working Group) Searching for galactic axions through magnetized media: The QUAX proposal

R. Barbieri^{a,b}, C. Braggio^c, G. Carugno^c, C.S. Gallo^c, A. Lombardi^d, A. Ortolan^d, R. Pengo^d, G. Ruoso^{d,*}, C.C. Speake^e

PHYSICAL REVIEW D 91, 084011 (2015)

Discovering the QCD axion with black holes and gravitational waves

Asimina Arvanitaki^{*}

Perimeter Institute for Theoretical Physics, Waterloo, Ontario N2L 2Y5, Canada

Masha Baryakhtar[†] and Xinlu Huang[‡] Stanford Institute for Theoretical Physics, Department of Physics, Stanford University, Stanford, California 94305, USA (Received 16 December 2014; published 7 April 2015)

PHYSICAL REVIEW D 91, 011701(R) (2015)

Search for dark matter axions with the Orpheus experiment

Gray Rybka,^{*} Andrew Wagner,[†] Kunal Patel, Robert Percival, and Katleiah Ramos University of Washington, Seattle, Washington 98195, USA

Aryeh Brill

Yale University, New Haven, Connecticut 06520, USA (Received 16 November 2014; published 21 January 2015)

CULTASK, The Coldest Axion Experiment at CAPP/IBS/KAIST in Korea

Woohyun Chung*

Center for Axion and Precision Physics Research, Institute for Basic Science (IBS), Republic of Korea

The Axion Rush

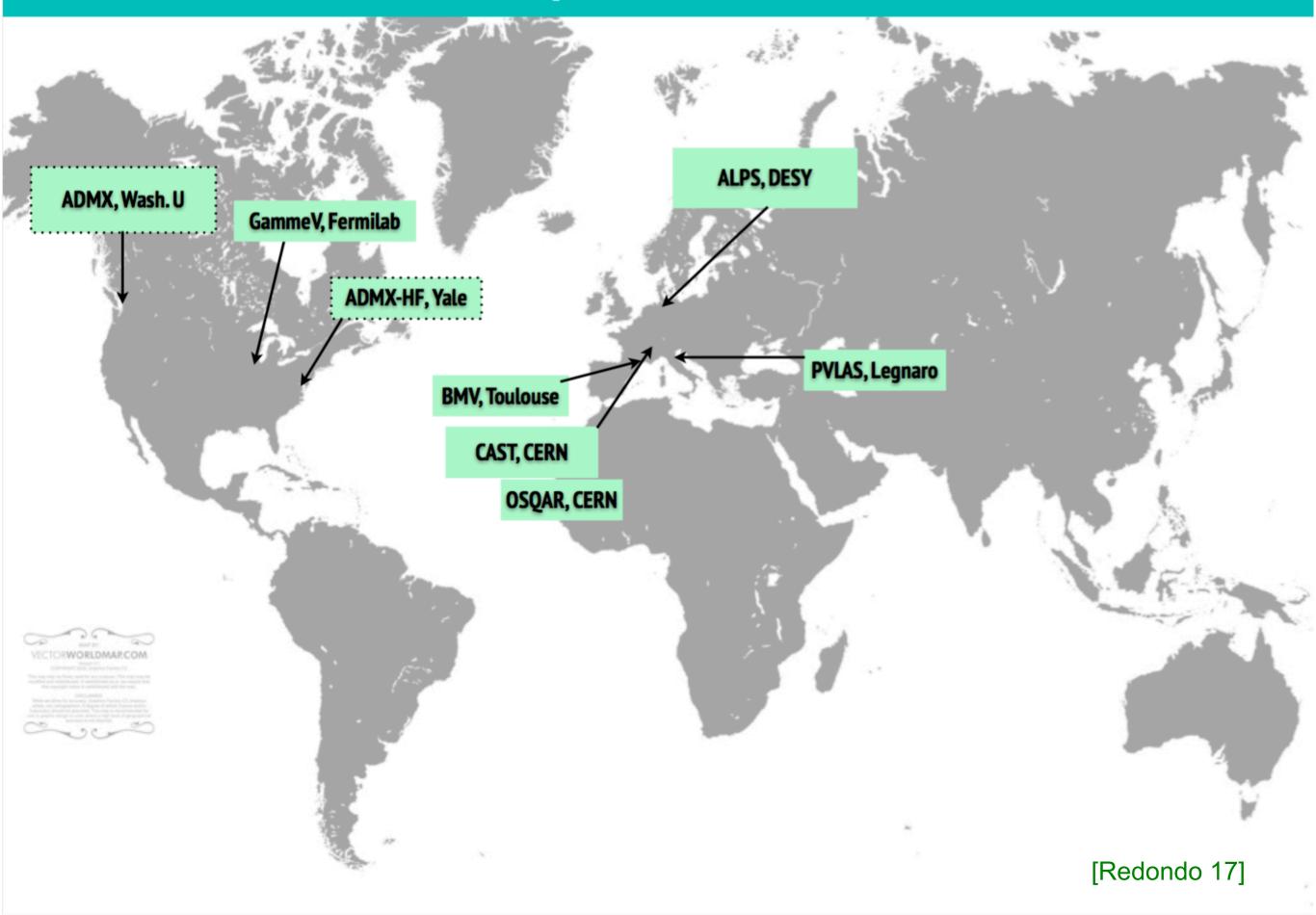


. Di Luzio (Pisa U.) - Rethinking the QCD axion

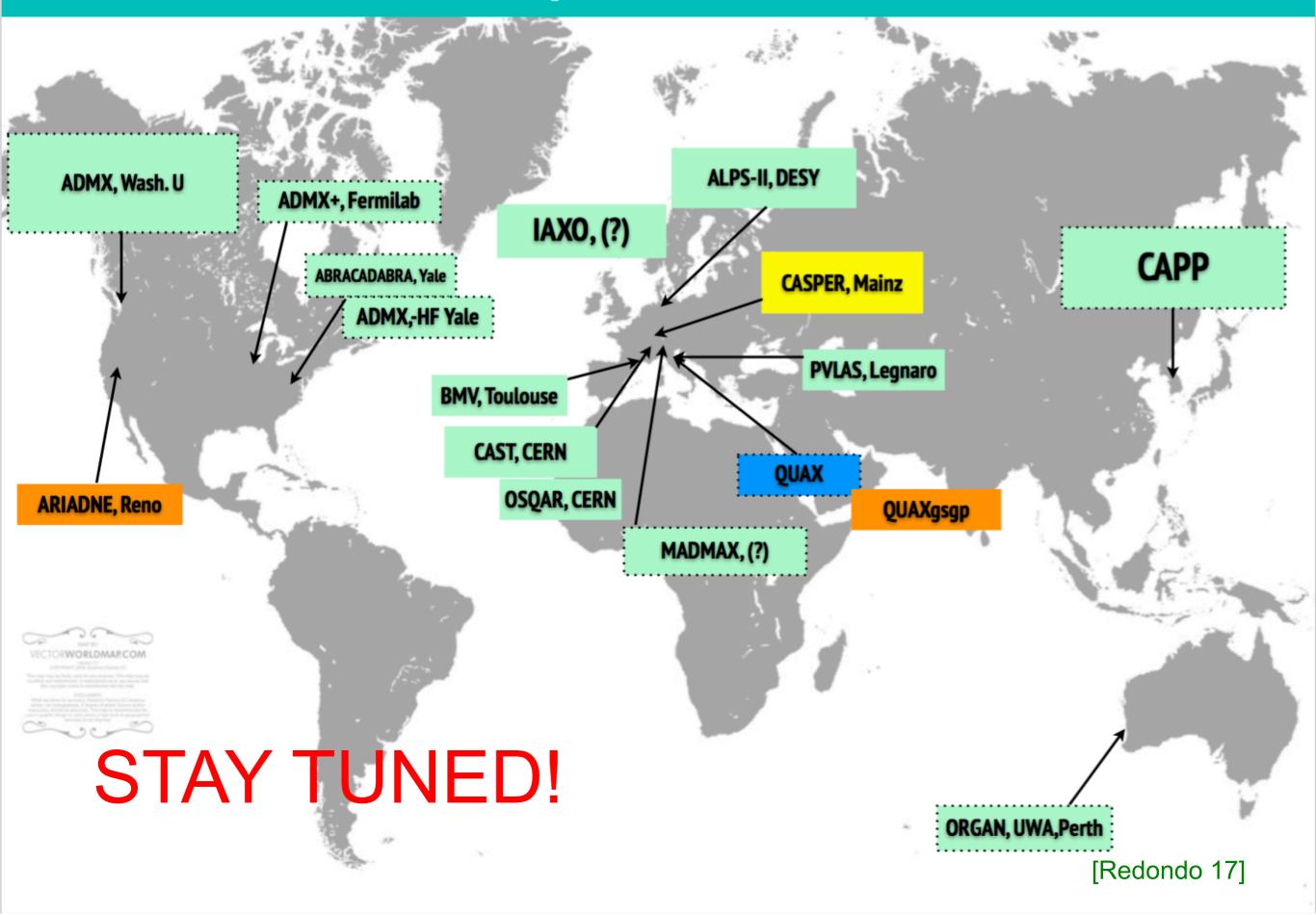
 $g_{a\gamma\gamma}$

 g_{aee}

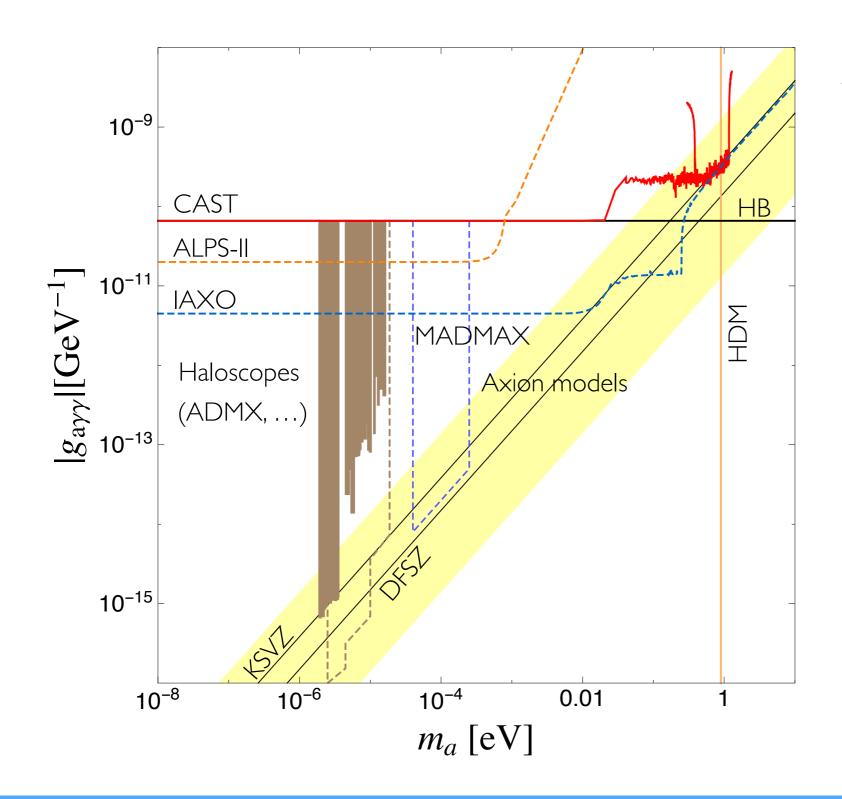
Lab experiments 2011



Lab experiments 2017



Need to know where to search



$$g_{a\gamma\gamma} = \frac{m_a}{\mathrm{eV}} \frac{2.0}{10^{10} \mathrm{GeV}} \left(\frac{E}{N} - 1.92\right)$$

E/N anomaly coefficients, depend on <u>UV completion</u>

$$|E/N - 1.92| \in [0.07, 7]$$

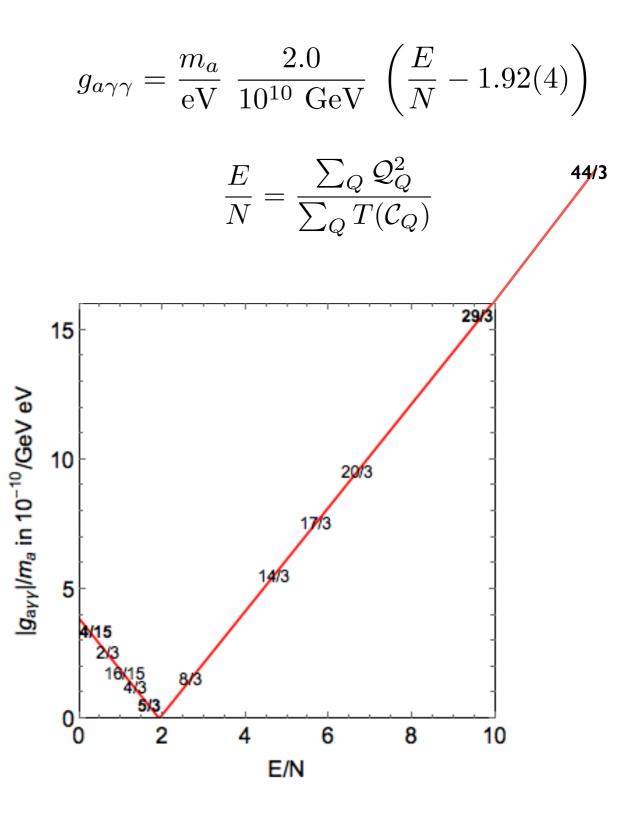
[Particle Data Group (since end of 90's). Chosen to include some representative KSVZ/DFSZ models e.g. from:

- Kaplan, NPB 260 (1985),
- Cheng, Geng, Ni, PRD 52 (1995),
- Kim, PRD 58 (1998)]

Pheno	preferred	KSVZ	fermions
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R_Q	\mathcal{O}_{Qq}	$\Lambda_{\rm Landau}^{\rm 2-loop}[{\rm GeV}]$	E/N
(3, 1, -1/3)	$\overline{Q}_L d_R$	$9.3 \cdot 10^{38}(g_1)$	2/3
(3, 1, 2/3)	$\overline{Q}_L u_R$	$5.4 \cdot 10^{34}(g_1)$	8/3
(3, 2, 1/6)	$\overline{Q}_R q_L$	$6.5 \cdot 10^{39}(g_1)$	5/3
(3, 2, -5/6)	$\overline{Q}_L d_R H^\dagger$	$4.3 \cdot 10^{27}(g_1)$	17/3
(3, 2, 7/6)	$\overline{Q}_L u_R H$	$5.6 \cdot 10^{22}(g_1)$	29/3
(3, 3, -1/3)	$\overline{Q}_R q_L H^\dagger$	$5.1 \cdot 10^{30}(g_2)$	14/3
(3, 3, 2/3)	$\overline{Q}_R q_L H$	$6.6 \cdot 10^{27}(g_2)$	20/3
(3, 3, -4/3)	$\overline{Q}_L d_R H^{\dagger 2}$	$3.5 \cdot 10^{18}(g_1)$	44/3
$(\overline{6}, 1, -1/3)$	$\overline{Q}_L \sigma_{\mu\nu} d_R G^{\mu\nu}$	$2.3 \cdot 10^{37}(g_1)$	4/15
$(\overline{6}, 1, 2/3)$	$\overline{Q}_L \sigma_{\mu\nu} u_R G^{\mu\nu}$	$5.1 \cdot 10^{30}(g_1)$	16/15
$(\overline{6}, 2, 1/6)$	$\overline{Q}_R \sigma_{\mu u} q_L G^{\mu u}$	$7.3 \cdot 10^{38}(g_1)$	2/3
(8, 1, -1)	$\overline{Q}_L \sigma_{\mu\nu} e_R G^{\mu\nu}$	$7.6 \cdot 10^{22}(g_1)$	8/3
(8, 2, -1/2)	$\overline{Q}_R \sigma_{\mu\nu} \ell_L G^{\mu\nu}$	$6.7 \cdot 10^{27}(g_1)$	4/3
(15, 1, -1/3)	$\overline{Q}_L \sigma_{\mu\nu} d_R G^{\mu\nu}$	$8.3 \cdot 10^{21}(g_3)$	1/6
(15, 1, 2/3)	$\overline{Q}_L \sigma_{\mu\nu} u_R G^{\mu\nu}$	$7.6 \cdot 10^{21}(g_3)$	2/3





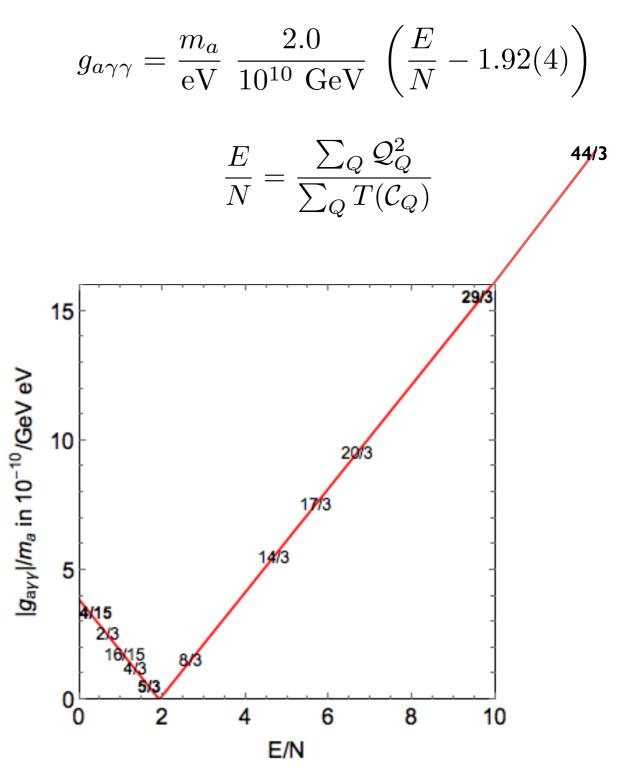
Pheno	preferred	KSVZ	fermions

R_Q	\mathcal{O}_{Qq}	$\Lambda_{\rm Landau}^{\rm 2-loop} [{\rm GeV}]$	E/N
(3, 1, -1/3)	$\overline{Q}_L d_R$	$9.3 \cdot 10^{38}(g_1)$	2/3
(3, 1, 2/3)	$\overline{Q}_L u_R$	$5.4 \cdot 10^{34}(g_1)$	8/3
(3, 2, 1/6)	$\overline{Q}_R q_L$	$6.5 \cdot 10^{39}(g_1)$	5/3
(3, 2, -5/6)	$\overline{Q}_L d_R H^\dagger$	$4.3 \cdot 10^{27}(g_1)$	17/3
(3, 2, 7/6)	$\overline{Q}_L u_R H$	$5.6 \cdot 10^{22}(g_1)$	29/3
(3, 3, -1/3)	$\overline{Q}_R q_L H^\dagger$	$5.1 \cdot 10^{30}(g_2)$	14/3
(3, 3, 2/3)	$\overline{Q}_R q_L H$	$6.6 \cdot 10^{27}(g_2)$	20/3
(3, 3, -4/3)	$\overline{Q}_L d_R H^{\dagger 2}$	$3.5 \cdot 10^{18}(g_1)$	44/3
(3, 3, -4/3) $(\overline{6}, 1, -1/3)$	$\frac{\overline{Q}_L d_R H^{\dagger 2}}{\overline{Q}_L \sigma_{\mu\nu} d_R G^{\mu\nu}}$	$\frac{3.5 \cdot 10^{18} (g_1)}{2.3 \cdot 10^{37} (g_1)}$	44/3 4/15
$(\overline{6}, 1, -1/3)$	$\overline{Q}_L \sigma_{\mu\nu} d_R G^{\mu\nu}$	$2.3 \cdot 10^{37}(g_1)$	4/15
$(\overline{6}, 1, -1/3)$ $(\overline{6}, 1, 2/3)$	$\overline{Q}_L \sigma_{\mu\nu} d_R G^{\mu\nu}$ $\overline{Q}_L \sigma_{\mu\nu} u_R G^{\mu\nu}$	$2.3 \cdot 10^{37}(g_1)$ $5.1 \cdot 10^{30}(g_1)$	4/15 16/15
$(\overline{6}, 1, -1/3) (\overline{6}, 1, 2/3) (\overline{6}, 2, 1/6)$	$\overline{Q}_{L}\sigma_{\mu\nu}d_{R}G^{\mu\nu}$ $\overline{Q}_{L}\sigma_{\mu\nu}u_{R}G^{\mu\nu}$ $\overline{Q}_{R}\sigma_{\mu\nu}q_{L}G^{\mu\nu}$	$2.3 \cdot 10^{37}(g_1)$ $5.1 \cdot 10^{30}(g_1)$ $7.3 \cdot 10^{38}(g_1)$	4/15 16/15 2/3
$(\overline{6}, 1, -1/3)$ $(\overline{6}, 1, 2/3)$ $(\overline{6}, 2, 1/6)$ $(8, 1, -1)$	$\overline{Q}_{L}\sigma_{\mu\nu}d_{R}G^{\mu\nu}$ $\overline{Q}_{L}\sigma_{\mu\nu}u_{R}G^{\mu\nu}$ $\overline{Q}_{R}\sigma_{\mu\nu}q_{L}G^{\mu\nu}$ $\overline{Q}_{L}\sigma_{\mu\nu}e_{R}G^{\mu\nu}$	$2.3 \cdot 10^{37}(g_1)$ $5.1 \cdot 10^{30}(g_1)$ $7.3 \cdot 10^{38}(g_1)$ $7.6 \cdot 10^{22}(g_1)$	4/15 16/15 2/3 8/3

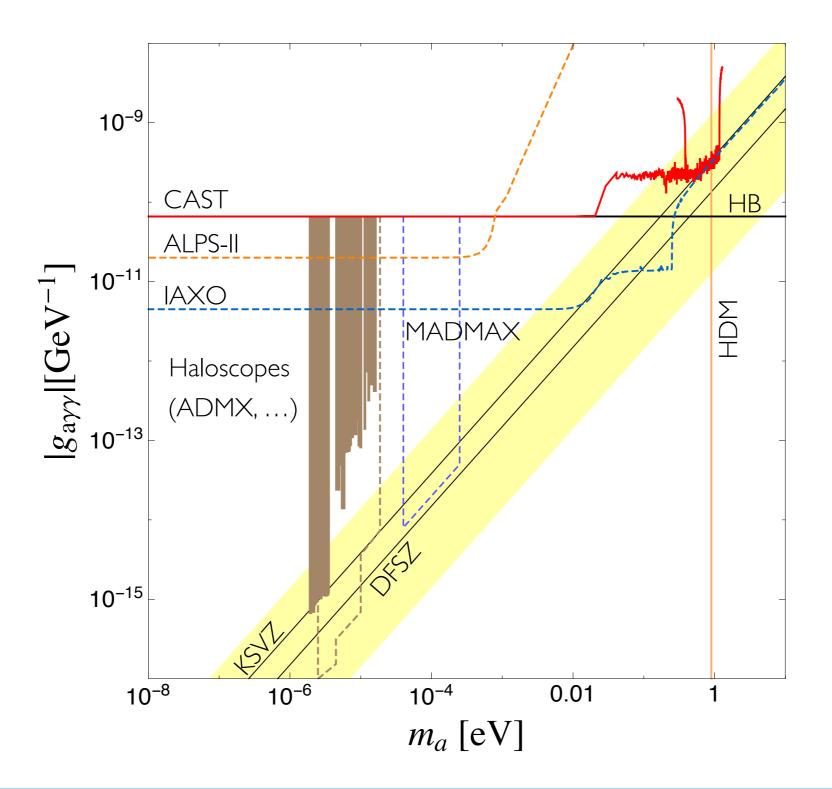
 R_Q^w

 R_Q^s

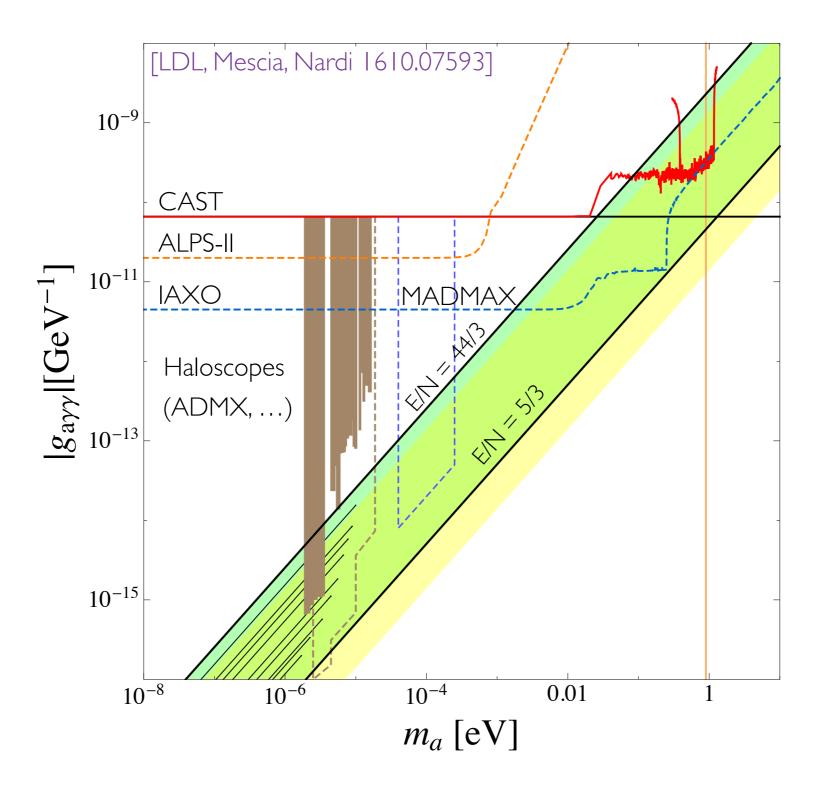




Redefining the axion window



Redefining the axion window



More Q's

• Combined anomaly factor

$$R_Q^1 + R_Q^2 + \dots$$
 $\frac{E_c}{N_c} = \frac{E_1 + E_2 + \dots}{N_1 + N_2 + \dots}$

• Strongest coupling (compatible with LP criterium)

 $(3, 3, -4/3) \oplus (3, 3, -1/3) \oplus (\overline{6}, 1, -1/3)$ $E_c/N_c = 170/3$

• <u>Complete decoupling</u> within theoretical error possible as well:

$$\begin{array}{c} (3,3,-1/3) \oplus (6,1,-1/3) \\ (\overline{6},1,2/3) \oplus (8,1,-1) \\ (3,2,-5/6) \oplus (8,2,-1/2) \end{array} \right\} \quad E_c/N_c = (23/12,64/33,41/21) \approx (1.92,1.94,1.95)$$

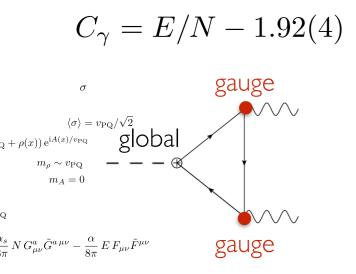
$$g_{a\gamma\gamma} = \frac{m_a}{\text{eV}} \frac{2.0}{10^{10} \text{ GeV}} \left(\frac{E_c}{N_c} - 1.92(4)\right)$$

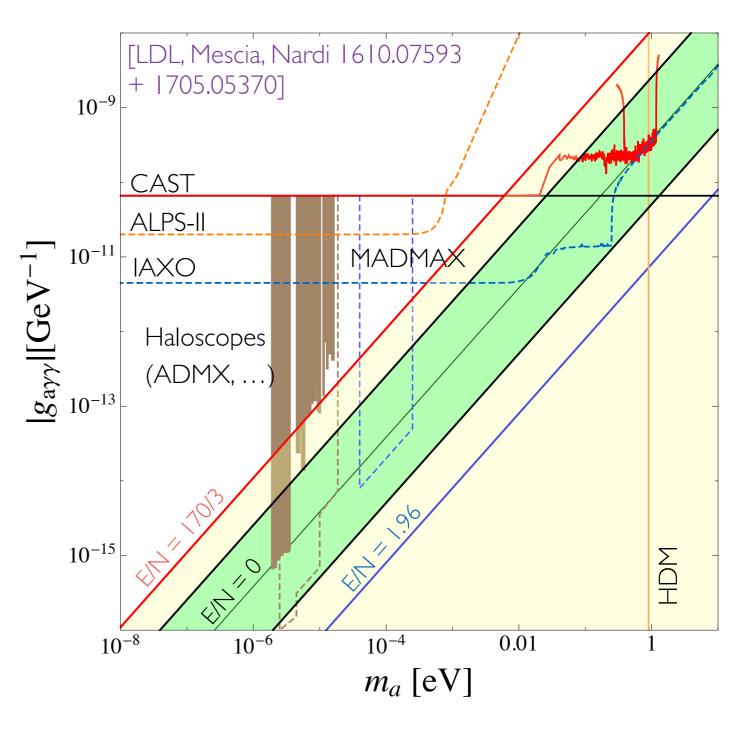
about photophobia: "such a cancellation is immoral, but not unnatural"

[D. B. Kaplan, (1985)]

Axion-photon summary

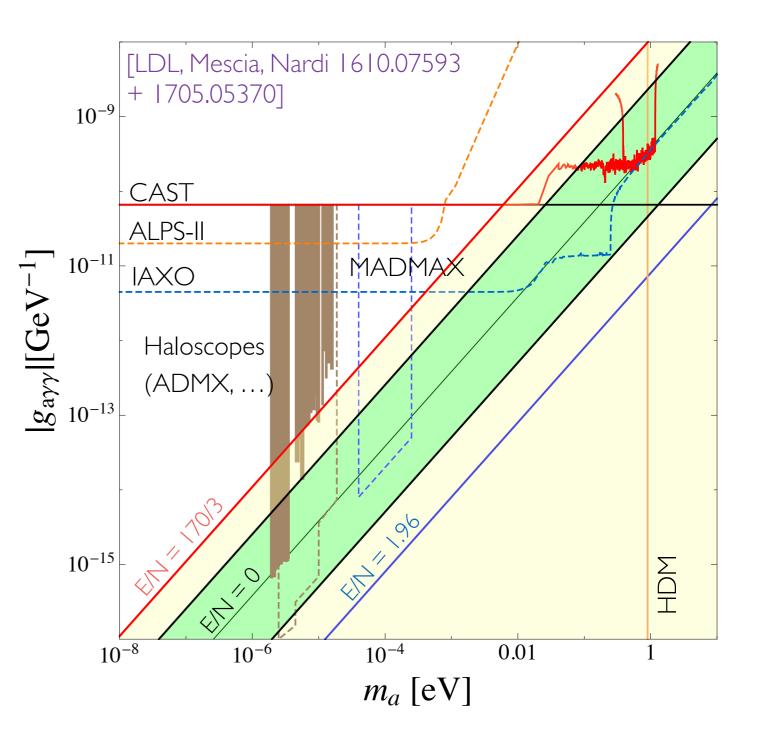
- Red line set by perturbativity [KSVZ] (going much above requires exotic constructions [more in backup slides])
- Blue line corresponds to a 2% 'tuning in theory space'





Axion-photon summary

- Red line set by perturbativity [KSVZ] (going much above requires exotic constructions [more in backup slides])
- Blue line corresponds to a 2% 'tuning in theory space'
- Messages for exp.'s :
- I. The QCD axion might already be in the reach of your experiment !
- 2. Don't stop at E/N = 0 (go deeper if you can)



Astrophobia

- Is it possible to decouple the axion both from nucleons and electrons ?
 - nucleophobia + electrophobia = astrophobia
- Why interested in such constructions ? [LDL, Mescia, Nardi, Panci, Ziegler 1712.04940]
 - I. is it possible at all ?
 - 2. would allow to relax the upper bound on axion mass by ~ 1 order of magnitude
 - 3. would improve visibility at IAXO (axion-photon)
 - 4. would improve fit to stellar cooling anomalies (axion-electron) [Giannotti et al. 1708.02111]
 - 5. unexpected connection with flavour

Astrophobia

- Is it possible to decouple the axion both from nucleons and electrons ?
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 - 5. unexpected connection with flavour

*conceptually easy (e.g. couple the electron to 3rd Higgs uncharged under PQ)

Conditions for nucleophobia

• Axion-nucleon couplings [Kaplan NPB 260 (1985), Srednicki NPB 260 (1985), Georgi, Kaplan, Randall PLB 169 (1986), ..., Grilli di Cortona et al. 1511.02867] v $\mathcal{L}_{q} = \frac{\partial_{\mu} a}{2 f_{c}} c_{q} \overline{q} \gamma^{\mu} \gamma_{5} q \qquad q = (u, d, s, \ldots)$ npEFT-1: quarks and gluons (in the basis where c_q contains aGGtilde contrib.) π e $\mathcal{L}_N = \frac{\partial_\mu a}{2f_a} C_N \overline{N} S^\mu N \qquad N = (p, n)$ aEFT-II: non-relativistic nucleons

Conditions for nucleophobia

• Axion-nucleon couplings

[Kaplan NPB 260 (1985), Srednicki NPB 260 (1985), Georgi, Kaplan, Randall PLB 169 (1986), ..., Grilli di Cortona et al. 1511.02867]

$$f_{a}$$

$$v$$

$$\mathcal{L}_{q} = \frac{\partial_{\mu}a}{2f_{a}}c_{q} \bar{q}\gamma^{\mu}\gamma_{5}q$$

$$n$$

$$p$$

$$\pi$$

$$e$$

$$\mathcal{L}_{N} = \frac{\partial_{\mu}a}{2f_{a}}C_{N}\overline{N}S^{\mu}N$$

$$\langle p|\mathcal{L}_q|p\rangle = \langle p|\mathcal{L}_N|p\rangle$$

$$s^{\mu}\Delta q \equiv \langle p | \overline{q} \gamma_{\mu} \gamma_{5} q | p \rangle$$

$$C_p + C_n = (c_u + c_d) (\Delta_u + \Delta_d) - 2\delta_s \quad [\delta_s \approx 5\%]$$

$$C_p - C_n = (c_u - c_d) (\Delta_u - \Delta_d)$$

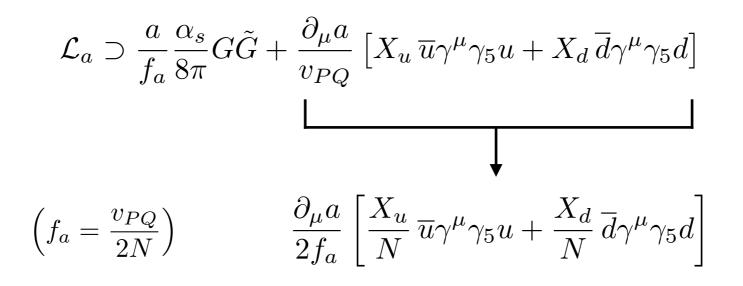
Independently of matrix elements:

(1):
$$C_p + C_n \approx 0$$
 if $c_u + c_d = 0$
(2): $C_p - C_n = 0$ if $c_u - c_d = 0$

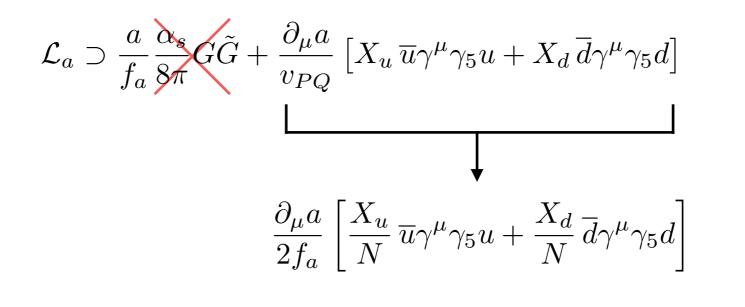


$$\mathcal{L}_a \supset \frac{a}{f_a} \frac{\alpha_s}{8\pi} G\tilde{G} + \frac{\partial_\mu a}{v_{PQ}} \left[X_u \,\overline{u} \gamma^\mu \gamma_5 u + X_d \,\overline{d} \gamma^\mu \gamma_5 d \right]$$

KSVZ/DFSZ no-go



KSVZ/DFSZ no-go





$$\frac{X_u}{N} \to c_u = \frac{X_u}{N} - \frac{m_d}{m_d + m_u} \qquad \qquad \frac{X_d}{N} \to c_d = \frac{X_d}{N} - \frac{m_u}{m_d + m_u}$$

KSVZ/DFSZ no-go

$$\mathcal{L}_{a} \supset \frac{a}{f_{a}} \frac{\alpha_{s}}{8\pi} G\tilde{G} + \frac{\partial_{\mu}a}{v_{PQ}} \begin{bmatrix} X_{u} \,\overline{u}\gamma^{\mu}\gamma_{5}u + X_{d} \,\overline{d}\gamma^{\mu}\gamma_{5}d \end{bmatrix}$$
$$\frac{\partial_{\mu}a}{2f_{a}} \begin{bmatrix} \frac{X_{u}}{N} \,\overline{u}\gamma^{\mu}\gamma_{5}u + \frac{X_{d}}{N} \,\overline{d}\gamma^{\mu}\gamma_{5}d \end{bmatrix}$$

$$\frac{X_u}{N} \to c_u = \frac{X_u}{N} - \frac{m_d}{m_d + m_u} \qquad \frac{X_d}{N} \to c_d = \frac{X_d}{N} - \frac{m_u}{m_d + m_u}$$

st condition
$$0 = c_u + c_d = \frac{\Lambda_u + \Lambda_d}{N} - 1$$

2nd condition
$$0 = c_u - c_d = \frac{X_u - X_d}{N} - \underbrace{\frac{m_d - m_u}{m_d + m_u}}_{\simeq 1/3}$$

KSVZ/DFSZ no-go

Ist condition
$$0 = c_u + c_d = \frac{X_u + X_d}{N} - 1$$

$$\begin{cases}
\frac{\mathsf{KSVZ}}{X_u = X_d = 0} & -1 \\
\frac{\mathsf{DFSZ}}{N = n_g(X_u + X_d)} & \frac{1}{n_g} - 1
\end{cases}$$

KSVZ/DFSZ no-go

Nucleophobia can be obtained in DFSZ models with non-universal (i.e. generation dependent) PQ charges, such that

$$N = N_1 \equiv X_u + X_d$$

Ist condition
$$0 = c_u + c_d = \frac{X_u + X_d}{N} - 1$$

$$\begin{cases}
\frac{KSVZ}{X_u = X_d = 0} & -1 \\
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\end{cases}$$

L. Di Luzio (Pisa U.) - Rethinking the QCD axion

sin distances in g

Implementing nucleophobia

• <u>Simplification</u>: assume 2+1 structure $X_{q_1} = X_{q_2} \neq X_{q_3}$

$$N \equiv N_1 + N_2 + N_3 = N_1 \qquad \qquad N_1 = N_2 = -N_3$$

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• $N_2 + N_3 = 0$ easy to implement with 2HDM

$$\mathcal{L}_Y \supset \bar{q}_3 u_3 H_1 + \bar{q}_3 d_3 \tilde{H}_2 + (\bar{q}_3 u_2 \dots + \dots) + \bar{q}_2 u_2 H_2 + \bar{q}_2 d_2 \tilde{H}_1 + (\bar{q}_2 d_3 \dots + \dots)$$
 $\Rightarrow \mathcal{N}_{3^{rd}} = 2X_{q_3} - X_{u_3} - X_{d_3} = X_1 - X_2 \Rightarrow \mathcal{N}_{2^{nd}} = 2X_{q_2} - X_{u_2} - X_{d_2} = X_2 - X_1$

• Ist condition <u>automatically</u> satisfied

Implementing nucleophobia

• <u>Simplification</u>: assume 2+1 structure $X_{q_1} = X_{q_2} \neq X_{q_3}$

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• 2nd condition can be implemented via a 10% tuning

$$\tan \beta = v_2/v_1 \qquad c_u - c_d = \underbrace{\frac{X_u - X_d}{N}}_{c_{\beta}^2 - s_{\beta}^2} - \underbrace{\frac{m_d - m_u}{m_u + m_d}}_{\simeq \frac{1}{3}} = 0 \qquad \Longrightarrow \qquad c_{\beta}^2 \simeq 2/3$$

Flavour connection

Nucleophobia implies flavour violating axion couplings !

 $[\mathrm{PQ}_d, Y_d^{\dagger} Y_d] \neq 0 \qquad \longrightarrow \qquad C_{ad_i d_j} \propto (V_d^{\dagger} \mathrm{PQ}_d V_d)_{i \neq j} \neq 0$

e.g. RH down rotations become physical

Flavour connection

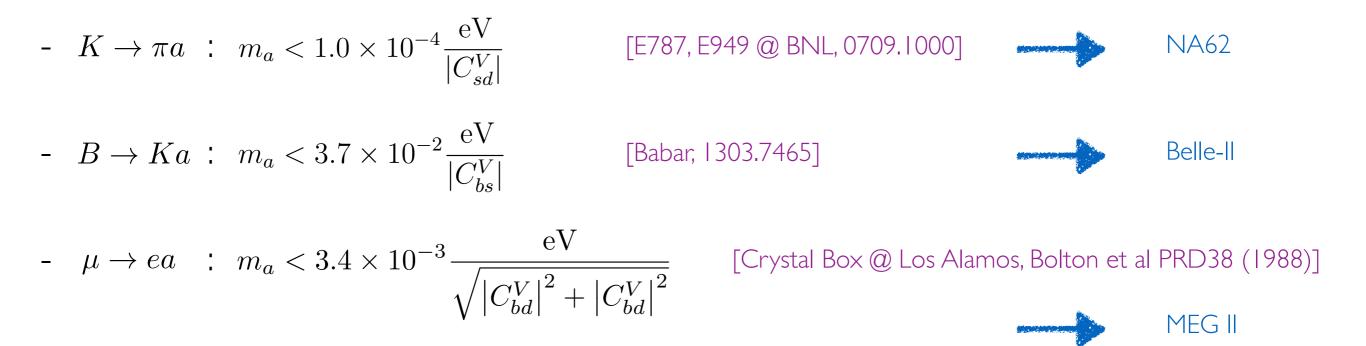
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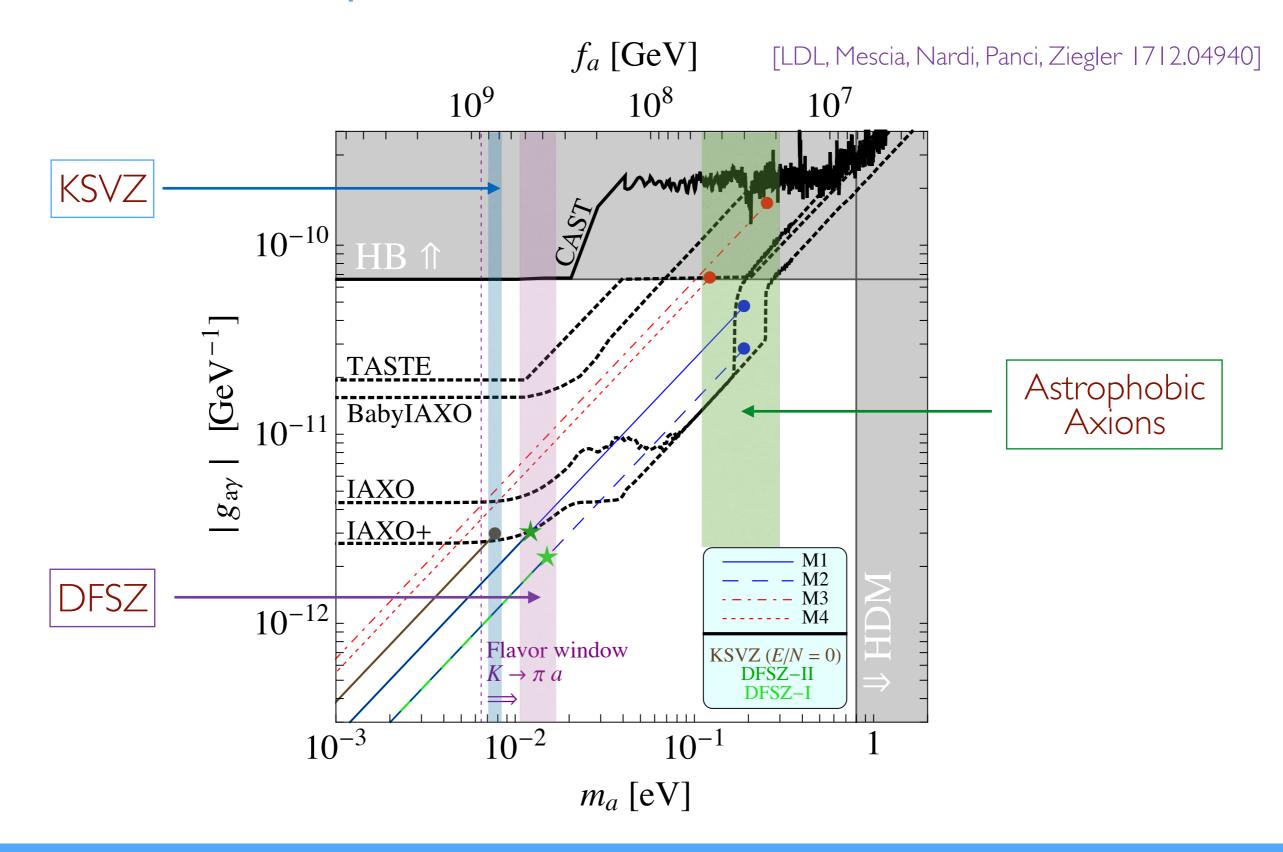
e.g. RH down rotations become physical

Plethora of low-energy flavour experiments probing

$$\frac{\partial_{\mu}a}{2f_a}\,\overline{f}_i\gamma^{\mu}(C^V_{ij}+C^A_{ij}\gamma_5)f_j$$



Astrophobic axion models





- QCD axion: 2 birds with 1 stone
 - solves the strong CP problem
 - provides an excellent DM candidate
- Healthy phase (experimentally driven)
 - we are entering <u>now</u> the preferred window for the QCD axion

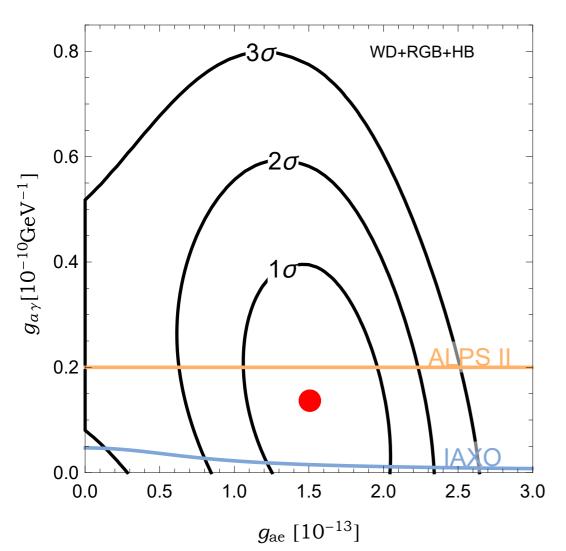


- QCD axion: 2 birds with 1 stone
 - solves the strong CP problem
 - provides an excellent DM candidate
- Healthy phase (experimentally driven)
 - we are entering <u>now</u> the preferred window for the QCD axion
- KSVZ and DFSZ are well-motivated minimal benchmarks, but...
 - axion couplings are UV dependent
 - worth to think about alternatives when confronting exp. bounds and sensitivities



Stellar cooling anomalies

- Hints of excessive cooling in WD+RGB+HB can be explained via an axion
- requires a sizeable axion-electron coupling in a region disfavoured by SN bound*





	Model	Global fit includes	$f_a \left[10^8 \mathrm{GeV} \right]$	$m_a \; [\mathrm{meV}]$	aneta	$\chi^2_{\rm min}/{ m d.o.f.}$
	DFSZ I	WD,RGB,HB	0.77	74	0.28	14.9/15
I		WD,RGB,HB,SN	11	5.3	140	16.3/16
		WD,RGB,HB,SN,NS	9.9	5.8	140	19.2/17
	DFSZ II	WD,RGB,HB	1.2	46	2.7	14.9/15
I		WD,RGB,HB,SN	9.5	6.0	0.28	15.3/16
		WD,RGB,HB,SN,NS	9.1	6.3	0.28	21.3/17

★ Nucleophobic axions should improve fit, allowing for fully perturbative Yukawas

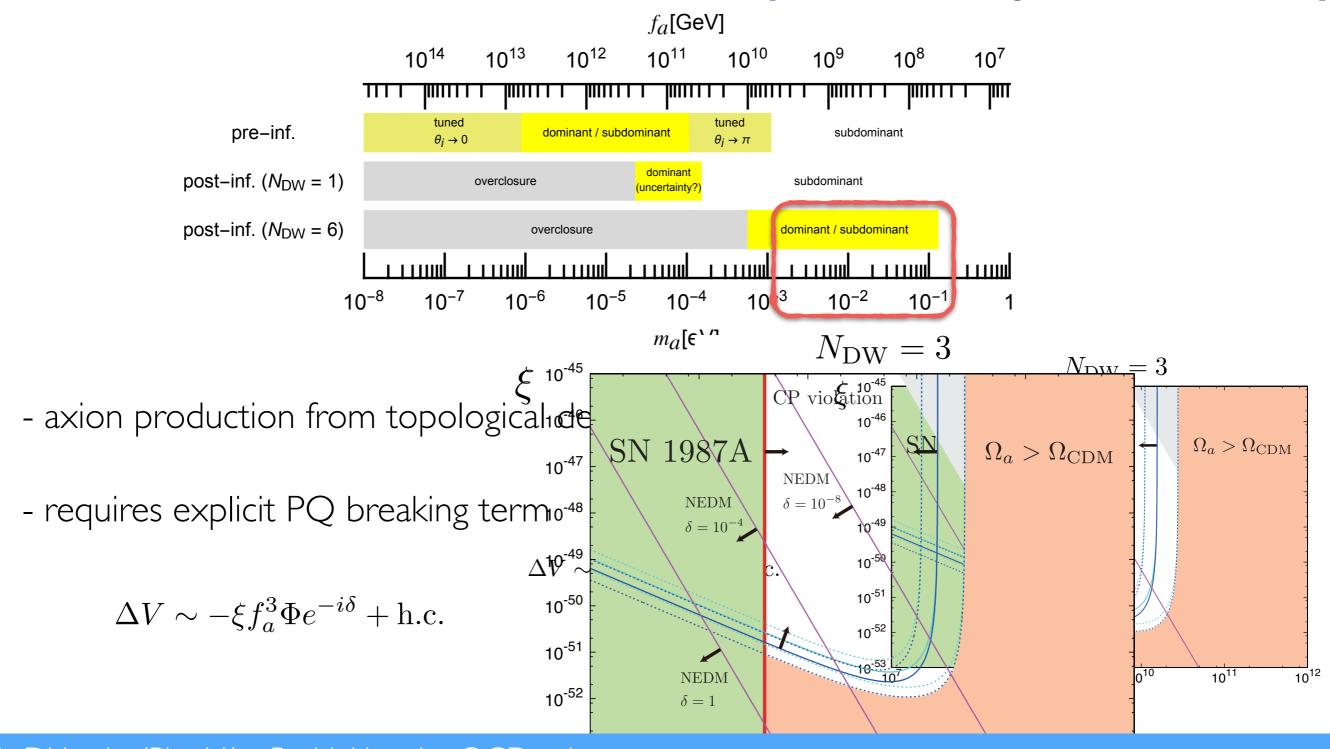
*SN bound a factor ~4 weaker than PDG one ?

[Chang, Essig, McDermott 1803.00993]

DM in the heavy axion window

• Post-inflationary PQ breaking with $N_{DW} \neq I$

[Kawasaki, Saikawa, Sekiguchi, 1412.0789 1709.07091]



Boosting E/N in DFSZ

• Potentially large E/N due to electron PQ charge

$$\frac{E}{N} = \frac{\sum_{j} \left(\frac{4}{3} X_{u}^{j} + \frac{1}{3} X_{d}^{j} + X_{e}^{j}\right)}{\sum_{j} \left(\frac{1}{2} X_{u}^{j} + \frac{1}{2} X_{d}^{j}\right)} \qquad \qquad \mathcal{L}_{Y} = Y_{u} \overline{Q}_{L} u_{R} H_{u} + Y_{d} \overline{Q}_{L} d_{R} H_{d} + Y_{e} \overline{L}_{L} e_{R} H_{e} + \text{h.c.}$$

- with n_H Higgs doublets and a SM singlet ϕ , enhanced global symmetry

$$U(1)^{n_H+1} \to U(1)_{\rm PQ} \times U(1)_Y$$

must be explicitly broken in the scalar potential via non-trivial invariants (e.g. $H_u H_d \Phi^2$)



non-trivial constraints on PQ charges of SM fermions

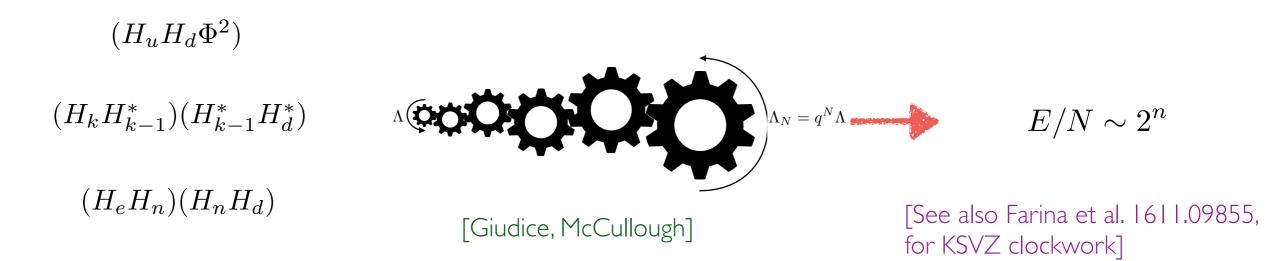
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 $\mathcal{L}_Y = Y_u \overline{Q}_L u_R H_u + Y_d \overline{Q}_L d_R H_d$ $+ Y_e \overline{L}_L e_R H_e + \text{h.c.}$

- Clockwork-like scenarios allow to boost E/N [LDL, Mescia, Nardi 1705.05370]
- n up-type doublets which *do not couple* to SM fermions (n ≤ 50 from LP condition)



Axion coupling to photons

• Axion effective Lagrangian

[See e.g. Grilli di Cortona et al., 1511.02867]

$$\mathcal{L}_a = \frac{1}{2} (\partial_\mu a)^2 + \frac{a}{f_a} \frac{\alpha_s}{8\pi} G_{\mu\nu} \tilde{G}^{\mu\nu} + \frac{1}{4} a g^0_{a\gamma\gamma} F_{\mu\nu} \tilde{F}^{\mu\nu} \qquad g^0_{a\gamma\gamma} = \frac{\alpha_{em}}{2\pi f_a} \frac{E}{N}$$

field-depended chiral transformation to eliminate aGGtilde:

 $q = \begin{pmatrix} u \\ d \end{pmatrix} \to e^{i\gamma_5 \frac{a}{2f_a}Q_a} \begin{pmatrix} u \\ d \end{pmatrix}$

 $\operatorname{tr} Q_a = 1$

Axion coupling to photons

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[See e.g. Grilli di Cortona et al., 1511.02867]

$$\mathcal{L}_{a} = \frac{1}{2} (\partial_{\mu} a)^{2} + \frac{a}{f_{a}} \frac{\alpha_{s}}{8\pi} \mathcal{C}_{\mu\nu} \tilde{G}^{\mu\nu} + \frac{1}{4} a g^{0}_{a\gamma\gamma} F_{\mu\nu} \tilde{F}^{\mu\nu} \qquad g^{0}_{a\gamma\gamma} = \frac{\alpha_{em}}{2\pi f_{a}} \frac{E}{N}$$

$$q = \begin{pmatrix} u \\ d \end{pmatrix} \rightarrow e^{i\gamma_{5}} \frac{a}{2f_{a}} Q_{a} \begin{pmatrix} u \\ d \end{pmatrix}$$

$$\mathcal{L}_a = \frac{1}{2} (\partial_\mu a)^2 + \frac{1}{4} a g_{a\gamma\gamma} F_{\mu\nu} \tilde{F}^{\mu\nu}$$

 $\operatorname{tr} Q_a = 1$



• Field content

Field	Spin	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$	$U(1)_{PQ}$
Q_L	1/2	\mathcal{C}_Q	\mathcal{I}_Q	\mathcal{Y}_Q	\mathcal{X}_L
Q_R	1/2	\mathcal{C}_Q	\mathcal{I}_Q	\mathcal{Y}_Q	\mathcal{X}_R
Φ	0	1	1	0	1

- PQ charges carried by a vector-like quark $Q = Q_L + Q_R$
 - original KSVZ model assumes Q ~ (3,1,0), but in general only $C_Q \neq I$ required

$$\partial^{\mu} J^{PQ}_{\mu} = \frac{N\alpha_s}{4\pi} G \cdot \tilde{G} + \frac{E\alpha}{4\pi} F \cdot \tilde{F} \qquad N = \sum_Q \left(\mathcal{X}_L - \mathcal{X}_R \right) T(\mathcal{C}_Q) \\ E = \sum_Q \left(\mathcal{X}_L - \mathcal{X}_R \right) \mathcal{Q}_Q^2 \qquad \} \text{ anomaly coeff.}$$

and a SM singlet Φ containing the "invisible" axion ($f_a \gg v$)

$$\Phi(x) = \frac{1}{\sqrt{2}} \left[\rho(x) + f_a \right] e^{ia(x)/f_a}$$

quences and this can be used to identify preferred and altheory aligned and the SAA cautoon of the SAA cautoon

KSVZ axions

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• Symmetry of the kinetic term

 $U(1)_{Q_L} \times U(1)_{Q_R} \times U(1)_{\Phi} \xrightarrow{y_Q \neq 0} U(1)_{PQ} \times U(1)_Q$ $\mathcal{L}_{PQ} = |\partial_u \Phi|^2 + \overline{Q} i D Q - (y_Q \overline{Q}_L Q_R \Phi + \text{H.c.})$

- U(1)_Q is the Q-baryon number: <u>if exact, Q would be stable</u>

cosmological issue if thermally produced in the early universe !



• Symmetry of the kinetic term

 $U(1)_{Q_L} \times U(1)_{Q_R} \times U(1)_{\Phi} \xrightarrow{y_Q \neq 0} U(1)_{PQ} \times U(1)_{Q}$

 $\mathcal{L}_{PQ} = |\partial_{\mu}\Phi|^2 + \overline{Q}iDQ - (y_Q\overline{Q}_LQ_R\Phi + H.c.)$

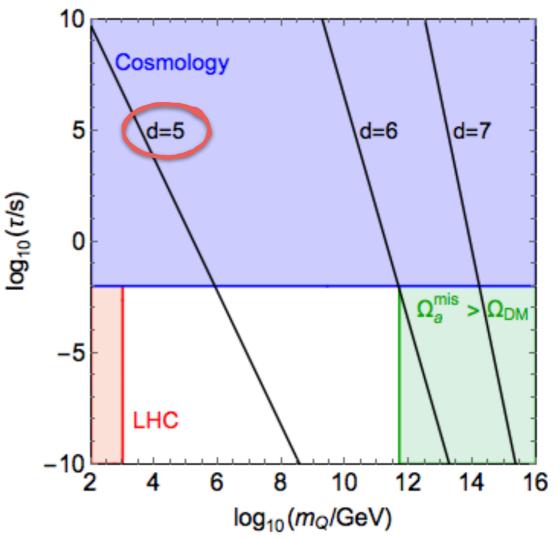
- $U(I)_Q$ is the Q-baryon number: if exact, Q would be stable
- if $\mathcal{L}_{Qq} \neq 0$ U(1)_Q is further broken and Q-decay is possible [Ringwald, Saikawa, 1512.06436]
- decay also possible via d>4 operators (e.g. Planck-induced)

Selection criteria

- We require: [for $T_{reheating} > m_Q \sim f_a$ (post-inflat. PQ breaking)]
 - I. Q sufficiently short lived $\tau_Q \lesssim 10^{-2} \text{ s}$
 - decays via d=4 operators are fast enough
 - decays via effective operators

$$\mathcal{L}_{Qq}^{d>4} = \frac{1}{M_{\text{Planck}}^{(d-4)}} \mathcal{O}_{Qq}^{d>4} + \text{h.c.}$$

$$\Gamma_{\rm NDA} = \frac{1}{4(4\pi)^{2n_f - 3}(n_f - 1)!(n_f - 2)!} \frac{m_Q^{2d - 7}}{M_{\rm Planck}^{2(d - 4)}}$$



Selection criteria

- We require: [for $T_{reheating} > m_Q \sim f_a$ (post-inflat. PQ breaking)]
 - I. Q sufficiently short lived $\tau_Q \lesssim 10^{-2}$ s
 - 2. No Landau poles below 10¹⁸ GeV
 - bound on Q multiplet dimensionality

$$\mu \frac{d}{d\mu} g_i = -b_i g_i^3 \qquad b_i = \text{gauge -matter}$$

0.020

0.015

 $\alpha_3/(4 \pi)$ 0.010

0.005

0.000

5

N.B. two-loop effects the diate if the diate if the diate is accidentally small below the cut-off Λ

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[LDL, Gröber, Kamenik, Nardec $\mathfrak{s}[0]$ (3),504.00359]



